



Universiteit
Leiden
The Netherlands

The chemistry of planet-forming disks: a story from inner to outer disk

Temmink, M.

Citation

Temmink, M. (2026, June 5). *The chemistry of planet-forming disks: a story from inner to outer disk*. Retrieved from <https://hdl.handle.net/1887/4304669>

Version: Publisher's Version

License: [Licence agreement concerning inclusion of doctoral thesis in the Institutional Repository of the University of Leiden](#)

Downloaded from: <https://hdl.handle.net/1887/4304669>

Note: To cite this publication please use the final published version (if applicable).

PART I

Chemical and physical
structure of the inner disk

Chapter 2

MINDS: The DR Tau disk

I. Combining JWST-MIRI data with high-resolution CO spectra to characterise the hot gas

M. Temmink, E. F. van Dishoeck, S. L. Grant, B. Tabone, D. Gasman, V. Christiaens, M. Samland, I. Argyriou, G. Perotti, M. Güdel, T. Henning, P.-O. Lagage, A. Abergel, O. Absil, D. Barrado, A. Caratti O Garatti, A. M. Glauser, I. Kamp, F. Lahuis, G. Olofsson, T. P. Ray, S. Scheithauer, B. Vandenbussche, L. B. F. M. Waters, A. M. Arabhavi, H. Jang, J. Kanwar, M. Morales-Calderón, D. Rodgers-Lee, J. Schreiber, K. Scwharz, L. Colina

A&A, 686, A117 (2024)

Abstract

Context. The MRS mode of the JWST-MIRI instrument has been shown to be a powerful tool to characterise the molecular gas emission of the inner region of planet-forming disks. Investigating their spectra allows us to infer the composition of the gas in these regions and, subsequently, the potential atmospheric composition of the forming planets. We present the JWST-MIRI observations of the compact T-Tauri disk, DR Tau, which are complemented by ground-based, high spectral resolution ($R \sim 60000$ - 90000) CO ro-vibrational observations.

Aims. The aim of this work is to investigate the power of extending the JWST-MIRI CO observations with complementary, high-resolution, ground-based observations acquired through the SpExoDisks database, as JWST-MIRI's spectral resolution ($R \sim 1500$ - 3500) is not sufficient to resolve complex CO line profiles. In addition, we aim to infer the excitation conditions of other molecular features present in the JWST-MIRI spectrum of DR Tau and link those with CO.

Methods. The archival complementary, high-resolution CO ro-vibrational observations were analysed with rotational diagrams. We extended these diagrams to the JWST-MIRI observations by binning and convolution with JWST-MIRI's pseudo-Voigt line profile. In parallel, local thermal equilibrium (LTE) 0D slab models were used to infer the excitation conditions of the detected molecular species.

Results. Various molecular species, including CO, CO₂, HCN, and C₂H₂, are detected in the JWST-MIRI spectrum of DR Tau, with H₂O being discussed in a subsequent paper. The high-resolution observations show evidence for two ¹²CO components: a broad component (full width at half maximum of FWHM ~ 33.5 km s⁻¹) tracing the Keplerian disk and a narrow component (FWHM ~ 11.6 km s⁻¹) tracing a slow disk wind. The rotational diagrams yield CO excitation temperatures of $T \geq 725$ K. Consistently lower excitation temperatures are found for the narrow component, suggesting that the slow disk wind is launched from a larger radial distance. In contrast to the ground-based observations, much higher excitation temperatures are found if only the high- J transitions probed by JWST-MIRI are considered in the rotational diagrams. Additional analysis of the ¹²CO line wings suggests a larger emitting area than inferred from the slab models, hinting at a misalignment between the inner ($i \sim 20^\circ$) and the outer disk ($i \sim 5^\circ$). Compared to CO, we retrieved lower excitation temperatures of $T \sim 325$ - 900 K for ¹²CO₂, HCN, and C₂H₂.

Conclusions. We show that complementary, high-resolution CO ro-vibrational observations are necessary to properly investigate the excitation conditions of the gas in the inner disk and they are required to interpret the spectrally unresolved JWST-MIRI CO observations. These additional observations, covering the lower- J transitions, are needed to put better constraints on the gas physical conditions and they allow for a proper treatment of the complex line profiles. A comparison with JWST-MIRI requires the use of pseudo-Voigt line profiles in the convolution rather than simple binning. The combined high-resolution CO and JWST-MIRI observations can then be used to characterise the emission, in addition to the physical and chemical conditions of the other molecules with respect to CO. The inferred

excitation temperatures suggest that CO originates from the highest atmospheric layers close to the host star, followed by HCN and C₂H₂ which emit, together with ¹³CO, from slightly deeper layers, whereas the CO₂ emission originates from even deeper inside or further out of the disk.

2.1 Introduction

The majority of the exoplanet population are thought to form in the inner regions (<10 au) of planet-forming disks (Morbidelli et al. 2012; Dawson & Johnson 2018). The chemical composition of these regions and, subsequently, the accreting planetary atmospheres are dictated by their high temperatures and densities, in addition to the location of the H_2O and CO_2 snowlines (e.g. Pontoppidan et al. 2014; Walsh et al. 2015; Öberg & Bergin 2021; Bosman et al. 2022b; Mollière et al. 2022). Snowlines are the radial distances that dictate what elements are for 50% present in the gas and that are locked-up in the icy mantles of dust grains for the other 50%.

Over the recent years, the Atacama Large Millimeter/submillimeter Array (ALMA) has allowed us to characterise the chemical composition of the gas, dust, and ice in the outer regions of planet-forming disks with an unprecedented sensitivity, as over 30 molecular species and 17 rare isotopologues have been detected (e.g. Booth et al. 2021b; van der Marel et al. 2021a; Brunken et al. 2022; Furuya et al. 2022; McGuire 2022; Öberg et al. 2023; Booth et al. 2024b). The composition of the inner planet-forming zone is, however, hard to probe with ALMA, as an angular resolution of a few milli-arcseconds is required to resolve structures at 1 au scales in the nearest star-forming regions. These resolutions can only be achieved in the most extended configurations (C-10 with baselines of 16.2 km) for the highest frequencies (602-720 GHz in Band 9 and 787-950 GHz in Band 10) and are sensitive to only the dust continuum (see, for example, Andrews et al. 2018).

Recently, the Medium Resolution Spectroscopy (MRS; Wells et al. 2015; Argyriou et al. 2023) mode of the Mid-InfraRed Instrument (MIRI; Rieke et al. 2015; Wright et al. 2015, 2023) aboard the *James Webb Space Telescope* (JWST; Rigby et al. 2023) has provided a new opportunity to study the inner planet-forming regions. Within its wide wavelength range (4.9 to 28.1 μm), a large ensemble of molecular species (including CO, CO_2 , and H_2O) are covered. As JWST-MIRI only covers the highest J -transitions of the P branch of CO (i.e. $J \geq 25$ for the ^{12}CO $v=1-0$ P branch) at a low spectral resolution ($R \sim 3500$) and many T-Tauri disks are too bright for the JWST Near Infrared Spectrograph (NIRSpec), complementary observations are required to fully investigate the excitation and kinematics of CO. These spectrally resolved observations can be obtained with ground-based telescopes, such as the upgraded Cryogenic IR Echelle Spectrometer (CRIRES+) at the Very Large Telescope (VLT), the iSHELL instrument at the NASA Infrared Telescope Facility (IRTF), and/or Keck-NIRSPEC (e.g. Salyk et al. 2011a; Brown et al. 2013; Banzatti et al. 2022; Grant et al. 2023a).

In this work, we present the JWST-MIRI observations of DR Tau, an actively accreting ($\dot{M} \simeq 2 \times 10^{-7} M_{\odot} \text{ yr}^{-1}$; Manara et al. 2023) T-Tauri star ($M \simeq 0.93 M_{\odot}$, $L \simeq 0.63 L_{\odot}$; Long et al. 2019) located at a distance of ~ 195 pc (Gaia Collaboration et al. 2018) in the Taurus star-forming region. In addition, we used complementary, high spectral resolution CO ro-vibrational observations to fully investigate the CO excitation properties.

The chemical composition of its inner disk has been revealed with instruments such as VLT-CRIRES and *Spitzer*. Available spectra show that lines originating

from the inner part of the DR Tau disk have one of the highest line-to-continuum ratio and that a wide variety of molecular species are present (CO, CO₂, OH, H₂O, HCN and C₂H₂; Bast et al. 2011; Mandell et al. 2012; Brown et al. 2013; Banzatti et al. 2020). As we subsequently show, these are all also detected with JWST-MIRI. Other works on high spectral-resolution, infrared observations have shown that the ¹²CO line profile can consist of two components: one narrow component related to a possible disk wind, while the other one is broad and the result of the disk’s Keplerian rotation (Bast et al. 2011; Brown et al. 2013; Banzatti et al. 2022). We revisit this analysis with recent high-resolution observations. As JWST-MIRI also observes part of the CO ro-vibrational ladder, it will be of interest to investigate how these observations of a limited number of high-*J* levels compare with the full range of *J*-levels covered from the ground, especially since the disk of DR Tau is too bright for JWST-NIRSpec observations. Additionally, we investigate how the emitting radius provided by LTE slab models to fit the CO rotational ladder compares with the expected inner and emitting radius of CO, which can be derived from optically thin and/or well resolved line profiles using Kepler’s law (Salyk et al. 2011a; Banzatti & Pontoppidan 2015; Banzatti et al. 2020).

The outer disk can, on the other hand, be investigated with millimetre instruments. ALMA observations have shown that the dust disk is very compact, with a 95% effective radius of $\sim 0.28''$ or ~ 54 au (Long et al. 2019). At the current resolution ($\sim 0.1''$) of the ALMA data, no dust substructures have been detected, however, visibility- and super-resolution fitting techniques suggest that the disk may be comprised of two rings in the outer disk (respectively at ~ 22 au and ~ 42.5 au; Jennings et al. 2020, 2022b; Zhang et al. 2023). Furthermore, Jennings et al. (2022b) note that the visibilities hint at underresolved structures at small spatial scales, which likely point towards a partially resolved inner disk. The structure of the innermost region of the disk can be characterised with instruments on the Very Large Telescope Interferometer (VLTI) and the GRAVITY instrument has, in particular, shown that the inner disk of DR Tau ($i \sim 18^\circ$; GRAVITY Collaboration et al. 2021) may be misaligned with respect to the outer disk ($i=5.4$; Long et al. 2019).

The compact size of the millimetre-sized dust disk and potential hints of substructures make DR Tau a very interesting target to explore the role of the inward drift of icy pebbles in enhancing the emission seen in the inner disk. H₂O will be of importance in investigating the significance of radial drift, as shown by Banzatti et al. (2020, 2023a). In addition, Braun et al. (2021) derive a gas disk radius of 246 au based on ALMA observations of ¹³CO and C¹⁸O. This yields a gas-to-dust disk radius ratio of ~ 4.6 . As noted by Trapman et al. (2019) a ratio of >4 is a clear sign of dust evolution and radial drift, suggesting that drift is very effective in the disk of DR Tau and that the molecular emission in the inner disk may be enhanced.

This paper is structured as follows: in Sections 7.2 and 4.3 we describe, respectively, the data acquisition, reduction, and analysis methods, while Section 2.4 contains our results. The discussions can be found in Section 7.4. Section 4.6 contains the conclusions and a small summary. Furthermore, the H₂O emission

observed in DR Tau are investigated and discussed together with OH and first limits on H₁ and H₂ in a separate paper (Temminck et al. 2024a). Any H₂O slab models displayed will be further explained in that paper.

2.2 Observations

In the following subsections we describe the used observations (JWST-MIRI in Section 2.2.1 and IRTF-iSHELL in Section 2.2.3) and data reduction techniques. Additionally, we introduce our continuum subtraction method in Section 2.2.2.

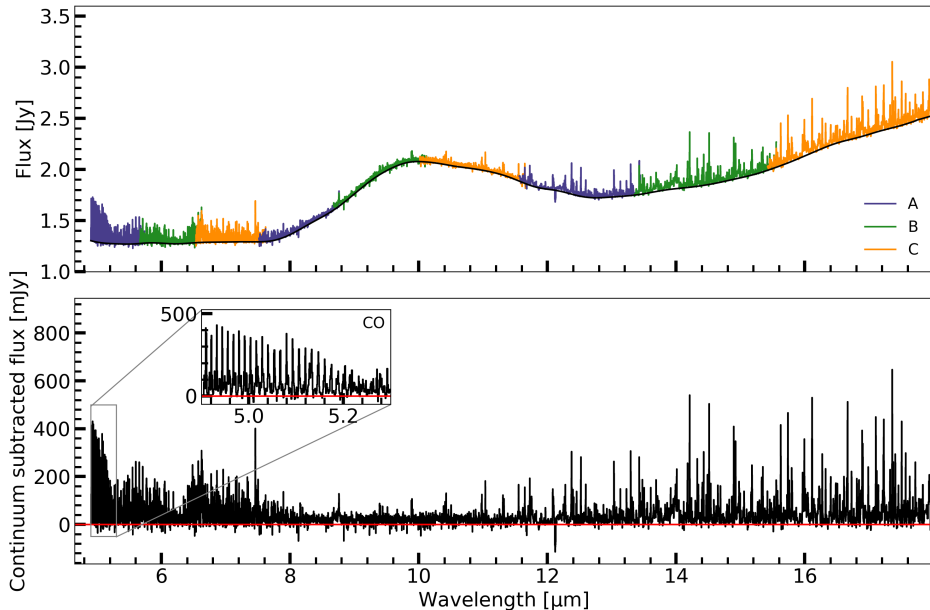


Figure 2.1: JWST-MIRI MRS spectrum of DR Tau over channels 1 through 3 (4.9-17.98 μm). The different wavelength ranges (subbands) of each MIRI channel are indicated in the top panel in blue (‘A’), green (‘B’), and orange (‘C’), respectively. The black line displays the estimated continuum. The bottom panel shows the continuum subtracted JWST-MIRI spectrum and contains a zoom-in on the CO transitions (4.9-5.3 μm). The red line in the bottom panel highlights the zero flux level.

2.2.1 JWST-MIRI observations

The MIRI/MRS observations of DR Tau have been taken as part of the MIRI mid-INfrared Disk Survey (MINDS; Henning et al. 2024) JWST Guaranteed Time Observations Program (PID: 1282, PI: T. Henning). The MRS mode involves 4 Integral Field Units: channel 1 (4.9-7.65 μm), channel 2 (7.51-11.71 μm), channel 3 (11.55-18.02 μm), and channel 4 (17.71-27.9 μm). As each channel consists of 3

wavelength subbands (respectively, A, B, and C), the MRS observations are comprised of a total of 12 wavelength bands. The data were taken in FASTR1 readout mode on March 4 2023, using a four-point dither pattern and a total on-source integration time of ~ 27.8 minutes.

A combination of the standard JWST pipeline (version 1.11.2, Bushouse et al. 2023a) and routines from the VIP package (Gomez Gonzalez et al. 2017; Christiaens et al. 2023), to compensate for known issues from the standard pipeline, have been used to reduce the data. Similar to the standard pipeline, the reduction pipeline is structured around the 3 main stages: Detector1, Spec2, and Spec3. We have skipped the background subtraction step in the Spec2 stage, and the outlier detection step in Spec3. The outlier detection step is known to introduce spurious artefacts in unresolved sources due to undersampling of the point-spread function (PSF). To compensate for the outlier detection, we have implemented the bad pixel correction routines from the VIP package. The bad pixels are identified through sigma-filtering and corrected through a Gaussian kernel. VIP-based routines have also been used for the centroiding of the central star. The frames of each spectral cube were aligned through an image cross-correlation algorithm, before a 2D Gaussian fit was used to identify the centroid location in the weighted mean image of the spectral cubes. These centroid locations are, subsequently, used for aperture photometry. We have extracted the spectrum by summing the signal in a 2.0 full-width half maximum (FWHM= $1.22 \lambda/D$, where $D \sim 6.5$ m is the diameter of the telescope) aperture centred on the source. To adjust for background emission, we have estimated the background from an annulus directly surrounding the aperture used for the aperture photometry. Aperture correction factors are used to account for the flux of the PSF outside the aperture and inside the annulus (Argyriou et al. 2023).

The calibrated JWST-MIRI spectrum of DR Tau over channels 1 through 3 is presented in Figure 3.1. The different MIRI subbands are displayed in different colours.

2.2.2 Continuum subtraction

Due to the line-richness of the DR Tau spectrum, we employed a different continuum subtraction method compared to Grant et al. (2023b) and Gasman et al. (2023). The method here relies on a baseline estimation using the PYBASELINES package (Erb 2022). Before estimating the baseline, we masked downward spikes, such that they cannot influence the estimate. The downward spikes were masked using the following method: the continuum level was roughly estimated using a Savitzky-Golay filter, consisting of window sizes of 100 data points and polynomials of order 3. Through an iterative process, we removed all emission lines which extended above 2σ of the standard deviation (STD) of the Savitzky-Golay filter. Once no emission lines remained, we subtracted the final Savitzky-Golay filter and considered all 3σ downward outliers from the residuals as downward spikes. These downward spikes were subsequently masked from the baseline estimation on the full spectrum. The baseline was estimated using the ‘Iterative Reweighted Spline Quantile Regression’ (IRSQR) method, which uses penalised splines and an iter-

ative reweighted least squares technique to apply quantile (using a value of 0.05) regression. Within the method, we have used cubic splines with knots every 75 points and differential matrices of order 3.

The estimated baseline and continuum-subtracted spectrum are displayed in the top and bottom panel of Figure 3.1, respectively. Appendix 2.A shows and explains the intermediate steps from the applied continuum subtraction method.

2.2.3 High-resolution CO observations

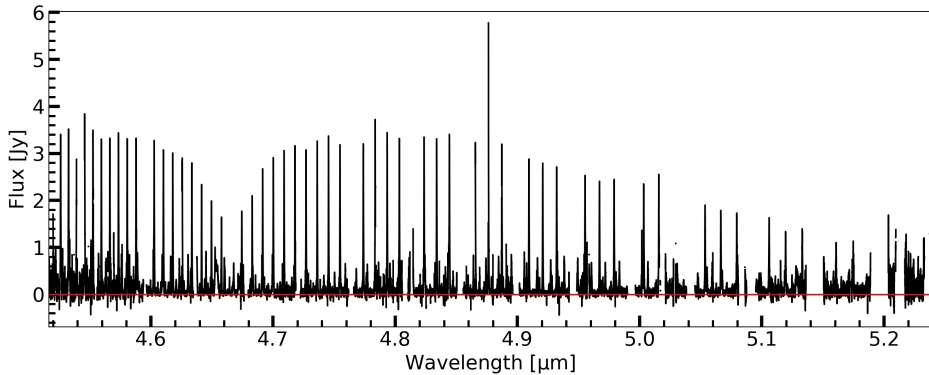


Figure 2.2: Continuum-subtracted iSHELL spectrum of DR Tau. The wavelength gaps visible in the spectrum have either not been observed, or were removed due to interference from telluric lines.

To complement the high- J levels of the CO P branch visible in the JWST spectrum at the shortest wavelengths ($<5.3 \mu\text{m}$), we have acquired high-resolution ($R \simeq 60000\text{-}92000$) IRTF-iSHELL (Rayner et al. 2016, 2022) data through SpExoDisks¹ (Wheeler et al. 2024). The iSHELL data were taken on January 23 2022 (see also Banzatti et al. 2022), were flux calibrated using the allWISE catalogue (WISE-W2: $\lambda=4.6 \mu\text{m}$, $F=1.91\pm 0.16 \text{ Jy}$; Wright et al. 2010; Cutri et al. 2013), and have been corrected for telluric features. As the allWISE flux calibration yields a small offset compared to the JWST-MIRI continuum, we have scaled the iSHELL observations by a factor ~ 0.71 , assuming that the flux at $\sim 5 \mu\text{m}$ is consistent across both observations. The required scaling may be the result of variability. However, as the iSHELL data were flux calibrated using WISE-W2 ($\lambda=4.6 \mu\text{m}$), JWST-NIRSpec observations are required to properly investigate variability. As DR Tau is too bright to observe with JWST-NIRSpec, this comparison cannot be made. The data extend over the wavelength range from approximately $\sim 4.516 \mu\text{m}$ to $\sim 5.239 \mu\text{m}$ and cover ro-vibrational transitions of ^{12}CO ($v=1\text{-}0$, $v=2\text{-}1$, and $v=3\text{-}2$) and ^{13}CO ($v=1\text{-}0$), several H_2O transitions, and the HI Pfund β ($\sim 4.655 \mu\text{m}$) and Humphreys ($\sim 4.675 \mu\text{m}$) lines. These data complement and extend upon the earlier VLT-CRIRES observations (at $R \simeq 100000$), see Bast et al.

¹SpExoDisks: <https://www.spexodisks.com/>

(2011), Brown et al. (2013), and Banzatti & Pontoppidan (2015).

Similar to the continuum subtraction method described in Section 2.2.2, we subtracted the baseline using the IRSQR-method. However, for the iSHELL data we did not mask any downward spikes, we used a quantile regression with a value of 0.10, and we placed the knots every 100 data points. The continuum-subtracted iSHELL data are presented in Figure 2.2. A comparison between the JWST-MIRI and iSHELL observations in the 4.9–5.1 μm region is displayed in Figure 2.3.

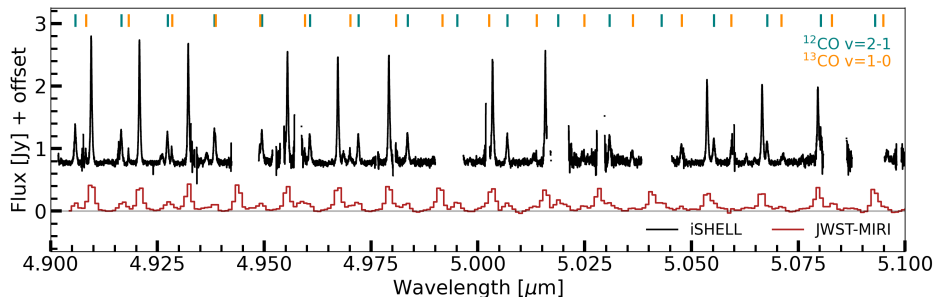


Figure 2.3: Comparison between the JWST-MIRI (red) and iSHELL (black) data within the wavelength region of 4.9–5.1 μm , to highlight the differences in flux and resolution. The iSHELL observations are offset by 0.75 Jy. The vertical lines at the top of the plot indicate the positions of the $^{12}\text{CO } v=2-1$ (teal) and $^{13}\text{CO } v=1-0$ (orange) transitions, to highlight the main contributors of the secondary CO emission peaks visible in this wavelength region.

2.3 Analysis

The following subsections provide an overview of the used techniques for obtaining the excitation properties. In Section 2.3.1 we describe our slab model retrieval process that has been used to characterise the emission from CO_2 , HCN, and C_2H_2 observed with JWST-MIRI. On the other hand, the techniques invoked for obtaining the CO line profiles and the rotational diagrams are described in Section 2.3.2.

2.3.1 LTE slab models

To extract information about the molecular features seen in the JWST-MIRI observations, we implement the same LTE slab model fitting procedure as described in Grant et al. (2023b); Gasman et al. (2023); Perotti et al. (2023), and Tabone et al. (2023). We have obtained the required spectroscopic data through the HITRAN database (Gordon et al. 2022). Our slab models assume Gaussian line profiles with a broadening of $\Delta V=4.7 \text{ km s}^{-1}$ ($\sigma=2 \text{ km s}^{-1}$), following Salyk et al. (2011b). In addition, we have accounted for the mutual shielding of adjacent lines in the Q branches of CO_2 , HCN, and C_2H_2 (see Tabone et al. 2023 for a description). We have convolved our CO_2 , HCN, and C_2H_2 models to a resolving power

of $\Delta\lambda/\lambda \sim 2500$. Finally, the SPECTRES package (Carnall 2017) was used to convolve the slab models to the JWST-MIRI wavelength grid.

The models consists of 3 free parameters that need to be varied to obtain the best fit to the molecular features: the column density N (in cm^{-2}), the gas temperature T (in K) and the emitting area πR_{em}^2 , which is parameterised by the emitting radius R_{em} (in au). We note that while the slab models are parameterised by a circular area, the observed emission may have a different emission morphology with an equivalent area. For example, the emission can originate from an annulus with an area equal to πR_{em}^2 .

To acquire the best combination of values for N , T , and R_{em} , we selected relatively isolated lines or regions of lines and used a reduced χ^2 analysis to fit the slab models to these lines:

$$\chi^2 = \frac{1}{N_{\text{obs}}} \sum_{i=1}^{N_{\text{obs}}} \frac{(F_{\text{obs},i} - F_{\text{mod},i})^2}{\sigma^2}. \quad (2.1)$$

Here, N_{obs} denotes the number of data points that were used for the fits, while F_{obs} and F_{mod} are, respectively, the observed and modelled continuum-subtracted fluxes. σ is the estimated noise. As opposed to Grant et al. (2023b) and Gasman et al. (2023), we have not estimated the noise from line-free regions, as those are not present in the extremely line-rich spectrum of DR Tau. Instead we base our values for σ on the median continuum flux level in each combination of channels and ranges, and divide this by the highly idealised signal-to-noise ratio (S/N) acquired through the JWST *Exposure Time Calculator* (ETC)². The median flux, obtained uncertainty and the estimate from the ETC for each subband can be found in Table 3.A.1. To account for the regions covering multiple subbands, we use a weighted average of the estimated uncertainties for each respective band. The adopted weights represent the number of data points used from each subband in the χ^2 -analysis and this yields a different value for σ for each molecule. We list the range of σ values for the molecules detected in Table 2.1. Our derived values for σ are higher than those found for GW Lup ($\sigma \sim 0.4$ mJy in Channel 3; Grant et al. 2023b) and Sz 98 ($\sigma \sim 1.8$ -9.6 mJy; Gasman et al. 2023), due to our adopted method. The confidence intervals for our fits are defined as $\chi_{\text{min}}^2 + 2.3$, $\chi_{\text{min}}^2 + 6.2$ and $\chi_{\text{min}}^2 + 11.8$ for 1σ , 2σ , and 3σ , respectively (Avni 1976; Press et al. 1992).

Throughout our χ^2 analysis we have used models based on the following grids for N , T and R_{em} : N ranged from 12 to 22 in \log_{10} -space, where we used a spacing of $\Delta(\log_{10}(N))=0.1$. For T , we have used a spacing of $\Delta T=25$ K and a range of $150 \leq T \leq 2500$ K. We note that R_{em} was allowed to vary between 0.01 au and 10 au, using steps of $\Delta R=0.02$ au.

2.3.2 CO line profiles and rotational diagrams

To obtain information about T , N , and R from the high-resolution ro-vibrational transitions of ^{12}CO and ^{13}CO we carried out a rotational diagram analysis on the integrated fluxes, following the method described in Appendix A of Banzatti

²ETC: <https://jwst.etc.stsci.edu/>

et al. (2012). We note that rotational diagram analyses and slab model fitting procedures are inherently the same, as long as the assumption of LTE is valid. We have assumed a Doppler broadening of $\delta V = 1 \text{ km s}^{-1}$. We note that using the same broadening as for the JWST-MIRI slab models ($\delta V = 4.7 \text{ km s}^{-1}$) in the rotational diagram analysis, the same excitation temperatures are inferred. However, the resulting column densities and emitting radii are found to be, respectively, higher and lower, while the total number of molecules is increased by less than 5%.

The required integrated fluxes have been obtained by, first, creating a weighted-averaged, normalised line profile, using the transitions that are unblended, not affected by telluric features, and have a high S/N -ratio. For the weighted average, we have used the errors on the flux as the weights. The line profile has been used to acquire one fixed value for the slight velocity offset (ΔV) from the heliocentric velocity ($\sim 27.6 \text{ km s}^{-1}$; Ardila et al. 2002) and for the FWHM.

For the ro-vibrational ladders of ^{12}CO ($v=1-0$, $v=2-1$, and $v=3-2$; see Section 2.4.2.2), we find that the line profile consists of two components: a narrow one, likely tracing an inner disk wind, and a broad one that traces the Keplerian rotation of the inner disk, as previously observed in Bast et al. (2011) and Brown et al. (2013). For these double components, we have used a double Gaussian line profile, whereas for the ^{13}CO $v=1-0$ transitions we have used a single Gaussian line profile. The line profiles were fitted using the python-package LMFIT (Newville et al. 2014). These line profiles have been used to obtain the integrated fluxes of a larger set of transitions, including lines that are partly blended with other transitions and/or have a lower S/N -ratio. For ^{12}CO $v=3-2$, no blended transitions are included, as we were unable to extract reasonable (compared with respect to the unblended lines) fluxes. The integrated fluxes have been acquired using the method described in Banzatti et al. (2012), based on the techniques provided in Pascucci et al. (2008); Najita et al. (2010) and Pontoppidan et al. (2010). In short, we invoke 1000 iterations of adding normally distributed noise to the observed flux. For each iteration, we determine the integrated flux and, subsequently, acquire a Gaussian distribution of measured line fluxes. We use the median of this distribution as the actual line flux and take the FWHM as the uncertainty.

To obtain information about both components, we carried out the rotational diagram analysis for all observed components separately. If the rotational diagrams consist of a straight line, the excitation temperature can be derived from the inverse of the slope of a fitted straight line, whereas the column density is given by the intercept. If the diagrams display curvature, which is an indication of optically thick emission (see Section 6.5.3.1), slab models must be used to properly derive the excitation conditions. Similarly as above, we have obtained the CO spectroscopic data from the HITRAN database. The best fitting values for T , N , and R_{em} have, similar to the slab-model fitting procedure, been acquired through a χ^2 -analysis, where σ in equation (4.7) now denotes the acquired error on the integrated flux. For the iSHELL data, we have used slightly different grids for the column density and temperature, but with the same step sizes: $14 \leq \log(N) \leq 22 \text{ cm}^{-2}$, $300 \leq T \leq 3000 \text{ K}$. For the emitting radius we adjusted both the grid and the stepsize into, respectively, $0.01 \leq R_{\text{em}} \leq 1 \text{ au}$ and $\Delta R_{\text{em}} = 0.001 \text{ au}$. We have used the same grid for the different isotopologues and vibrational transitions.

2.4 Results

We present the results of our analysis in the following subsections. In particular, we highlight the observed molecular species with JWST-MIRI (CO₂, HCN, and C₂H₂) in Section 2.4.1 and we provide an extensive analysis of the CO emission in Section 2.4.2, including our results regarding the excitation conditions, the line profiles, the optical depth, and the emitting radius.

2.4.1 JWST spectrum and detected molecules

The JWST-MIRI spectrum of DR Tau presented in Figure 3.1 is very line-rich. Most of the visible lines correspond to H₂O transitions, which are analysed in (Temminck et al. 2024a). Here, we focus on the molecules, besides H₂O and OH, for which transitions are covered by JWST-MIRI. The bottom panel of Figure 3.1 also contains a zoom-in on the CO transitions ($J \geq 25$), highlighting the strong emission features.

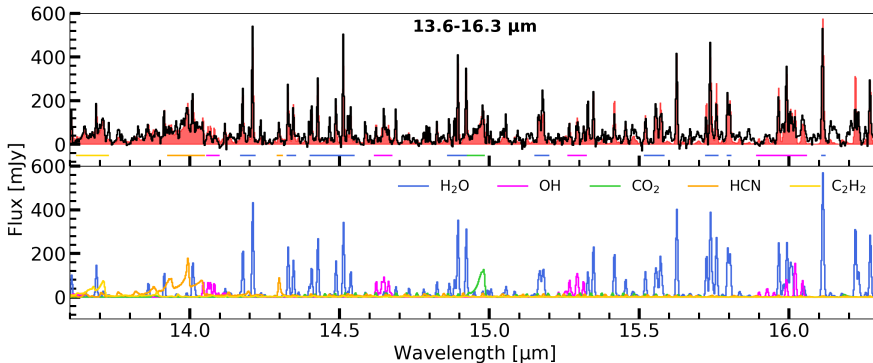


Figure 2.4: Best-fitting slab models of ¹²CO₂, HCN, and C₂H₂ in the 13.6-16.3 μm wavelength region. The top panel displays the continuum subtracted JWST spectrum in a specific region, while the full model spectrum is shown in red. In addition, the horizontal bars show for each molecule the spectral windows used in the χ^2 fits. The bottom panel shows the models for the individually detected molecules. The H₂O and OH slab models are shown for completeness. Their model properties are presented in (Temminck et al. 2024a)

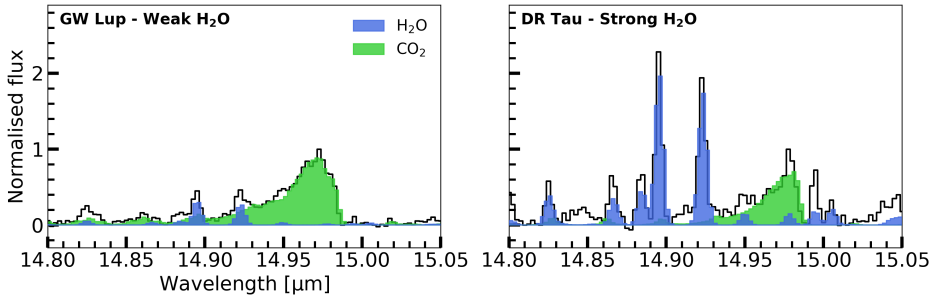
We detect emission from CO, CO₂, HCN, and C₂H₂. Table 2.1 displays the parameters of the best fitting slab models for CO₂, HCN, and C₂H₂. The uncertainties listed have been derived from the minimum and maximum value for each parameter that falls within the 1 σ -confidence interval. We also list the total number of molecules (\mathcal{N}), which is well constrained for optically thin emission. The total number of molecules has been calculated by multiplying the column density with the emitting area: $\mathcal{N} = N \pi R_{\text{em}}^2$. The best fitting slab models are displayed in Figure 3.B.1, whereas the χ^2 -maps are shown in Figure 2.C.1.

Table 2.1: Parameters of the best-fitting slab models for the different molecules observed with JWST-MIRI.

Molecule	$\log_{10}(N)$ [cm^{-2}]	T [K]	R_{em} [au]	\mathcal{N}
13.6-16.3 μm ($\sigma=2.19$ - 2.23 mJy)				
$^{12}\text{CO}_2$	$17.4^{+0.7}_{-0.2}$	325^{+50}_{-100}	$0.53^{+0.36}_{-0.06}$	4.96×10^{43}
HCN	$14.7^{+2.1}_{-0.6}$	900^{+50}_{-50}	$4.83^{+4.96}_{-4.38}$	8.22×10^{42}
C_2H_2	$15.0^{+5.6}_{-1.7}$	775^{+150}_{-625}	$1.45^{+8.56}_{-1.32}$	1.48×10^{42}

2.4.1.1 $^{12}\text{CO}_2$

The Q branch of $^{12}\text{CO}_2$ is well detected in DR Tau, whereas individual P - and R branch, and the hot-bands are not strongly detected. Our fit only extends over the Q branch, which yields a column density of $N=10^{17.4} \text{ cm}^{-2}$, a gas temperature of $T=325$ K and an emitting radius of $R=0.53$ au. Compared to H_2O , our $^{12}\text{CO}_2$ Q branch is significantly weaker. This is similar to Sz 98 (Gasman et al. 2023) and EX Lup (Kóspál et al. 2023), but totally the opposite for GW Lup (Grant et al. 2023b) and PDS 70 (Perotti et al. 2023). The difference with GW Lup is also visualised in Figure 2.5, which displays a zoom-in on the normalised $^{12}\text{CO}_2$ Q branch. As opposed to GW Lup, we do not detect any emission signature from $^{13}\text{CO}_2$.

**Figure 2.5:** Zoom-in on the $^{12}\text{CO}_2$ Q branch (14.80-15.05 μm) of GW Lup (left; Grant et al. 2023b) and DR Tau (right). Both spectra have been scaled to a common distance of 150 pc and normalised to the peak of the $^{12}\text{CO}_2$ Q branch.

2.4.1.2 HCN & C_2H_2

Similar to GW Lup (Grant et al. 2023b), but contrarily to PDS 70 (Perotti et al. 2023), we detect HCN and C_2H_2 in the wavelength region of 13.6-16.3 μm . The HCN Q branch ($\sim 14 \mu\text{m}$) and hot-band ($\sim 14.3 \mu\text{m}$) are both strongly detected. The emission is likely optically thin, which causes the column densities and emitting radius to be degenerate (see also Figure 2.C.1). Nonetheless, our best-fitting slab model suggests a column density of $N=10^{14.7} \text{ cm}^{-2}$, a temperature of $T=900$

K, and an emitting radius of $R=4.83$ au.

The parameters of C_2H_2 ($\sim 13.7 \mu\text{m}$) are much less constrained compared to those of HCN. Similar to GW Lup, the inferred column density is on the border between optically thin and thick, which adds another degeneracy: for high column densities, there is a degeneracy between the column density and the gas temperature. For C_2H_2 we find a best-fitting column density of $N=10^{15.0} \text{ cm}^{-2}$, a temperature of $T=775$ K, and a emitting radius of $R=1.45$ au.

2.4.2 CO analysis

As the main focus of this paper is the CO emission and a comparison between the JWST-MIRI and IRTF-iSHELL observations, this following section presents the results of the extensive CO analysis.

2.4.2.1 ^{12}CO as seen by JWST-MIRI

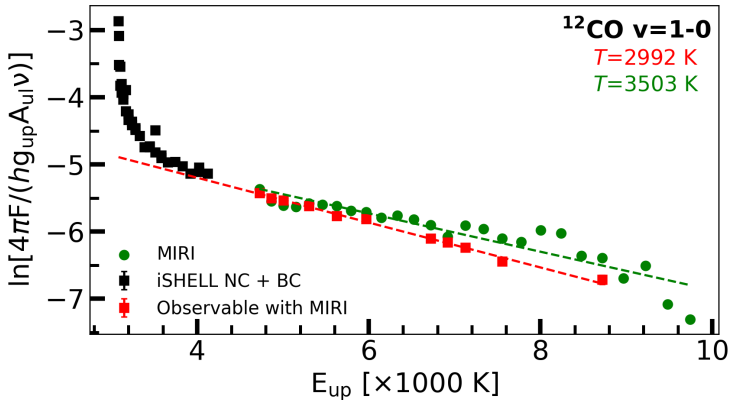


Figure 2.6: Rotational diagram of the ^{12}CO $v=1-0$ transitions. As JWST-MIRI is unable to distinguish between the narrow (NC) and broad (BC) components, their contributions have been added together. The black squares indicate the fluxes inferred from the iSHELL observations, while the ones marked denote the transitions that are also observable with JWST-MIRI. Errorbars on the iSHELL observations are plotted, however, these are too small with respect to the size of the squares. The circles in green are the integrated fluxes inferred from the JWST-MIRI observations using a pseudo-Voigt profile. The red, dashed line is a fit to the red points, used to derive what excitation temperature JWST-MIRI would probe as seen with the iSHELL observations ($T=2992\pm 40$ K). The green dashed line indicates the excitation temperature derived from these observations, $T=3503_{-269}^{+318}$ K.

For molecules, such as CO, with well identified individual ro-vibrational lines, the excitation is commonly analysed by plotting the integrated fluxes in a rotational diagram. Figure 2.6 shows in green the measured JWST-MIRI fluxes of ^{12}CO using a pseudo-Voigt profile (Labiano et al. 2021), assuming that the observable

flux originates in the $v=1-0$ lines, that is, we ignore any blending with the ^{12}CO $v=2-1$, $v=3-2$, and ^{13}CO $v=1-0$ transitions. Recall that JWST-MIRI only probes the transitions with the largest J values ($J \geq 25$) of the ^{12}CO P branch.

The temperature, T_{ex} , derived from such a rotational is given by the inverse of the slope, whereas the column density can be obtained from the intercept. For ^{12}CO , we acquire a temperature as high as $T_{\text{ex}}=3503_{-269}^{+318}$ K and a column density as low as $1.3 \times 10^{17} \text{ cm}^{-2}$ assuming an emitting area with a radius of 0.4 au (see Table 2.2). However, this simple analysis assumes that the line emission is optically thin. If the emission is optically thick, the inferred temperature can be much higher than the actual kinetic temperature. As demonstrated by, for example, Herczeg et al. (2011) (see their Appendix D) and Francis et al. (2024), optically thick line emission introduces a curvature at medium J values. This curvature causes the high- J transitions (probed by JWST-MIRI) to mimic much higher excitation temperatures than the kinetic one when only those transitions are fitted in a diagram.

We emphasise this point by including the integrated iSHELL fluxes of the ^{12}CO $v=1-0$ transitions in Figure 2.6, with the black and red squares obtained by taking the sum over the narrow and broad components. The red squares mark the transitions that are observable with JWST-MIRI and, as seen in the Figure, some small differences are visible in the measured fluxes with respect to JWST-MIRI, as we have not accounted for the blending of lines in the JWST-MIRI spectrum. As shown in Figure 2.D.5, many of the ^{12}CO $v=1-0$ transitions are blended with other lines, while only a handful are unblended, some of which are highlighted in Figure 2.D.5, whereas a few more can be found at longer wavelengths ($\geq 5.18 \mu\text{m}$). Such blending will be worse for sources with higher intrinsic line wings (e.g. sources with outflows or galaxies), where one may not be able to detect any unblended line at all.

The iSHELL fluxes clearly show a curvature in the rotational diagrams. For comparison, we fitted a straight line to the iSHELL integrated fluxes that cover the JWST-MIRI wavelength range (the red squares). The fit yields an excitation temperature of $T_{\text{ex}}=2992 \pm 40$ K. As will be demonstrated in Section 2.4.2.2 (see Table 2.2), the inferred temperatures are much lower when the iSHELL observations are fitted over the full range of J values with a LTE slab model that accounts for optical depth. This demonstrates the importance of having information on the fluxes of the lower- J lines.

As mentioned before, JWST-MIRI's resolution is not sufficient to distinguish between the two components present in the complex line profile of ^{12}CO . The total ^{12}CO line profile can, on the other hand, only be marginally resolved with JWST-MIRI. For unblended ^{12}CO $v=1-0$ transitions (see Section 2.4.2.6), we infer values for the FWHM in the range of $\sim 84-100 \text{ km s}^{-1}$, which are slightly larger than JWST-MIRI's velocity resolution of $\sim 80 \text{ km s}^{-1}$ (Labiano et al. 2021). The narrow component, tracing the disk wind, could potentially be observed with JWST-MIRI as extended emission. However, no extended emission is observed in the CO lines.

2.4.2.2 iSHELL CO line profiles and rotational diagrams

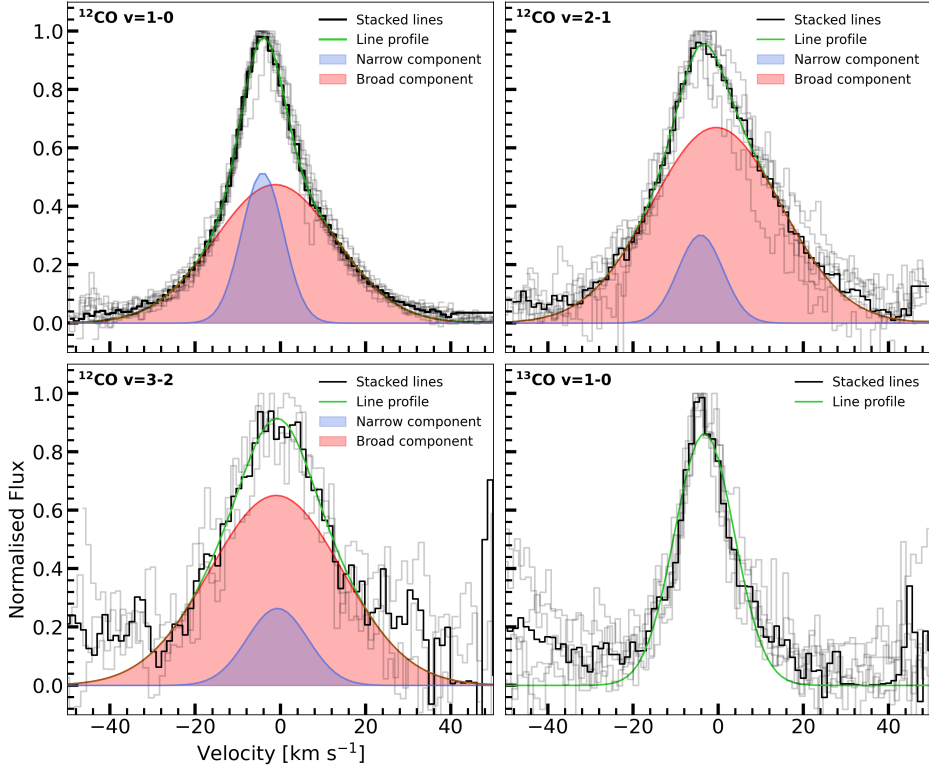


Figure 2.7: Fitted iSHELL line profiles for the $^{12}\text{CO } v=1-0$, $v=2-1$, $v=3-2$, and the $^{13}\text{CO } v=1-0$ transitions. The median line profile is shown in black, whereas the fitted line profile is shown in green. For the ^{12}CO transitions, we have indicated the narrow and broad components in, respectively, blue and red. The faint, grey line profiles visible in the background correspond to the individual line profiles used in creating the weighted-averaged, normalised line profile.

A proper analysis of the high-resolution, ground-based CO observations starts with a thorough analysis of the line profiles. The line profiles are displayed in Figure 2.7, whereas the acquired values for ΔV and the FWHM are listed in Table 2.2. The rotational diagrams themselves are displayed in Figure 2.8, while the best-fit parameters, for the broad and narrow components, are summarised, together with the values for the average FWHM and ΔV , in Table 2.2. The rotational diagrams (Figure 2.8) of the ^{12}CO vibrational ladders and $^{13}\text{CO } v=1-0$ transitions are presented separately. In addition, we separated out the narrow and broad components for ^{12}CO . For the broad component we find consistently higher integrated fluxes and excitation temperatures compared to those of the narrow one. All diagrams display an upward curvature at the lower end of the E_{up} range, suggesting optically thick emission. Optical depth is further discussed in Section

6.5.3.1. We do not list any uncertainties on the best fitting parameters (T and N), but they can be viewed in Figure 2.D.2. Models, based on the rotational diagrams, for the transitions of ^{12}CO $v=1-0$ (red), $v=2-1$ (blue), $v=3-2$ (green), and ^{13}CO $v=1-0$ (yellow) are displayed in Figure 2.D.1, while a zoom-in on the 4.68-4.72 μm region is shown in Figure 2.9, to provide a better view of how well the model fits the data.

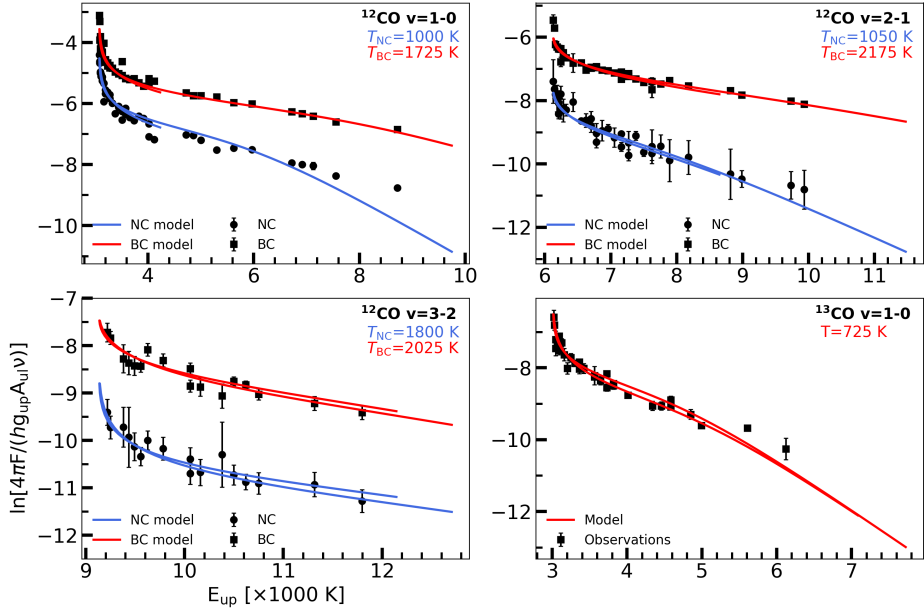


Figure 2.8: Rotational diagrams for ^{12}CO $v=1-0$ (top left), $v=2-1$ (top right), $v=3-2$ (bottom left), and ^{13}CO $v=1-0$ (bottom right). In each panel, the slab models are given by the solid line. For the ^{12}CO transitions, the narrow and broad components (NC and BC, respectively) are shown separately. The integrated fluxes for the narrow component are given by the dots, while those for the broad component are indicated by the squares. The two lines in each model correspond the R - and P branches.

We find column densities in the range of 1.6×10^{17} - 5.0×10^{18} cm^{-2} for the different transitions and temperatures of 725-2175 K. We find that the narrow components of the various ^{12}CO ro-vibrational transitions trace colder temperatures (respectively, 1000, 1050, and 1800 K) compared to the broad components (respectively, 1725, 2175, and 2025 K), confirming the different origins of the two components and suggesting that the broad component does trace the hot inner regions of the disk. For ^{13}CO we find a significantly lower temperature of 725 K, which is slightly higher than the value reported by Bast et al. (2011) and Brown et al. (2013) of $T=510$ - 570 K. However, both Bast et al. (2011) and Brown et al. (2013) used only transitions with $E_{\text{up}} \sim 3000$ - 4000 K, whereas our data include transitions with values of E_{up} up to ~ 6200 K.

Table 2.2: Best fit parameters acquired through the rotational diagram analysis for the iSHELL data.

Molecule	Vibr. Trans.	$\Delta V^{(\alpha)}$ [km s ⁻¹]	FWHM [km s ⁻¹]	N [cm ⁻²]	T [K]	R_{em} [au]	$\mathcal{N}^{(\beta)}$
¹² CO	v=1-0 (NC)	-4.2	11.6	3.2×10^{17}	1000	0.46	$>4.6 \times 10^{43}$
	v=1-0 (BC)	-1.2	33.5	6.3×10^{17}	1725	0.38	$>6.3 \times 10^{44}$
	v=2-1 (NC)	-4.1	12.5	7.9×10^{17}	1050	0.21	$>2.3 \times 10^{43}$
	v=2-1 (BC)	-0.5	35.8	5.0×10^{17}	2175	0.22	$>1.6 \times 10^{43}$
	v=3-2 (NC)	-0.7	16.9	5.0×10^{18}	1800	0.05	$>8.8 \times 10^{42}$
	v=3-2 (BC)	-1.0	36.6	1.6×10^{18}	2025	0.13	$>1.9 \times 10^{43}$
¹³ CO	v=1-0	-3.2	16.5	1.6×10^{17}	725	0.47	$>2.4 \times 10^{43}$
C ¹⁸ O	v=1-0	-4.2	10.3	2.0×10^{16}	975	0.23	7.4×10^{41}

Notes. (α): ΔV is the offset of the line centre with respect to the heliocentric velocity of DR Tau, ~ 27.6 km s⁻¹.

(β): As both ¹²CO and ¹³CO are found to be optically thick (see Section 6.5.3.1), the values listed for the total number of molecules must be treated as lower limits.

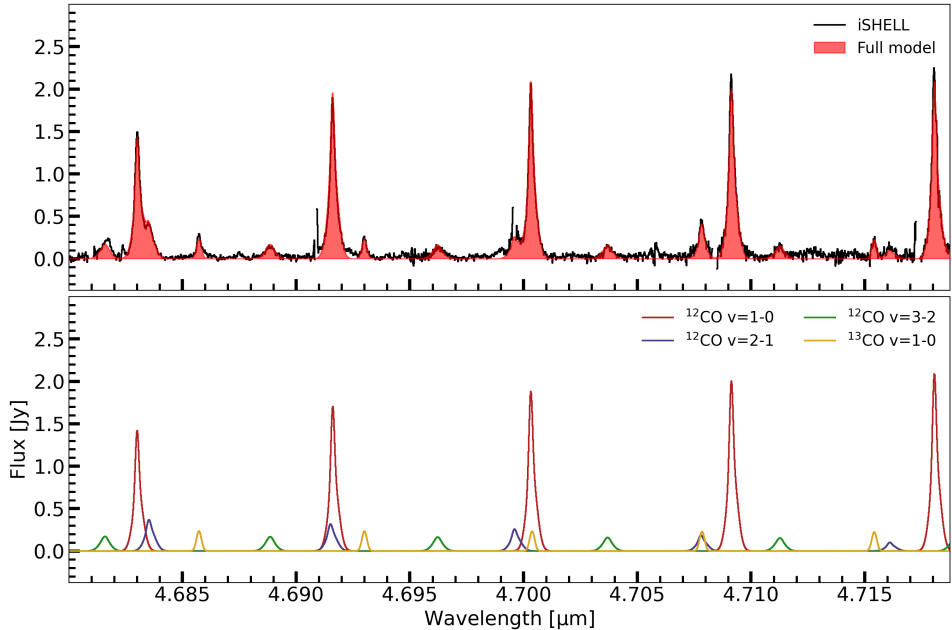


Figure 2.9: Zoom-in (4.68-4.72 μm) of the continuum-subtracted iSHELL spectrum of DR Tau with a model based on the best-fitting parameters obtained through the rotational diagram analysis. A full version can be found in Figure 2.D.1.

2.4.2.3 Optical depth: ^{12}CO and ^{13}CO

As previously found by Brown et al. (2013), the ^{12}CO emission of DR Tau is optically thick. Similarly as their Figure 11, Figure 2.D.3 displays the rotational diagrams of the ^{12}CO $v=1-0$, where we have combined the narrow and broad components, and ^{13}CO $v=1-0$ transitions together. In addition, we have multiplied the best fitting model of ^{13}CO by a factor of 68 to account for the isotopologue ratio as in the solar neighbourhood (Milam et al. 2005; $^{12}\text{C}/^{13}\text{C}=68\pm 15$). If ^{12}CO were optically thin, the scaled ^{13}CO model would have coincided with the ^{12}CO fluxes. However, we see that the scaled ^{13}CO lies above the ^{12}CO fluxes, confirming in a similar manner as Brown et al. (2013) that ^{12}CO is optically thick. Furthermore, ^{12}CO being optically thick is also confirmed by the shape of the line fluxes. As shown by Herczeg et al. (2011) (see their Figure D.1), for optically thin emission one would expect a straight line, whereas if the emission becomes optically thick the fluxes of the lines with higher upper level energies flatten off. Furthermore, as seen in Figure 2.D.3, the ^{13}CO $v=1-0$ model is also not completely a straight line, suggesting that the ^{13}CO is also (moderately) optically thick. However, as the ^{13}CO emission is less optically thick, a better lower limit on the total number of molecules can be obtained by multiplying the total number of molecules found for ^{13}CO by the isotopologue ratio of 68. This multiplication yields a total number of molecules of $\mathcal{N}_{\text{CO}} \simeq 1.6 \times 10^{45}$.

As the ^{13}CO emission is also (moderately) optically thick, rarer, less optically thick isotopologues are needed to infer the total amount of molecules. While C^{18}O is not detected in the iSHELL observations, the $v=1-0$ transitions are detected in the VLT-CRIRES data of Bast et al. (2011). For a description of the data, we refer to Bast et al. (2011) and Brown et al. (2013). We also scale the VLT-CRIRES data to match the JWST-MIRI flux at $\sim 5 \mu\text{m}$. Using the same approach as described in Section 2.2.3, we carry out a rotational diagram analysis for the C^{18}O $v=1-0$ transitions to obtain a better estimate for the total number of molecules.

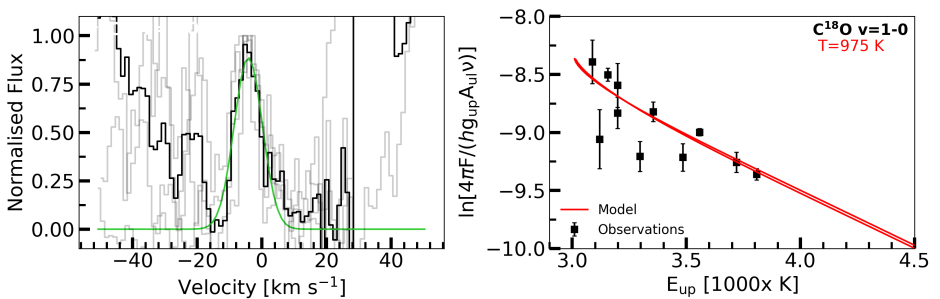


Figure 2.10: Inferred Gaussian line profile (left panel) and rotational diagram (right panel) for the C^{18}O $v=1-0$ transitions. The rotational diagram yields an excitation temperature of $T=975$ K.

First, for the C^{18}O line profile we find a velocity offset of $\Delta V = -4.2 \text{ km s}^{-1}$

with respect to DR Tau’s heliocentric velocity and a FWHM of 10.3 km s^{-1} . Second, the rotational diagram yields an excitation temperature of $T=975 \text{ K}$, a column density of $N=2.0 \times 10^{16} \text{ cm}^{-2}$, and an emitting radius of $R_{\text{em}}=0.23 \text{ au}$. The acquired line profile and rotational diagram are displayed in, respectively, the left and right panel of Figure 2.10. The χ^2 -map, visualising the uncertainties of the fit, is shown in the bottom right panel of Figure 2.D.2. The inferred excitation temperature for C^{18}O is found to be higher than that of ^{13}CO . However, the χ^2 -maps of C^{18}O show a large contour for the 1σ uncertainty, suggesting that the temperatures agree within the uncertainties. Finally, multiplying the column density by the corresponding emitting area yields a total number of molecules of $\mathcal{N}=7.4 \times 10^{41}$, which multiplied by the isotopologue ratio of $^{16}\text{O}/^{18}\text{O}=557 \pm 30$ (Wilson 1999) yields $\mathcal{N}_{\text{CO}}=4.1 \times 10^{44}$.

2.4.2.4 Estimated emitting radii of CO

Previous studies (e.g. Salyk et al. 2011a; Banzatti & Pontoppidan 2015; Banzatti et al. 2022) have shown that the emitting radius where the line flux peaks can be estimated from the line profiles using Kepler’s law, as the emission is broadened by the Keplerian rotation:

$$R = GM_* \left(\frac{\sin(i)}{\Delta v} \right)^2, \quad (2.2)$$

where i is the inclination and Δv is the line width, often taken to be equal to the half width at half maximum (HWHM). The inner emitting radius can, subsequently, also be estimated by taking Δv equal to the half width at 10% (HW10%; Banzatti et al. 2022). Both the HWHM and the HW10% have been derived from the averaged line profiles displayed in Figure 2.7, for simplicity we have taken the HWHM equal to half the FWHM listed in Table 2.2. Assuming the inclination of the inner disk of DR Tau to be equal to the inclination of the outer disk, we use $i=5.4^\circ$ (Long et al. 2019). Furthermore, as this method only applies to the lines broadened by the Keplerian rotation, we calculate the (inner) emitting radius only for the broad components of the different ^{12}CO line profiles and the $^{13}\text{CO} \text{ v}=1-0$ line profile. The calculated values are listed in Table 2.3.

All the calculated emitting radii (R_{CO}) differ significantly from those inferred through the rotational diagrams. One potential explanation for the differences can be found in the chosen value for the inclination. The used inclination has been derived from the continuum emission as probed by ALMA. However, inner disks can be misaligned with respect to the outer disk, for instance caused by perturbations induced by companions (see, for example, Bohn et al. 2022). By testing a wide variety of larger inclinations, we infer that inclinations of, respectively, 20.1° , 22.4° , 23.0° , and, 10.2° are required to match the corresponding emitting radii for the broad components of the various ^{12}CO vibrational transitions and the $^{13}\text{CO} \text{ v}=1-0$ transitions inferred from the rotational diagrams. This holds for the assumption that these emitting radii correspond to circular area enclosing the host star. As the high inferred excitation temperatures suggest that the emission of the broad component must originate from inside the dust sublimation radius, this assump-

Table 2.3: Derived (inner) emitting radii for the ro-vibrational transitions of ^{12}CO and ^{13}CO using an inclination of $i=5.4^\circ$.

Molecule	Vibr. Trans.	HWHM [km s $^{-1}$]	R_{CO} [au]
^{12}CO	v=1-0	16.8	0.03
	v=2-1	17.9	0.02
	v=3-2	18.3	0.02
^{13}CO	v=1-0	8.3	0.11
Molecule	Vibr. Trans.	HW10% [km s $^{-1}$]	$R_{\text{CO,in}}$ [au]
^{12}CO	v=1-0	29.5	0.01
	v=2-1	32.0	0.01
	v=3-2	32.7	0.01
^{13}CO	v=1-0	14.4	0.04

tion may be valid for DR Tau. Such a higher inferred inclination of the inner disk agrees with the value of $i_{\text{inner}} \sim 18_{-18}^{+10^\circ}$ derived by GRAVITY Collaboration et al. (2021) using VLTI-GRAVITY observations. It must be noted, however, that the uncertainties on this inclination also encompass the inclination of the outer disk ($i_{\text{outer}}=5.4_{-2.6}^{+2.1^\circ}$). Although this cannot yet be confirmed, the VLTI-GRAVITY observations and the CO line profiles both hint at a misalignment between the inner and outer disk.

2.4.2.5 LTE versus non-LTE

When using slab models or creating rotational diagrams, LTE is (almost) always assumed, but the question remains whether this is a valid assumption. A simple test to see if all ^{12}CO emission lines can be characterised by a single temperature can be carried out by using the ^{12}CO v=1-0 best-fit parameters for the v=2-1 transitions. If the v=1-0 parameters reproduce the observed v=2-1 fluxes, the emission can be considered in LTE. Otherwise, the vibrational excitation is in non-LTE and the various transitions need to be considered separately, as we have done for the high-resolution observations. The right panel of Figure 2.D.4 shows the model prediction of the ^{12}CO v=2-1 transitions using the best-fit parameters of the v=1-0 transitions (see Table 2.2). As can be seen, the model overpredicts the emission of the ^{12}CO v=2-1 transitions, confirming that the vibrational excitation is not in LTE. The various vibrational transitions thus need to be considered separately, while the rotational populations can still be in LTE.

Our findings are not surprising, considering the work by Bast et al. (2011). They find a higher vibrational temperature ($T \sim 1700$ K) for DR Tau, while only a temperature of $T \sim 500$ K for the rotational ^{13}CO lines. Higher vibrational temperatures are more commonly found for Herbig Ae/Be stars (e.g. Brittain et al. 2007 and van der Plas et al. 2015), which may be attributed to their higher UV fields and subsequent UV-pumping into the higher vibrational states. For

T-Tauri stars, UV-pumping into the higher vibrational states can be achieved through higher UV fluxes following accretion by the host star (Valenti et al. 2000). As DR Tau is known to be an actively accreting system, UV-pumping provides a possible explanation for the higher vibrational temperatures found by Bast et al. (2011).

2.4.2.6 Implication for JWST-MIRI analysis

While the LTE slab model of ^{12}CO fitted to the JWST-MIRI observations (see Table 2.1) roughly agrees with the excitation parameters found for the ^{12}CO $v=1-0$ broad component (see Table 2.2), these results must be treated with caution. As mentioned before, the JWST-MIRI observations do not have the spectral resolution to distinguish between the broad and narrow components observed for ^{12}CO and, as discussed in Section 2.4.2.5, the CO emission is not in LTE, suggesting that the observed emission cannot be described by a single temperature. In the following section, we explore how the slab models fitted to the rotational diagrams of the iSHELL observations can be used to describe the CO emission as observed by JWST-MIRI.

The main difference between the JWST-MIRI and iSHELL observations is the spectral resolution of JWST-MIRI, which does not allow one to distinguish between the narrow and broad components (this also holds for JWST-NIRSpec), as displayed in Figure 2.7. In addition, as mentioned before, the JWST-MIRI observations only cover the high- J transitions of the P branch. The excitation temperature as probed by JWST-MIRI would, subsequently, not only be affected by the combination of both components (likely approaching the weighted average of the two), but would also be biased to higher excitation temperatures following the inclusion of only transitions with high upper level energies. As discussed in Section 2.4.2.1 and displayed in Figure 2.6, a temperature of ~ 2992 K is acquired from the lines covered by JWST-MIRI, which is significantly higher than probed by the high-resolution iSHELL observations. Additionally, as shown in Figure 2.3, various transitions that are unblended in the iSHELL spectrum are blended in the JWST-MIRI one. Subsequently, it is harder to identify the contributions from the various (vibrational) transitions in JWST-MIRI's spectrum.

To be able to compare the CO emission observed with iSHELL and JWST-MIRI, and, more importantly, to show that we probe the same emission with both instruments, we bin our iSHELL model to JWST-MIRI's lower spectral resolution and convolve the binned model with JWST-MIRI's line profile. The binning was carried out using the python-package SPECTRES, whereas the convolution was implemented using ASTROPY and a kernel based on JWST-MIRI's line profile. As discussed in Labiano et al. (2021), JWST-MIRI's line profile is best described by a pseudo-Voigt profile, which is a weighted sum between a Gaussian and a Lorentzian profile (see Equation 2.3). In comparison, a normal Voigt profile is given by the convolution of a Gaussian and Lorentzian profile. To create the convolution kernel, we first identified the strongest, unblended ^{12}CO $v=1-0$ transitions in the JWST-MIRI spectrum. These lines are displayed in Figure 2.D.5. Subsequently, we created an average, normalised line emission profile, which is displayed

in Figure 2.D.6, by considering the 7 resolution elements enclosing the line peaks (blue shaded areas in Figure 2.D.5). Finally, we used LMFIT to fit a pseudo-Voigt profile to the averaged emission, which is also shown in Figure 2.D.6. The fitted pseudo-Voigt profile was, subsequently, adopted as our convolution kernel.

The used pseudo-Voigt profile is described by the following equation:

$$f(x; A, \mu, \sigma_f, \alpha) = \frac{(1 - \alpha)A}{\sigma_g \sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma_g^2} + \frac{\alpha A}{\pi} \left[\frac{\sigma_f}{(x - \mu)^2 + \sigma_f^2} \right]. \quad (2.3)$$

Here, A denotes the amplitude, μ the centre of the line, σ_f describes the width, and α gives the weights. Furthermore, σ_g is defined as $\sigma_g = \sigma_f / \sqrt{2 \ln(2)}$. Table 2.4 gives the best fitting values and their confidence intervals for A , μ , σ_f , and α .

Figure 2.11 shows our results: the top panel shows the full CO model on

Table 2.4: Best-fitting values and the corresponding confidence intervals for the pseudo-Voigt profile used to characterise the JWST-MIRI line profile.

Parameter ⁽¹⁾	Value	Confidence interval
A	2.99	± 0.22
μ	2.84	± 0.06
σ_f	1.03	± 0.08
α	0.76	± 0.20

Notes. (1): the units of the listed parameters are all arbitrary, see also Figure 2.D.6.

top of the iSHELL observations, whereas the middle and bottom panel shows the model on top of the JWST-MIRI data after applying the binning and convolution, respectively. As clearly shown in the middle panel, solely binning the high-resolution model down to JWST-MIRI's resolution does not provide a good fit, as the peak flux is clearly overproduced. The subsequent convolution, on the other hand, yields a good description of the JWST-MIRI observations, as is shown in the bottom panel. To conclude, by binning a high-resolution model to JWST-MIRI's spectral resolution and by convolving the model with JWST-MIRI's line profile, we have shown that the high-resolution observations can be used as a good template for the JWST-MIRI observations and that a proper treatment of the line profile is crucial.

We note that, even after convolution, the model does not provide a perfect fit to the JWST-MIRI observations. The small residual differences are potentially related to uncertainties of the flux calibration of the iSHELL observations or the different sensitivities of the instruments. In addition, stellar variability at the 20% level cannot be excluded as an explanation. Nonetheless, we have shown and argue that the best way to characterise the CO lines observed with JWST-MIRI is to combine them with high spectral resolution observations of ground-based instruments, such as iSHELL or VLT-CRIRES(+), that are publicly available for many sources through SpExoDisks.

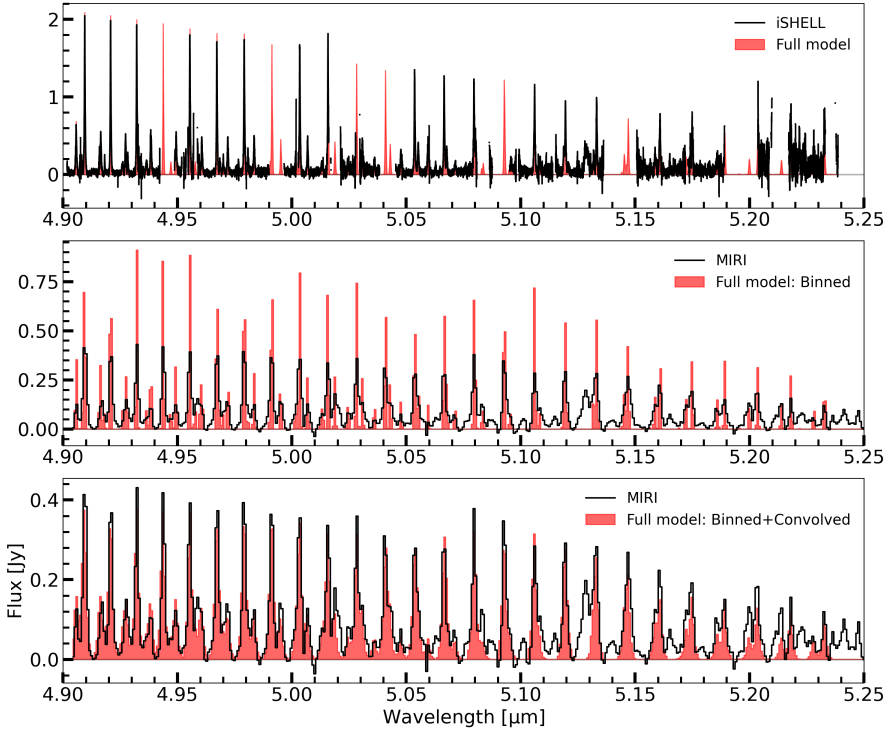


Figure 2.11: The top panel shows the continuum-subtracted iSHELL data (black) with the best-fitting model (red) based on the various slab model fits to the rotational diagrams over the 4.90-5.25 μm wavelength region. The middle panel shows the best fitting model binned to the JWST-MIRI resolution together with the JWST-MIRI observations, whereas the bottom panel shows the model convolved with the pseudo-Voigt profile shown in Figure 2.D.6.

2.4.2.7 JWST-MIRI line profile: Pseudo-Voigt versus Gaussian

As line profiles are often considered to be of pure Gaussian nature, we discuss in this subsection the different results one may acquire when treating JWST-MIRI's line profile as a Gaussian. When using a Gaussian line profile, we derive integrated fluxes that are 10% or less smaller than those acquired when using a pseudo-Voigt profile. Figure 2.D.7 compares the JWST-MIRI rotational diagrams when considering the different line profiles. A straight line fitted to the Gaussian integrated fluxes yields an excitation temperature of $T=3565^{+368}_{-305}$ K, which is slightly higher than the one ($T=3503^{+318}_{-269}$ K) probed when using a pseudo-Voigt profile. The temperatures do, however, agree well within the uncertainties.

In addition, we reproduce the analysis conducted in Section 2.4.2.6 for a Gaussian line profile, given by the first part of Equation 2.3 (setting $\alpha=0$). Figure 2.D.6 contains the fitted Gaussian line profile to the normalised, unblended ^{12}CO transitions, which is described by the following parameters: $A=2.40$, $\mu=2.85$, and

$\sigma_g=0.98$. The bottom panel of Figure 2.D.8 shows the convolution of the binned CO model with the Gaussian line profile. A close visual comparison between Figures 2.11 and 2.D.8 yields only small differences between the two convolutions: the main difference can, as expected, be found in the line wings of the convolved model. The Lorentzian contribution ensures that the pseudo-Voigt profile provides a better fit to the line wings compared to the Gaussian one. On the other hand, the Gaussian convolution can yield a model with slightly higher peak values, as less flux is distributed over the line wings.

Even though the Gaussian convolution yields similar results as the pseudo-Voigt one, the pseudo-Voigt profile, as found by Labiano et al. (2021), provides a significantly better description of the JWST-MIRI observations in subband 1A, as demonstrated by Figure 2.11. Depending on the application, a Gaussian profile may provide a sufficient fit to the observations, but one must take into consideration that the flux in the line wings will be underproduced.

An incorrect treatment of the line profile can also impact the analysis of the excitation conditions, as the underproduced line wings may result in an underestimation of the line fluxes. For example, the integral of the Gaussian line profile displayed in Figure 2.D.6 is $\sim 5\%$ lower than that of the Pseudo-Voigt line profile. Consequently, a rotational diagrams analysis can yield a lower value on the total column density and a different value for the excitation temperature, depending on how the slope is changed by these underestimated fluxes.

2.5 Discussion

2.5.1 CO excitation temperature as probed by JWST-MIRI

As shown in Figure 2.6, the excitation temperature derived when only considering the high- J transitions observed by JWST-MIRI, assuming optically thin emission, is significantly higher than that derived from a rotational diagram that includes also lower- J values. As discussed in Section 2.4.2.1, the higher excitation temperature follows from the fact that the ^{12}CO emission is optically thick. We emphasise the need for complementary observations when deriving the excitation properties of CO, either from space (e.g. with JWST-NIRSpec) or from the ground (e.g. with VLT-CRIRES(+), IRTF-iSHELL or Keck-NIRSPEC). If only space-based observations are used, we advise to treat the results with caution, since JWST-NIRSpec and JWST-MIRI do not have the spectral resolution to resolve the commonly observed, complex CO line profiles of planet-forming disks (see also Banzatti et al. 2022, 2023b).

2.5.2 Emitting region of CO

The high inferred excitation temperatures of $T \geq 1725$ K suggest that the broad component of the ^{12}CO emission must come from inside the dust sublimation radius ($T_{\text{dust}} \simeq 1500$ K) as also indicated in Figure 14 of Banzatti et al. (2022). Alternatively, the emission may originate from an elevated layer of the disk's atmosphere, where the gas temperature can be well above that of the dust. The

^{13}CO emission, on the other hand, should trace a deeper layer of the disk, as it is less optically thick compared to ^{12}CO , consistent with the lower probed excitation temperature. Depending on the flaring of the inner disks, the emission originating from these elevated emitting layers (as seen from the disk's midplane) could also explain the larger inclinations, or viewing angles, required for the emitting radii derived from the CO line profiles and slab models fitted to the rotational diagrams to match. Alternatively, a misalignment between the inner and outer disks, as hinted at by the VLTI-GRAVITY and ALMA observations, may also explain the required inclinations.

Thermo-chemical models have shown that the gas temperature in the inner regions of T-Tauri disks, in particular the elevated layers, can reach temperatures of ≥ 1000 K (Thi et al. 2013; Bruderer et al. 2015; Walsh et al. 2015; Woitke et al. 2018). These high temperatures further strengthen the notion that the CO emission must originate from the region inside of the dust sublimation radius and/or elevated layers of the disk.

2.5.3 Comparing the emitting properties of CO with the other molecules

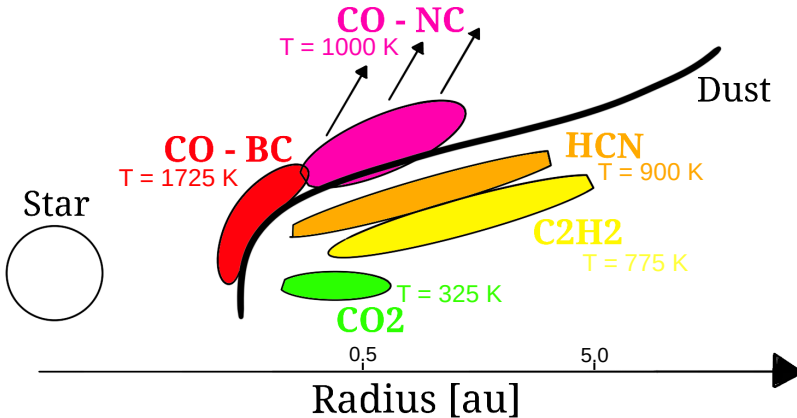


Figure 2.12: Cartoon visualising the expected emission regions, based on the slab models and interpreting the emitting radius as the disk radius, for our investigated molecules (CO, CO₂, HCN, and C₂H₂).

Compared with the other molecules studied here, CO₂, HCN, and C₂H₂, the excitation temperatures probed by CO are much higher. It must be noted that the temperatures inferred for CO₂, HCN, and C₂H₂ are similar to those in the other T-Tauri disks, GW Lup and Sz 98 (Grant et al. 2023b; Gasman et al. 2023). Models by Woitke et al. (2018) suggest that the emission likely originates from an onion-like structure, where CO has the highest emitting height and C₂H₂ the lowest. CO₂ and HCN originate from layers in between, with CO₂ originating from a slightly higher layer than HCN. Based on the derived excitation temperatures,

this is in partial disagreement with our slab modelling efforts, which suggest that the CO₂ emission should originate from either a deeper emitting layer or from a larger radial distance compared to that of HCN and C₂H₂. The expected emission regions, based on our slab models, for the investigated molecules are visualised in Figure 2.12. Since the same findings hold for the disks around GW Lup and Sz 98, additional (thermo)chemical modelling work is necessary to explain the observations and to infer from which layers these molecules originate from.

2.6 Conclusions & summary

In this work we have investigated the JWST-MIRI observations of the disk around the young star DR Tau. In addition, we have used complementary, high resolution CO ro-vibrational observations to fully investigate the emission properties of CO. Below we summarise our main conclusions:

- We have confirmed the detections of CO, ¹²CO₂, HCN, and C₂H₂ with JWST-MIRI, all of which have been observed before with Spitzer and from the ground. With JWST-MIRI we are now able to better constrain the excitation conditions and find excitation conditions of ¹²CO₂, HCN, and C₂H₂ for DR Tau that are similar to those derived for GW Lup and Sz 98. The conditions suggest that HCN and C₂H₂ originate from a layer higher up in the disk's atmosphere than ¹²CO₂.
- Using high-resolution IRTF-iSHELL observations we have thoroughly analysed the CO emission properties using slab model fits to rotational diagrams. These observations cover various transitions of ¹²CO v=1-0, v=2-1, and v=3-2, and ¹³CO v=1-0. Similar to previous studies, we note that the ¹²CO transitions are comprised of two components: a narrow and a broad component. The narrow part is linked to a potential inner disk wind, whereas the broad component is thought to arise from the Keplerian rotation of the disk. The high inferred temperatures (≥ 1725 K) for the broad component of the ¹²CO transitions suggest that the emission likely originates from a high atmospheric layer and/or from inside the dust sublimation radius.
- In addition to the emitting radii inferred from the slab models, we have calculated the emitting radii based on the line profiles, which are found to be significantly smaller than those inferred from the rotational diagrams. To match the emitting radii, we require higher inclinations (or viewing angles if the emission comes from a flared elevated layer) of the inner disk of $i \sim 10\text{-}23^\circ$, suggesting, under the assumption that the inferred emitting radii correspond to a circular emitting area enclosing the host star, that the inner disk of DR Tau may be slightly misaligned with the respect to the outer disk ($i_{\text{outer}} \sim 5^\circ$).
- Based on the flux ratios and curvature visible in the rotational diagrams, we find that the ¹²CO and ¹³CO transitions are optically thick. Using C¹⁸O transitions covered in VLT-CRIRES observations and applying the same

rotational diagram analysis, we have inferred a total number of molecules for CO in the inner disk (≤ 0.23 au) of DR Tau: $\mathcal{N}_{\text{CO}} \sim 4.1 \times 10^{44}$.

- Finally, we show that, to properly compare the JWST-MIRI and high-resolution, ground-based CO observations, one needs to bin the high-resolution model to JWST-MIRI’s spectral resolution and convolve the binned spectrum with a pseudo-Voigt profile.

With this work we emphasise that, although JWST-MIRI is a powerful instrument and is able to confidently detect the high- J transitions of CO, complementary, high-resolution observations are necessary to properly investigate the physical properties of the emitting gas. For DR Tau, the Keplerian CO emission must originate from inside the dust sublimation radius at temperatures of $T \geq 1725$ K, close to the host star. Other molecules, such as $^{12}\text{CO}_2$, HCN, and C_2H_2 are found to originate from farther out in the disk, with $^{12}\text{CO}_2$ likely originating from the deepest layer in the disk of DR Tau. In addition, the slow disk wind, as traced by the narrow component of ^{12}CO ($T \geq 1000$ K), is launched from a larger radial distance compared to the Keplerian emission.

Acknowledgements

The authors would like to thank Andrea Banzatti for the many very useful discussions.

This work is based on observations made with the NASA/ESA/CSA James Webb Space Telescope. The data were obtained from the Mikulski Archive for Space Telescopes at the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS 5-03127 for JWST. These observations are associated with program #1282. The following National and International Funding Agencies funded and supported the MIRI development: NASA; ESA; Belgian Science Policy Office (BELSPO); Centre Nationale d’Etudes Spatiales (CNES); Danish National Space Centre; Deutsches Zentrum für Luft- und Raumfahrt (DLR); Enterprise Ireland; Ministerio De Economía y Competividad; Netherlands Research School for Astronomy (NOVA); Netherlands Organisation for Scientific Research (NWO); Science and Technology Facilities Council; Swiss Space Office; Swedish National Space Agency; and UK Space Agency.

This research used the SpExoDisks Database at www.spexodisks.com

M.T. and E.v.D. acknowledge support from the ERC grant 101019751 MOLD-ISK. E.v.D. acknowledges support from the Danish National Research Foundation through the Center of Excellence “InterCat” (DNRF150). B.T. is a Laureate of the Paris Region fellowship program, which is supported by the Ile-de-France Region and has received funding under the Horizon 2020 innovation framework program and Marie Skłodowska-Curie grant agreement No. 945298. D.G., V.C., I.A., A.O., and B.V. thank the Belgian Federal Science Policy Office (BELSPO) for the provision of financial support in the framework of the PRODEX Programme of the European Space Agency (ESA). V.C. and A.O. acknowledge fund-

ing from the Belgian F.R.S.-FNRS. G.P. gratefully acknowledges support from the Max Planck Society. T.H. and K.S. acknowledge support from the European Research Council under the Horizon 2020 Framework Program via the ERC Advanced Grant Origins 83 24 28. D.B. and M.MC have been funded by Spanish MCIN/AEI/10.13039/501100011033 grants PID2019-107061GB-C61 and No. MDM-2017-0737. A.C.G. acknowledges from PRIN-MUR 2022 20228JPA3A “The path to star and planet formation in the JWST era (PATH)” and by INAF-GoG 2022 “NIR-dark Accretion Outbursts in Massive Young stellar objects (NAOMY)” and Large Grant INAF 2022 “YSOs Outflows, Disks and Accretion: towards a global framework for the evolution of planet forming systems (YODA)”. I.K., A.M.A., and E.v.D. acknowledge support from grant TOP-1 614.001.751 from the Dutch Research Council (NWO). I.K. and J.K. acknowledge funding from H2020-MSCA-ITN-2019, grant no. 860470 (CHAMELEON). T.P.R acknowledges support from ERC grant 743029 EASY. L.C. acknowledges support by grant PIB2021-127718NB-I00, from the Spanish Ministry of Science and Innovation/State Agency of Research MCIN/AEI/10.13039/501100011033.

Appendix

2.A Continuum subtraction

This section provides the immediate steps of the continuum subtraction described in Section 2.2.2. The necessary images are shown in Figure 2.A.1. The top panel of this figure shows the final Savitzky-Golay filter (green) after all $>2\sigma$ emission lines (light grey) have been filtered, together with the line-filtered spectrum. The middle panel displays the residuals after subtracting the Savitzky-Golay filter from the line-filtered spectrum. The green lines indicate the $-3\times$ level of the STD of the residuals. All the red crosses indicate the data points that lie below the $-3\times$ STD lines and have, subsequently, been masked throughout the baseline estimation. Finally, the bottom panel shows the full JWST-MIRI spectrum, together with the estimated baseline, and the masked data points.

2.B Uncertainties for the JWST-MIRI subbands

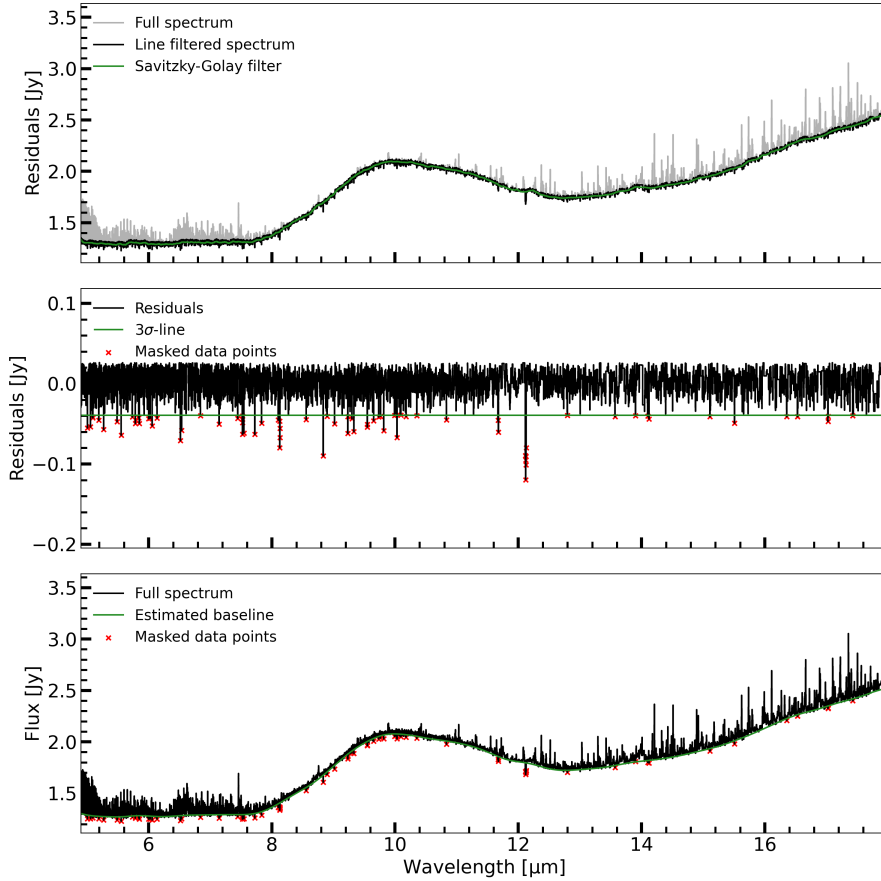


Figure 2.A.1: Intermediate steps of the continuum subtraction method described in Section 2.2.2. The top panel shows the final Savitzky-Golay filter (green) on the filtered line spectrum (black) and the filtered lines (light grey). The middle panel displays the residuals (black; line-filtered spectrum after subtracting the Savitzky-Golay filter), together with their $-3\times\text{STD}$ level (green), and the data points that fall below the $-3\times$ level (red crosses). The bottom panel shows the full JWST-MIRI spectrum (black) together with the estimated baseline (green) and the data points that have been masked throughout the estimation of the baseline (red crosses).

Table 2.B.1: Median continuum flux, estimated S/N from the ETC, and the acquired uncertainty σ for each subband.

Subband (μm)	Median flux [Jy]	ETC S/N	σ [mJy]
1A (4.90-5.74)	1.31	482.3	2.7
1B (5.66-6.63)	1.31	539.2	2.4
1C (6.53-7.65)	1.32	653.2	2.0
2A (7.51-8.77)	1.43	677.7	2.1
2B (8.67-10.13)	1.98	895.9	2.2
2C (10.02-11.70)	2.03	982.5	2.1
3A (11.55-13.47)	1.79	845.3	2.1
3B (13.34-15.57)	1.89	865.5	2.2
3C (15.41-17.98)	2.34	1030.3	2.3
4A (17.70-20.95)	2.74	425.0	6.4
4B (20.69-24.48)	2.85	246.3	11.6
4C (24.19-27.90)	2.69	76.6	35.2

2.C χ^2 -maps of CO₂, HCN, and C₂H₂

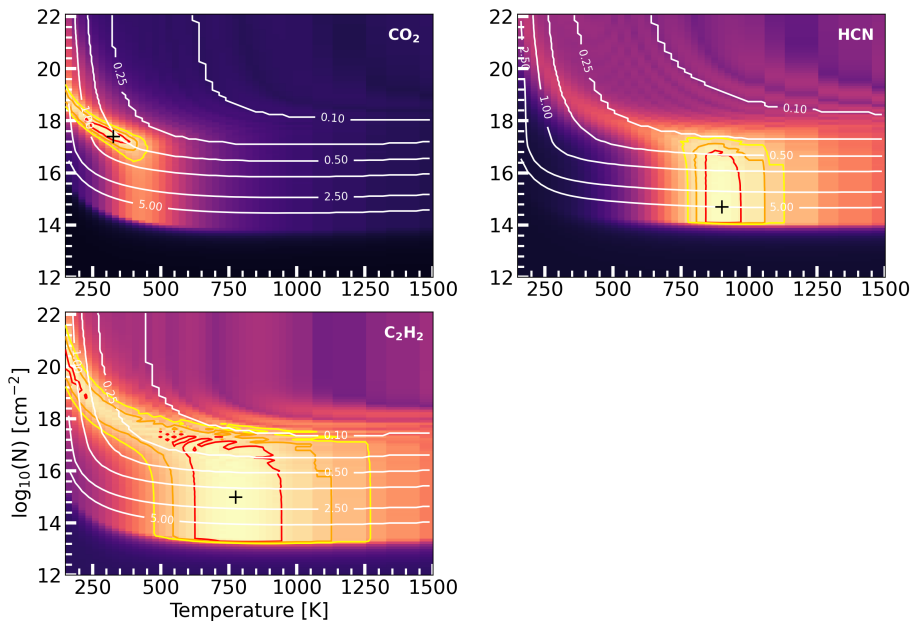


Figure 2.C.1: Normalised χ^2 maps (χ_{\min}^2/χ^2) for CO₂ (top left), HCN (top right), and C₂H₂ (bottom left). The dark plus indicates the best fitting parameters, while red, orange, and yellow contours indicate the 1 σ -, 2 σ -, and 3 σ -confidence intervals, respectively. The white contours indicate the emitting radii in au.

2.D Complementary CO ro-vibrational observations

2.D.1 Line information and integrated fluxes

Table 2.D.1: Information on the CO transitions used for the rotational diagrams and corresponding integrated fluxes.

Molecule	Rot. Trans.	Wavelength [μm]	E_{up} [K]	A_{ul} [s^{-1}]	g_{up}	Int. Flux ^(a)		Line prof. ^(b)	Blend ^(c)	
						Narrow comp. [$\text{erg s}^{-1} \text{cm}^{-2}$]	Broad comp.			
$^{12}\text{CO } v=1-0$	R-18	4.52589	4123.9	19.15	39	$1.98 \pm 0.05 \times 10^{-14}$	$1.34 \pm 0.03 \times 10^{-13}$	N	N	
	R-17	4.53237	4020.0	19.03	37	$2.04 \pm 0.05 \times 10^{-14}$	$1.38 \pm 0.03 \times 10^{-13}$	N	N	
	R-14	4.55236	3741.0	18.66	31	$2.84 \pm 0.17 \times 10^{-14}$	$1.12 \pm 0.04 \times 10^{-13}$	N	Y	
	R-13	4.55922	3658.9	18.52	29	$2.91 \pm 0.06 \times 10^{-14}$	$1.01 \pm 0.01 \times 10^{-13}$	N	Y	
	R-12	4.56617	3582.2	18.38	27	$3.00 \pm 0.09 \times 10^{-14}$	$9.77 \pm 0.17 \times 10^{-14}$	N	N	
	R-11	4.57323	3511.0	18.24	25	$2.99 \pm 0.06 \times 10^{-14}$	$9.75 \pm 0.20 \times 10^{-14}$	N	Y	
	R-10	4.58038	3445.3	18.08	23	$3.12 \pm 0.07 \times 10^{-14}$	$9.36 \pm 0.14 \times 10^{-14}$	N	N	
	R-9	4.58764	3385.1	17.91	21	$2.30 \pm 0.19 \times 10^{-14}$	$8.99 \pm 0.20 \times 10^{-14}$	N	Y	
	R-7	4.60244	3281.0	17.52	17	$3.00 \pm 0.07 \times 10^{-14}$	$8.86 \pm 0.12 \times 10^{-14}$	N	Y	
	R-6	4.61000	3237.1	17.28	15	$3.00 \pm 0.31 \times 10^{-14}$	$8.33 \pm 0.07 \times 10^{-14}$	N	Y	
	R-5	4.61766	3198.8	17.00	13	$2.92 \pm 0.06 \times 10^{-14}$	$7.86 \pm 0.12 \times 10^{-14}$	N	Y	
	R-4	4.62541	3165.9	16.65	11	$1.65 \pm 0.04 \times 10^{-14}$	$1.12 \pm 0.02 \times 10^{-13}$	N	N	
	R-3	4.63328	3138.5	16.20	9	$2.94 \pm 0.06 \times 10^{-14}$	$6.64 \pm 0.09 \times 10^{-14}$	Y	N	
	R-2	4.64124	3116.6	15.54	7	$2.39 \pm 0.04 \times 10^{-14}$	$5.88 \pm 0.07 \times 10^{-14}$	Y	N	
	R-1	4.64931	3100.1	14.42	5	$1.63 \pm 0.03 \times 10^{-14}$	$5.45 \pm 0.06 \times 10^{-14}$	Y	N	
	R-0	4.65749	3089.2	11.95	3	$1.13 \pm 0.04 \times 10^{-14}$	$4.43 \pm 0.06 \times 10^{-14}$	N	Y	
	P-1	4.67415	3083.7	35.46	1	$1.47 \pm 0.05 \times 10^{-14}$	$5.35 \pm 0.09 \times 10^{-14}$	N	N	
	P-2	4.68264	3089.2	23.51	3	$2.34 \pm 0.04 \times 10^{-14}$	$4.71 \pm 0.07 \times 10^{-14}$	N	Y	
	P-3	4.69124	3100.1	21.04	5	$2.46 \pm 0.04 \times 10^{-14}$	$5.27 \pm 0.16 \times 10^{-14}$	N	Y	
	P-4	4.69995	3116.6	19.92	7	$2.83 \pm 0.05 \times 10^{-14}$	$6.42 \pm 0.10 \times 10^{-14}$	N	Y	
	P-5	4.70877	3138.5	19.26	9	$3.03 \pm 0.05 \times 10^{-14}$	$7.26 \pm 0.09 \times 10^{-14}$	Y	N	
	P-6	4.71769	3165.9	18.80	11	$3.32 \pm 0.09 \times 10^{-14}$	$7.01 \pm 0.15 \times 10^{-14}$	Y	N	
	P-7	4.72673	3198.8	18.45	13	$2.75 \pm 0.08 \times 10^{-14}$	$7.73 \pm 0.13 \times 10^{-14}$	N	Y	
	P-8	4.73587	3237.1	18.17	15	$3.28 \pm 0.04 \times 10^{-14}$	$7.71 \pm 0.06 \times 10^{-14}$	Y	N	
	P-9	4.74513	3281.0	17.93	17	$3.35 \pm 0.07 \times 10^{-14}$	$8.10 \pm 0.10 \times 10^{-14}$	Y	N	
	P-10	4.75450	3330.3	17.71	19	$2.80 \pm 0.06 \times 10^{-14}$	$8.78 \pm 0.09 \times 10^{-14}$	N	Y	
	P-12	4.77358	3445.3	17.35	23	$2.98 \pm 0.06 \times 10^{-14}$	$8.70 \pm 0.08 \times 10^{-14}$	Y	N	
	P-13	4.78330	3511.0	17.19	25	$2.05 \pm 0.09 \times 10^{-14}$	$1.38 \pm 0.06 \times 10^{-13}$	N	N	
	P-14	4.79312	3582.2	17.03	27	$3.21 \pm 0.05 \times 10^{-14}$	$8.50 \pm 0.07 \times 10^{-14}$	N	N	
	P-17	4.82331	3828.5	16.61	33	$2.95 \pm 0.06 \times 10^{-14}$	$8.83 \pm 0.08 \times 10^{-14}$	N	Y	
	P-18	4.83361	3921.6	16.48	35	$2.85 \pm 0.06 \times 10^{-14}$	$8.26 \pm 0.22 \times 10^{-14}$	N	Y	
	P-19	4.84403	4020.0	16.35	37	$2.50 \pm 0.08 \times 10^{-14}$	$9.45 \pm 0.14 \times 10^{-14}$	N	Y	
	P-25	4.90912	4725.0	15.62	49	$2.19 \pm 0.04 \times 10^{-14}$	$8.66 \pm 0.07 \times 10^{-14}$	Y	N	
	P-26	4.92041	4861.5	15.50	51	$2.20 \pm 0.04 \times 10^{-14}$	$8.16 \pm 0.06 \times 10^{-14}$	Y	N	
	P-27	4.93182	5003.4	15.39	53	$1.94 \pm 0.07 \times 10^{-14}$	$8.36 \pm 0.12 \times 10^{-14}$	N	N	
	P-29	4.95504	5303.5	15.16	57	$1.48 \pm 0.10 \times 10^{-14}$	$8.50 \pm 0.16 \times 10^{-14}$	N	N	
	P-31	4.97878	5625.1	14.93	61	$1.65 \pm 0.07 \times 10^{-14}$	$7.38 \pm 0.16 \times 10^{-14}$	N	Y	
	P-33	5.00305	5968.2	14.71	65	$1.65 \pm 0.09 \times 10^{-14}$	$7.36 \pm 0.14 \times 10^{-14}$	N	N	
	P-37	5.05324	6718.9	14.28	73	$1.15 \pm 0.04 \times 10^{-14}$	$6.13 \pm 0.07 \times 10^{-14}$	N	N	
	P-38	5.06613	6920.0	14.17	75	$1.11 \pm 0.05 \times 10^{-14}$	$5.90 \pm 0.08 \times 10^{-14}$	N	N	
	P-39	5.07917	7126.4	14.06	77	$1.08 \pm 0.12 \times 10^{-14}$	$5.50 \pm 0.22 \times 10^{-14}$	N	Y	
	P-41	5.10568	7555.1	13.85	81	$8.02 \pm 0.58 \times 10^{-15}$	$4.73 \pm 0.11 \times 10^{-14}$	N	Y	
	P-46	5.17452	8719.7	13.32	91	$5.76 \pm 0.43 \times 10^{-15}$	$3.90 \pm 0.29 \times 10^{-14}$	N	Y	
	$^{12}\text{CO } v=2-1$	R-22	4.55692	7625.6	37.63	47	$3.86 \pm 0.83 \times 10^{-15}$	$2.91 \pm 0.72 \times 10^{-14}$	N	Y
		R-21	4.56309	7501.1	37.43	45	$3.85 \pm 0.52 \times 10^{-15}$	$3.47 \pm 0.09 \times 10^{-14}$	N	Y
		R-19	4.57573	7268.3	37.01	41	$3.12 \pm 0.54 \times 10^{-15}$	$4.13 \pm 0.11 \times 10^{-14}$	N	Y
R-18		4.58219	7159.9	36.79	39	$5.77 \pm 0.38 \times 10^{-15}$	$3.25 \pm 0.07 \times 10^{-14}$	N	Y	
R-17		4.58875	7057.0	36.57	37	$4.86 \pm 1.49 \times 10^{-15}$	$3.75 \pm 0.26 \times 10^{-14}$	N	N	
R-14		4.60902	6780.5	35.86	31	$3.46 \pm 0.63 \times 10^{-15}$	$3.62 \pm 0.12 \times 10^{-14}$	N	Y	
R-13		4.61598	6699.2	35.60	29	$5.34 \pm 1.10 \times 10^{-15}$	$3.29 \pm 0.18 \times 10^{-14}$	Y	N	
R-12		4.62303	6623.2	35.33	27	$5.86 \pm 1.25 \times 10^{-15}$	$2.86 \pm 0.22 \times 10^{-14}$	N	N	
R-11		4.63019	6552.7	35.05	25	$5.28 \pm 0.39 \times 10^{-15}$	$3.31 \pm 0.07 \times 10^{-14}$	N	Y	
R-9		4.64481	6427.9	34.43	21	$7.91 \pm 2.35 \times 10^{-15}$	$2.70 \pm 0.80 \times 10^{-14}$	N	N	
R-6		4.66750	6281.3	33.22	15	$4.41 \pm 0.37 \times 10^{-15}$	$2.30 \pm 0.06 \times 10^{-14}$	N	Y	
R-5		4.67528	6243.3	32.69	13	$5.93 \pm 1.45 \times 10^{-15}$	$1.63 \pm 0.25 \times 10^{-14}$	Y	N	
R-4		4.68315	6210.7	32.02	11	$2.60 \pm 0.37 \times 10^{-15}$	$2.07 \pm 0.07 \times 10^{-14}$	N	Y	
R-1		4.70742	6145.5	27.73	5	$2.25 \pm 0.66 \times 10^{-15}$	$1.54 \pm 0.12 \times 10^{-14}$	N	Y	
P-1		4.73265	6129.2	68.19	1	$1.40 \pm 0.96 \times 10^{-15}$	$9.67 \pm 1.64 \times 10^{-15}$	N	N	
P-4		4.75886	6161.8	38.31	7	$3.62 \pm 0.60 \times 10^{-15}$	$1.75 \pm 0.21 \times 10^{-14}$	N	Y	

Table 2.D.1: Continuation of Table 2.D.1

Molecule	Rot. Trans.	Wavelength	E_{up}	A_{ul}	g_{up}	Int. Flux ^(a)		Line prof. ^(b)	Blend ^(c)
						Narrow comp.	Broad comp.		
		[μm]	[K]	[s^{-1}]		[erg s^{-1}]	[cm^{-2}]		
	P-5	4.76782	6183.6	37.04	9	$3.96 \pm 1.66 \times 10^{-15}$	$2.02 \pm 0.33 \times 10^{-14}$	N	N
	P-6	4.77689	6210.7	36.15	11	$4.10 \pm 1.59 \times 10^{-15}$	$2.31 \pm 0.32 \times 10^{-14}$	N	N
	P-7	4.78608	6243.3	35.48	13	$3.96 \pm 1.31 \times 10^{-15}$	$2.64 \pm 0.22 \times 10^{-14}$	N	N
	P-8	4.79537	6281.3	34.94	15	$4.24 \pm 1.52 \times 10^{-15}$	$2.61 \pm 0.27 \times 10^{-14}$	N	N
	P-9	4.80479	6324.7	34.48	17	$4.80 \pm 0.90 \times 10^{-15}$	$2.51 \pm 0.20 \times 10^{-14}$	N	Y
	P-15	4.86370	6699.2	32.48	29	$5.79 \pm 1.32 \times 10^{-15}$	$2.95 \pm 0.23 \times 10^{-14}$	Y	N
	P-16	4.87394	6780.5	32.21	31	$3.86 \pm 1.19 \times 10^{-15}$	$3.17 \pm 0.22 \times 10^{-14}$	Y	N
	P-17	4.88429	6867.3	31.95	33	$4.44 \pm 1.44 \times 10^{-15}$	$2.99 \pm 0.25 \times 10^{-14}$	Y	N
	P-18	4.89477	6959.4	31.70	35	$4.92 \pm 0.68 \times 10^{-15}$	$3.07 \pm 0.15 \times 10^{-14}$	N	Y
	P-20	4.91609	7159.9	31.21	39	$3.04 \pm 0.42 \times 10^{-15}$	$3.23 \pm 0.07 \times 10^{-14}$	N	Y
	P-21	4.92694	7268.3	30.97	41	$3.62 \pm 1.29 \times 10^{-15}$	$2.92 \pm 0.23 \times 10^{-14}$	N	N
	P-22	4.93792	7382.0	30.73	43	$4.68 \pm 0.65 \times 10^{-15}$	$2.82 \pm 0.13 \times 10^{-14}$	N	Y
	P-24	4.96025	7625.6	30.27	47	$3.55 \pm 1.90 \times 10^{-15}$	$2.78 \pm 0.33 \times 10^{-14}$	N	N
	P-25	4.97161	7755.5	30.05	49	$3.70 \pm 1.36 \times 10^{-15}$	$2.65 \pm 0.22 \times 10^{-14}$	Y	N
	P-26	4.98310	7890.7	29.82	51	$2.44 \pm 1.61 \times 10^{-15}$	$3.04 \pm 0.27 \times 10^{-14}$	Y	N
	P-28	5.00647	8177.3	29.38	55	$2.85 \pm 1.51 \times 10^{-15}$	$2.72 \pm 0.25 \times 10^{-14}$	N	N
	P-32	5.05482	8814.6	28.52	63	$1.85 \pm 1.47 \times 10^{-15}$	$2.57 \pm 0.24 \times 10^{-14}$	N	N
	P-33	5.06725	8987.2	28.31	65	$1.62 \pm 0.43 \times 10^{-15}$	$2.29 \pm 0.07 \times 10^{-14}$	N	Y
	P-37	5.11838	9731.0	27.47	73	$1.43 \pm 0.62 \times 10^{-15}$	$2.05 \pm 0.12 \times 10^{-14}$	N	Y
	P-38	5.13151	9930.1	27.26	75	$1.27 \pm 0.78 \times 10^{-15}$	$1.89 \pm 0.14 \times 10^{-14}$	N	Y
¹² CO v=3-2	R-30	4.56764	11797.2	56.33	63	$1.55 \pm 0.38 \times 10^{-15}$	$1.00 \pm 0.14 \times 10^{-14}$	N	N
	R-27	4.58436	11315.7	55.55	57	$1.96 \pm 0.50 \times 10^{-15}$	$1.08 \pm 0.16 \times 10^{-14}$	N	N
	R-23	4.60800	10748.0	54.46	49	$1.68 \pm 0.38 \times 10^{-15}$	$1.10 \pm 0.13 \times 10^{-14}$	N	N
	R-22	4.61415	10619.3	54.17	47	$1.65 \pm 0.27 \times 10^{-15}$	$1.29 \pm 0.10 \times 10^{-14}$	N	N
	R-21	4.62041	10496.0	53.88	45	$1.82 \pm 0.38 \times 10^{-15}$	$1.31 \pm 0.12 \times 10^{-14}$	N	N
	R-20	4.62676	10378.0	53.59	43	$2.65 \pm 1.83 \times 10^{-15}$	$9.14 \pm 2.35 \times 10^{-15}$	Y	N
	R-18	4.63976	10157.9	52.97	39	$1.63 \pm 0.45 \times 10^{-15}$	$9.88 \pm 1.94 \times 10^{-15}$	Y	N
	R-17	4.64641	10055.9	52.66	37	$1.49 \pm 0.33 \times 10^{-15}$	$9.49 \pm 1.20 \times 10^{-15}$	N	N
	R-12	4.68118	9626.2	50.89	27	$2.11 \pm 0.42 \times 10^{-15}$	$1.43 \pm 0.19 \times 10^{-14}$	N	N
	R-11	4.68844	9556.3	50.49	25	$1.38 \pm 0.27 \times 10^{-15}$	$9.24 \pm 1.15 \times 10^{-15}$	Y	N
	R-10	4.69581	9491.8	50.06	23	$1.54 \pm 0.45 \times 10^{-15}$	$8.49 \pm 1.71 \times 10^{-15}$	N	N
	R-9	4.70328	9432.7	49.59	21	$1.70 \pm 1.07 \times 10^{-15}$	$8.16 \pm 2.01 \times 10^{-15}$	N	N
	R-8	4.71085	9378.9	49.08	19	$1.88 \pm 0.79 \times 10^{-15}$	$7.95 \pm 2.35 \times 10^{-15}$	N	N
	R-5	4.73421	9249.8	47.09	13	$1.22 \pm 0.29 \times 10^{-15}$	$8.07 \pm 1.09 \times 10^{-15}$	N	N
	P-6	4.83745	9217.5	52.11	11	$1.54 \pm 0.42 \times 10^{-15}$	$8.30 \pm 1.62 \times 10^{-15}$	N	N
	P-16	4.93614	9782.0	46.44	31	$1.76 \pm 0.43 \times 10^{-15}$	$1.13 \pm 0.15 \times 10^{-14}$	N	N
	P-19	4.96812	10055.9	45.34	37	$1.63 \pm 0.39 \times 10^{-15}$	$1.10 \pm 0.13 \times 10^{-14}$	N	N
¹³ CO v=1-0	R-30	4.55970	5607.8	18.60	126	-	$5.10 \pm 0.40 \times 10^{-15}$	N	Y
	R-26	4.58188	4992.5	18.25	110	-	$4.65 \pm 0.30 \times 10^{-15}$	N	Y
	R-23	4.59947	4585.4	17.97	98	-	$8.28 \pm 0.93 \times 10^{-15}$	N	N
	R-22	4.60551	4460.0	17.88	94	-	$6.71 \pm 0.78 \times 10^{-15}$	N	N
	R-21	4.61165	4339.9	17.78	90	-	$6.39 \pm 0.81 \times 10^{-15}$	Y	N
	R-18	4.63062	4010.5	17.48	78	-	$7.30 \pm 0.31 \times 10^{-15}$	N	Y
	R-16	4.64373	3817.0	17.26	70	-	$8.36 \pm 0.80 \times 10^{-15}$	Y	N
	R-15	4.65043	3728.0	17.15	66	-	$7.45 \pm 0.72 \times 10^{-15}$	Y	N
	R-13	4.66411	3565.8	16.91	58	-	$8.69 \pm 0.73 \times 10^{-15}$	N	N
	R-10	4.68535	3361.6	16.51	46	-	$1.01 \pm 0.08 \times 10^{-14}$	N	N
	R-9	4.69262	3304.0	16.36	42	-	$8.79 \pm 0.74 \times 10^{-15}$	Y	N
	R-7	4.70747	3204.4	16.01	34	-	$6.05 \pm 0.95 \times 10^{-15}$	N	Y
	R-6	4.71504	3162.5	15.79	30	-	$7.69 \pm 1.33 \times 10^{-15}$	N	N
	R-4	4.73047	3094.4	15.22	22	-	$6.12 \pm 0.77 \times 10^{-15}$	N	N
	R-3	4.73834	3068.2	14.81	18	-	$6.06 \pm 0.92 \times 10^{-15}$	N	N
	R-2	4.74631	3047.2	14.20	14	-	$4.87 \pm 1.18 \times 10^{-15}$	N	N
	P-2	4.78771	3021.0	21.50	6	-	$5.84 \pm 1.17 \times 10^{-15}$	N	N
	P-3	4.79630	3031.5	19.25	10	-	$7.03 \pm 0.99 \times 10^{-15}$	N	N
	P-4	4.80499	3047.2	18.23	14	-	$4.86 \pm 1.01 \times 10^{-15}$	N	Y
	P-6	4.82270	3094.4	17.20	22	-	$1.01 \pm 0.05 \times 10^{-14}$	N	Y
	P-7	4.83172	3125.8	16.89	26	-	$9.66 \pm 1.11 \times 10^{-15}$	Y	N
	P-10	4.85942	3251.6	16.22	38	-	$8.91 \pm 1.05 \times 10^{-15}$	N	N
	P-12	4.87844	3361.6	15.89	46	-	$7.67 \pm 1.00 \times 10^{-15}$	Y	N
	P-13	4.88812	3424.4	15.75	50	-	$8.40 \pm 1.15 \times 10^{-15}$	N	N
	P-15	4.90781	3565.8	15.47	58	-	$7.79 \pm 2.00 \times 10^{-15}$	N	N
	P-16	4.91783	3644.3	15.35	62	-	$7.16 \pm 0.82 \times 10^{-15}$	N	N
	P-17	4.92796	3728.0	15.23	66	-	$9.16 \pm 0.26 \times 10^{-15}$	N	Y
	P-18	4.93821	3817.0	15.11	70	-	$7.35 \pm 0.56 \times 10^{-15}$	N	Y
	P-25	5.01328	4585.4	14.34	98	-	$5.03 \pm 0.39 \times 10^{-15}$	N	Y
	P-27	5.03582	4851.7	14.13	106	-	$4.32 \pm 0.58 \times 10^{-15}$	N	Y
	P-35	5.13110	6123.2	13.33	138	-	$1.98 \pm 0.59 \times 10^{-15}$	N	Y

Table 2.D.1: Continuation of Table 2.D.1

Molecule	Rot. Trans.	Wavelength	E_{up}	A_{ul}	g_{up}	Int. Flux ^(α)		Line prof. ^(β)	Blend ^(γ)
						Narrow comp.	Broad comp.		
		[μm]	[K]	[s^{-1}]		[$\text{erg s}^{-1} \text{cm}^{-2}$]			
$\text{C}^{18}\text{O } v=1-0$	R-12	4.68007	3485.0	16.66	27	-	$1.51 \pm 0.18 \times 10^{-15}$	Y	N
	R-10	4.69434	3354.6	16.39	23	-	$1.87 \pm 0.16 \times 10^{-15}$	N	N
	R-7	4.71646	3198.0	15.88	17	-	$1.68 \pm 0.32 \times 10^{-15}$	Y	N
	R-5	4.73170	3119.7	15.42	13	-	$7.80 \pm 1.98 \times 10^{-16}$	Y	N
	R-4	4.73947	3088.4	15.11	11	-	$1.26 \pm 0.24 \times 10^{-15}$	N	N
	P-8	4.84983	3156.3	16.51	15	-	$1.64 \pm 0.09 \times 10^{-15}$	N	Y
	P-9	4.85907	3198.0	16.29	17	-	$1.32 \pm 0.18 \times 10^{-15}$	N	N
	P-11	4.87786	3297.2	15.93	21	-	$1.09 \pm 0.14 \times 10^{-15}$	Y	N
	P-15	4.91678	3558.0	15.36	29	-	$1.77 \pm 0.06 \times 10^{-15}$	N	Y
	P-17	4.93692	3719.7	15.11	33	-	$1.52 \pm 0.13 \times 10^{-15}$	N	N
	P-18	4.94717	3808.3	15.00	35	-	$1.44 \pm 0.07 \times 10^{-15}$	N	Y

Notes. (α): for the ^{13}CO and $\text{C}^{18}\text{O } v=1-0$ transitions, we list the integrated flux of the single component under the column of the broad component, assuming that the observed emission originates from the Keplerian disk.

(β): this entry lists all the transitions that have been used in acquiring the median, normalised line profile (Y) and those that have only been used for the rotational diagram (N).

(γ): this entry lists all the transitions that are blended with other transitions.

2.D.2 Full iSHELL model

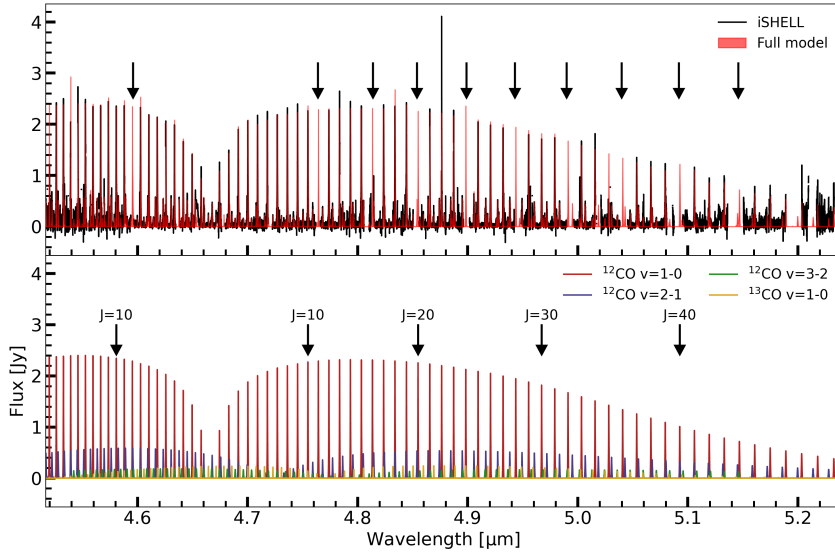


Figure 2.D.1: Continuum-subtracted iSHELL spectrum of DR Tau with a model based on the best-fitting parameters obtained through the rotational diagram analysis. The gaps visible (highlighted by the black arrows in the top panel) in the iSHELL spectrum correspond to removed telluric features. The top panel shows the full model, whereas the bottom panel shows the contribution of each band separately. For ^{12}CO , the narrow and broad component are shown together. In addition, in the bottom panel we highlight the ^{12}CO transitions which have an upper level J -value of 10, 20, 30, or 40.

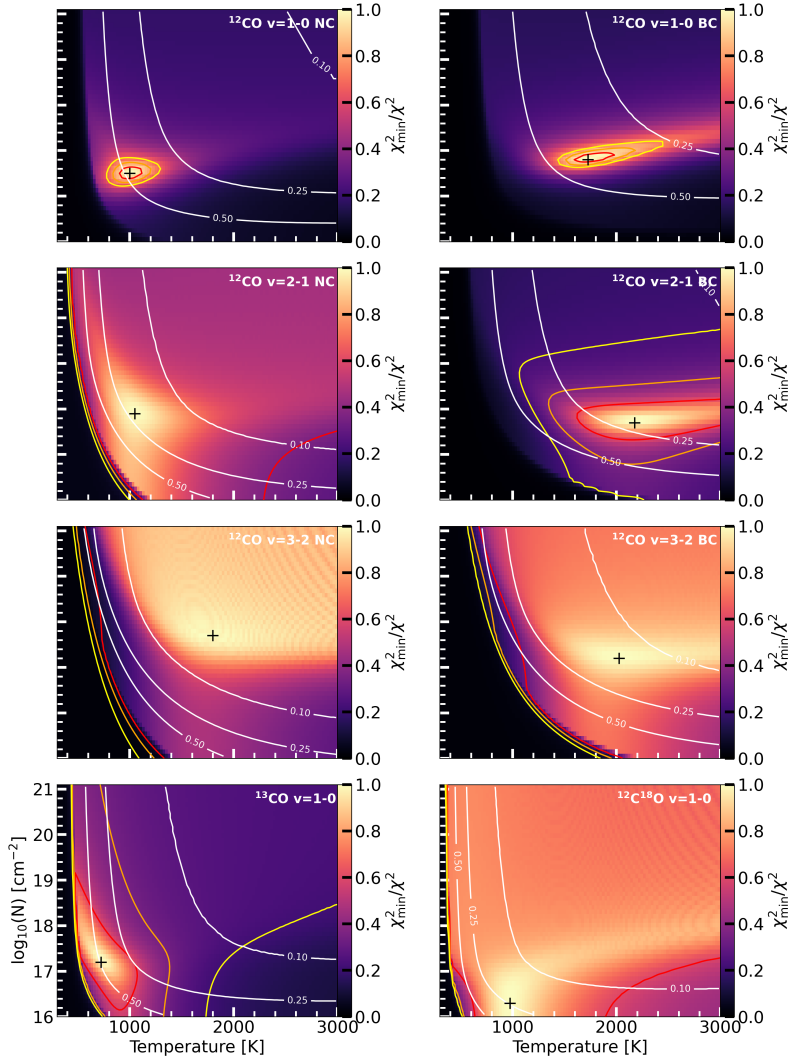
2.D.3 χ^2 -maps of the CO rotational diagrams

Figure 2.D.2: Similar as Figure 2.C.1, but for the iSHELL CO rotational diagrams. The top row shows those for the narrow (left) and broad (right) component of ^{12}CO $v=1-0$ transitions. Those for the ^{12}CO $v=2-1$ and $v=3-2$ transitions are shown on the second and third row, respectively, whereas the ones for the ^{13}CO and C^{18}O (using VLT-CRIRES data) are shown on the bottom row.

2.D.4 Optical depth of ^{12}CO

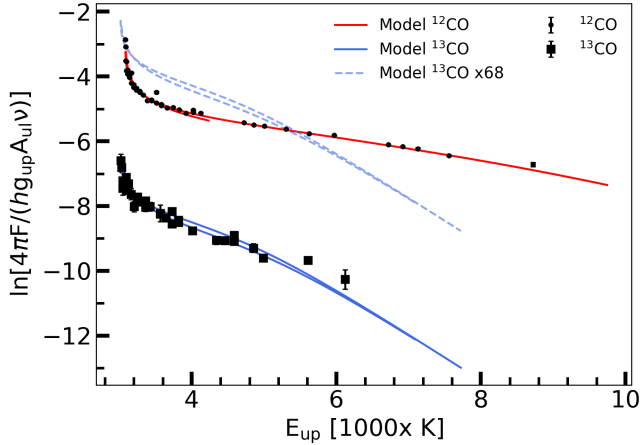


Figure 2.D.3: Rotational diagrams for ^{12}CO $v=1-0$ (dots) and ^{13}CO $v=1-0$ (squares). The dashed blue line indicates the model of ^{13}CO ($T=750$ K) multiplied by a factor of 68 to account for the isotopologue ratio. The fluxes shown for the ^{12}CO are a summation of the narrow ($T=1000$ K) and broad ($T=1725$ K) components.

2.D.5 LTE versus non-LTE

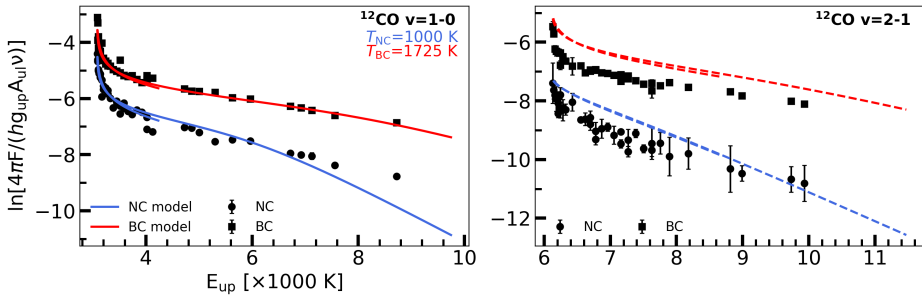


Figure 2.D.4: Comparison between the rotational diagrams of the ^{12}CO $v=1-0$ and $v=2-1$ transitions to test the assumption of LTE. The left panel shows the ^{12}CO $v=1-0$ rotational diagrams (see also Figure 2.8). The right panel shows the non-LTE test, where the ^{12}CO $v=2-1$ integrated fluxes are shown together with expected models based on the results of the ^{12}CO $v=1-0$ rotational diagrams. As the models overproduce the observed ^{12}CO $v=2-1$ fluxes, invalidating the assumption that the levels can be characterised by a single temperature.

2.D.6 Convolution iSHELL to JWST-MIRI resolution

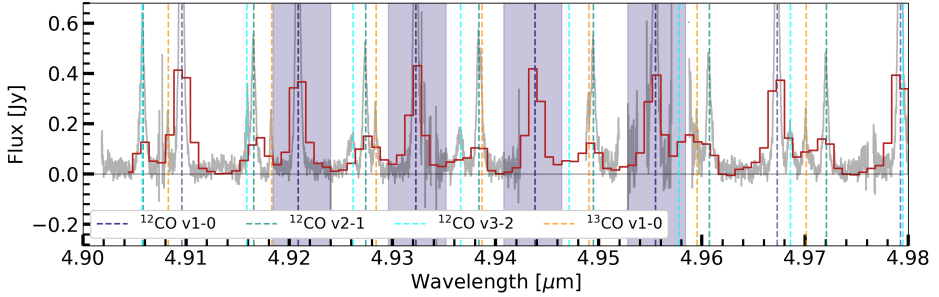


Figure 2.D.5: Xoom-in of Figure 2.3 on the JWST-MIRI data (red) within the wavelength region 4.90-4.98 μm . The iSHELL observations are shown here in grey. The different transitions in this wavelength region of the ^{12}CO $v=1-0$ (dark blue), $v=2-1$ (teal), $v=3-2$ (cyan), and the ^{13}CO $v=1-0$ (orange) transitions are shown to identify the different lines and highlight corresponding line overlaps. The dark blue shaded areas indicate the (relatively) isolated ^{12}CO $v=1-0$ transitions that have been used to determine the pseudo-Voigt line profile of the JWST-MIRI data.

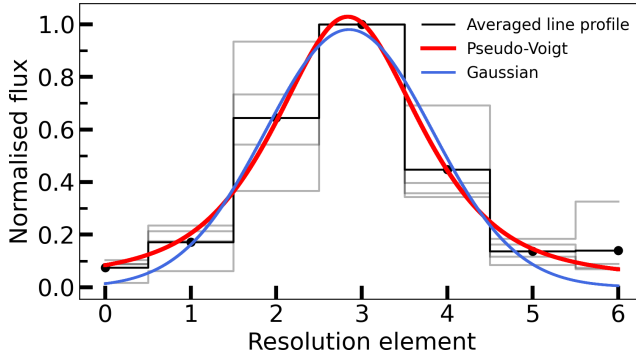


Figure 2.D.6: Averaged, normalised line profile of the four selected, unblended ^{12}CO $v=1-0$ transitions observed with JWST-MIRI (see also Figure 2.D.5). The faint grey lines indicate the individual, normalised lines, whereas the red and blue lines display, respectively, the fitted pseudo-Voigt and Gaussian profiles.

2.D.6.1 Gaussian line profile

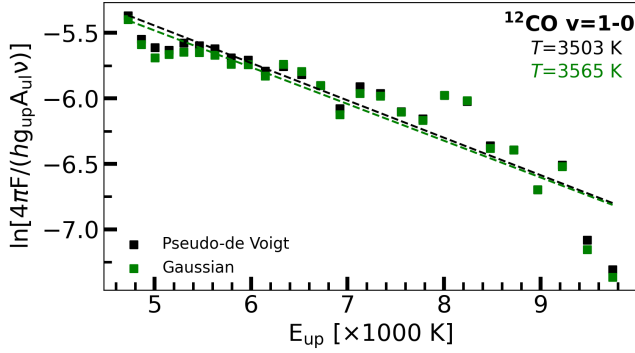


Figure 2.D.7: Simple rotational diagrams of the JWST-MIRI integrated fluxes when considering a pseudo-Voigt (black) or a Gaussian (green) line profile. Straight line fits suggest excitation temperatures of $T=3503 \text{ K}$ when considering the pseudo-Voigt profile and $T=3565$ when using a Gaussian.

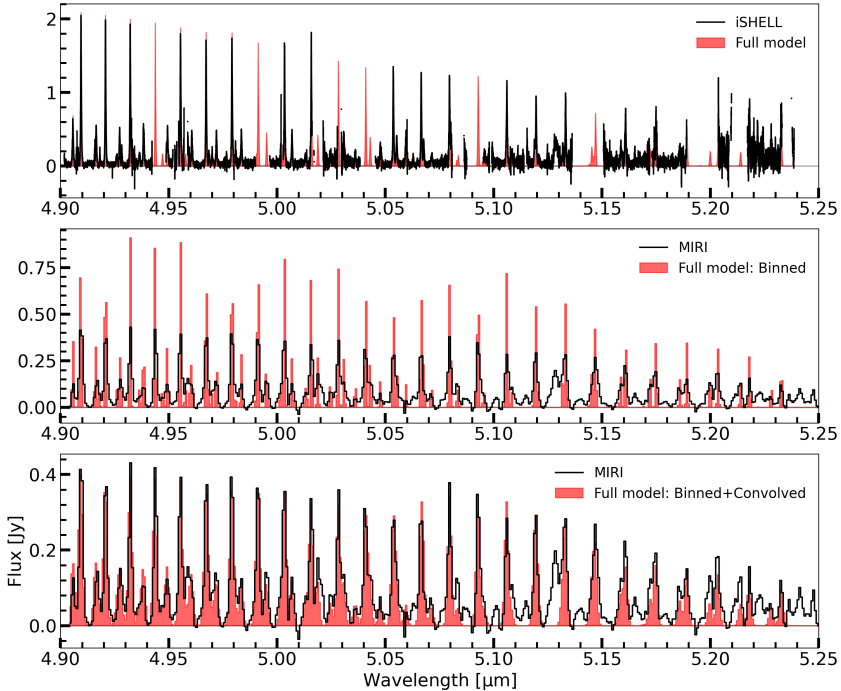


Figure 2.D.8: Same as Figure 2.11, but for the Gaussian line profile.