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Dissemination models: applications in epidemiology, rumour spreading, wealth distribution, and opinion formation

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Dissemination Models

Applications in
epidemiology, rumour spreading,
wealth distribution, and opinion formation

Kit Ming Danny Chan

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Dissemination Models

Applications in
epidemiology, rumour spreading,
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