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The wild Brauer-Manin obstruction on $K3$ surfaces

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THE WILD BRAUER–MANIN OBSTRUCTION ON $K3$ SURFACES

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