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Hybrid quantum-classical metaheuristics for automated machine learning applications

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Curriculum Vitae

David Von Dollen, born in 1978 in Berkeley, California, USA, received his Bachelor of Arts in Music from William Paterson University in 2007. He worked for four years as a mathematics teacher, completing his certificate in education from the state of New Jersey, USA, before transitioning into a career in data science, working in the finance and insurance industries. In 2014, he completed his professional certification in data science from the University of Washington. In 2018, he earned his Master of Science in Computer Science from The Georgia Institute of Technology while working as a data scientist for Audi of America and the Volkswagen Group. While at the Volkswagen Group, David co-authored three patents and seven publications and worked on projects related to artificial intelligence, quantum computing, intelligent transportation, mobility, and information technology. He started his Ph.D. at Leiden University in 2019. During his Ph.D. studies, he supervised two Master's students and coordinated the Quantum Computing for Industrial Applications Group. In 2023, he traveled to Leiden, where he gave a guest lecture on quantum machine learning, and attended classes on practicing ethical science. Since 2022, David has held technology leadership and advisory positions at several startups operating in the intelligent transportation, IoT, computer vision, and mobile application spaces. He currently resides in the Portland, Oregon, USA, metro area, where he enjoys spending time with his family and friends outside of his scientific and professional work.

Acronyms

AGI

Artificial General Intelligence

AI

Artificial Intelligence

AutoML

Automated Machine Learning

BPP

Bounded Error Probabilistic Polynomial Time

BQP

Bounded Error Quantum Polynomial Time

EDQA

Evolutionary Designed Quantum Algorithms

ELBO

Evidence Lower Bound

ES

Evolution Strategies

FS

Feature Selection

GBR

Gradient Boosted Regression tree

GMIC

Generalized Mean Information Coefficient

7.1. ACRONYMS

GPR

Gaussian Process Regression

HHL

Harrow, Hassidim, Lloyd algorithm

HPO

Hyper-Parameter Optimization

LHS

Leap Hybrid Sampler

LR

Linear Regression

MDP

Markov Decision Process

MI

Mutual Information

MIC

Maximal Information Coefficient

ML

Machine Learning

MRMR

Maximum Relevancy Minimum Redundancy

NAS

Neural Architecture Search

NFL

No Free Lunch

NISQ

Noisy Intermediate Scale Quantum

NP

Nondeterministic Polynomial Time

P

Polynomial Time

PCC

Pearson Correlation Coefficient

PQK

Projected Quantum Kernel

PSD

Positive Semi-Definite

QA

Quantum Assisted

QE

Quantum Enhanced

QEA

Quantum Evolutionary Algorithms

QIEA

Quantum-Inspired Evolutionary Algorithms

QMA

Quantum Merlin-Arthur

QML

Quantum Machine Learning

QPU

Quantum Processing Unit

QUBO

Quadratic Unconstrained Binary Optimization

RFE

Recursive Feature Elimination

RFF

Random Fourier Features

RL

Reinforcement Learning

SA

Simulated Annealing

7.1. ACRONYMS

SD

Steepest Descent

TT

Tensor train

VQC

Variational Quantum Circuit

Symbols

\mathcal{A} learning algorithm (AutoML process in preliminaries chapter)

\mathbf{a} chromosome/individual

a activation function

$\hat{\alpha}$ acquisition function parameter

α fitness weight in QUBO

$\boldsymbol{\alpha}$ GP weight vector

\mathbf{a}^+ current best point

argmax argmax operator

argmin argmin operator

\mathbf{a}^* best solution found

A_t time coefficient for driver Hamiltonian

b_d phase shift (indexed)

β diversity weight in QUBO

\mathcal{O} big-O notation

$\{0, 1\}$ binary set

$B(n)$ maximum grid size parameter

b phase shift

$\langle \cdot |$ bra

$\langle \cdot | \cdot \rangle$ quantum bra-ket notation

B_t time coefficient for target Hamiltonian

\mathbf{b} bias vector

7.1. SYMBOLS

CE	cross-entropy loss
Cholesky	Cholesky decomposition
C	characteristic matrix
cov	covariance function
C^*	maximal characteristic matrix
d	dimension of feature vectors
\mathcal{D}_c	classical dataset
distance (\cdot, \cdot)	distance metric
\mathcal{D}'	processed dataset
\mathcal{D}_q	quantum dataset
D	number of random Fourier features
\mathcal{D}	dataset
E	energy function
EI	expected improvement
ELBO	ELBO function
ℓ	feature index (second)
E_1	first excited state energy
ϵ	error term
\mathbb{E}	expectation
E_0	ground state energy
$f(\cdot)$	function
f_Q	QUBO objective function
\mathbf{f}_*	function at test points
$f(\mathbf{x}^+)$	current best observation
γ	RBF kernel length scale parameter
$\gamma_{\mathbf{RL}}$	RL discount factor
G	generations to convergence

GD	genotype diversity
g	generation index
GMIC	generalized mean information coefficient
g_{\min}	minimum energy gap
\mathcal{H}	Hilbert space
Hamming(\cdot, \cdot)	Hamming distance
H_f	target/final Hamiltonian
h	learning hypothesis
H_I	driver/initial Hamiltonian
hit_score	hit score
h	neural network layer
h^*	optimal hypothesis
H_t	time-dependent Hamiltonian
i	iteration index
I	identity matrix
\mathbb{I}	indicator function
$\langle \cdot \cdot \rangle$	inner product
I^*	maximum mutual information
j	feature index
κ	UCB exploration parameter
κ_{nn}	number of nearest neighbors (MI estimation)
kernel (\cdot, \cdot)	kernel function
$ \cdot\rangle$	ket
k	number of features in reduced space
KL	KL divergence
\mathbf{K}_m	reduced kernel matrix
K	kernel/Gram matrix

7.1. SYMBOLS

$\tilde{\mathbf{K}}$	reduced quantum kernel matrix
\mathbf{K}_{X^*X}	kernel matrix (test-train)
$\mathbf{K}_{X^*X^*}$	kernel matrix (test-test)
\mathbf{K}_{XX}	kernel matrix (train-train)
\mathbf{K}_{XX}^{-1}	kernel matrix inverse
λ	number of offspring
λ_s	penalty weight for QUBO size constraint
\mathbf{L}	Cholesky lower triangular matrix
length_score	length score
m	number of inducing points
MAE	mean absolute error
MIC	maximum information coefficient
MI	mutual information
MSE	mean squared error
μ	number of selected parents
$\hat{\mu}$	predicted mean
$\tilde{\mu}$	mean function
n	number of samples/population size
\mathcal{N}	Gaussian/normal distribution
$\ \cdot\ $	Euclidean norm
n_q	number of qubits
N	number of samples for MSE
$\hat{\mathbf{o}}$	optimal binary solution
o_i	binary decision variable
ω_d	frequency vector (indexed)
ω	frequency vector
$\tilde{\mathbf{o}}$	binary solution for inducing points

\mathbf{o}	binary decision variable vector
PCC	Pearson correlation coefficient
$P_{\mathcal{D}}$	preprocessing function
Φ	standard normal CDF
$\phi(\cdot)$	quantum feature map
ϕ	standard normal PDF
P_{λ}	offspring population
P_{μ}	parent population
p_m	mutation probability
$P(\omega)$	spectral density
P	population
p	prior distribution
PQK	projected quantum kernel
ψ	digamma function
$\hat{\mathbf{Q}}$	QUBO matrix for features
q	qubit index
Q	QUBO matrix
$\tilde{\mathbf{Q}}$	QUBO matrix for inducing points
ρ_q	quantum state for qubit q
ρ	density operator
\mathbb{R}	real numbers
SA	subset accuracy
σ	mutation strength
$\hat{\sigma}$	predicted standard deviation
σ_n^2	noise variance
s	performance score
\otimes	tensor product

7.1. SYMBOLS

T evolution timescale

θ hyperparameters (rotation parameters when applied to quantum circuits)

θ^* optimal hyperparameters

θ_{var} variational parameters (VGPR)

t maximum generations

UCB upper confidence bound

\mathbf{u} inducing point values

U unitary operator

U_{Z_j} unitary rotation for qubit j

$U_{Z_j Z_\ell}$ controlled-Z unitary

val_acc validation accuracy

\mathbf{V} intermediate matrix for covariance

\mathbf{W} weight matrix

\mathbf{w} weights for linear regression

x_j individual feature component

\mathbf{X}_m inducing point subset

\mathbf{X} set of input data

\mathbf{x}^+ current best point

\mathbf{X}^* test data matrix

\mathbf{x}^* test feature vector

$\tilde{\mathbf{X}}$ reduced training data

\mathbf{x} feature vector

$\hat{\mathbf{y}}$ predicted observation vector

y label/observation

y^+ current observation

\mathbf{y} observation vector

z_d RFF basis function

\mathbf{z} inducing points

Z_j Pauli-Z operator for qubit j

Z_{norm} normalization constant (GMIC)

Z Pauli-Z operator

7.1. SYMBOLS
