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Capturing dynamics with noisy quantum computers

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Capturing dynamics with noisy quantum computers

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Meinen Eltern, für ihre Unterstützung und Erziehung

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