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## **The state of the earth: estimating physical parameters from noisy and incomplete earth observation data**

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