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Complex pathways in multistable matter

Meulblok, C.M.

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Complex pathways in multistable matter

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Colin Michel Meulblok
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in 1997

Promotor: Prof.dr. M.L. van Hecke

Co-promotor: Dr. M. Serra-Garcia

Promotiecommissie: Prof.dr. P.M. Reis EPFL, Zwitserland
Prof.dr. J.D. Paulsen St. Olaf College, VS
Prof.dr.ir. J.T.B. Overvelde TU Eindhoven
Prof.dr. D.J. Kraft
Prof.dr.ir. S.J. van der Molen

Inspired by Swallowtail by Salvador Dalí, this cover presents an artistic representation of complex pathways by Colin M. Meulblok. The front highlights path dependency, while the back emphasizes multiperiodic orbits.

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“We adore chaos because we love to produce order”

M.C. Escher

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