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## The wild Brauer-Manin obstruction on K3 surfaces

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# THE WILD BRAUER–MANIN OBSTRUCTION ON $K3$ SURFACES

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# Contents

<b>Introduction</b>	<b>1</b>
<b>1 The Brauer–Manin obstruction and the refined Swan conductor</b>	<b>7</b>
1.1 The Brauer–Manin obstruction . . . . .	9
1.2 The refined Swan conductor . . . . .	17
1.3 Refined Swan conductor and Brauer–Manin obstruction . . . . .	31
<b>2 An example of Brauer–Manin obstruction coming from a prime of good reduction</b>	<b>37</b>
2.1 Swinnerton-Dyer’s question . . . . .	37
2.2 Proof of Theorem 2.1.10 . . . . .	43
2.3 A family of K3 surfaces with the same property . . . . .	48
<b>3 The role of primes of good reduction in the Brauer–Manin obstruction</b>	<b>53</b>
3.1 Ordinary good reduction . . . . .	54
3.2 Non-ordinary good reduction . . . . .	58
<b>4 Computations with the refined Swan conductor</b>	<b>69</b>
4.1 Refined Swan conductor and extension of the base field . . . . .	70
4.2 Computation on $p$ -torsion elements . . . . .	73
4.3 The case of K3 surfaces . . . . .	79
4.4 Example of Chapter 2 revisited . . . . .	82
4.5 Kummer K3 surfaces over 2-adic fields . . . . .	82
4.6 Family of examples . . . . .	92
<b>Bibliography</b>	<b>97</b>
<b>Summary</b>	<b>103</b>
<b>Samenvatting</b>	<b>107</b>

<b>Acknowledgments</b>	<b>111</b>
<b>Curriculum Vitae</b>	<b>113</b>