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From inference to influence: applying causal game theory to complex security environments

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From Inference to Influence: Applying Causal Game Theory to Complex Security Environments

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