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Automata learning: from probabilistic to quantum

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Automata Learning: from Probabilistic to Quantum

Wenjing Chu

Automata Learning: from Probabilistic to Quantum

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