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Hybrid quantum-classical metaheuristics for automated machine learning applications

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David Von Dollen

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