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Influence of aortic aneurysm on the local distribution of NO and O$_2$ using image-based computational fluid dynamics

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A R T I C L E   I N F O

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A B S T R A C T

There is a pressing need to establish novel biomarkers to predict the progression of thoracic aortic aneurysm (TAA) dilatation. Aside from hemodynamics, the roles of oxygen (O$_2$) and nitric oxide (NO) in TAA pathogenesis are potentially significant. As such, it is imperative to comprehend the relationship between aneurysm presence and species distribution in both the lumen and aortic wall. Given the limitations of existing imaging methods, we propose the use of patient-specific computational fluid dynamics (CFD) to explore this relationship. We have performed CFD simulations of O$_2$ and NO mass transfer in the lumen and aortic wall for two cases: a healthy control (HC) and a patient with TAA, both acquired using 4D-flow magnetic resonance imaging (MRI). The mass transfer of O$_2$ was based on active transport by hemoglobin, while the local variations of the wall shear stress (WSS) drove NO production. Comparing hemodynamic properties, the time-averaged WSS was considerably lower for TAA, while the oscillatory shear index and endothelial cell activation potential were notably elevated. O$_2$ and NO showed a non-uniform distribution within the lumen and an inverse correlation between the two species. We identified several locations of hypoxic regions for both cases due to lumen-side mass transfer limitations. In the wall, NO varied spatially, with a clear distinction between TAA and HC. In conclusion, the hemodynamics and mass transfer of NO in the aorta exhibit the potential to serve as a diagnostic biomarker for TAA. Furthermore, hypoxia may provide additional insights into the onset of other aortic pathologies.

1. Introduction

Thoracic aortic aneurysm (TAA) is a progressive pathology of the aorta characterized by vessel dilatation, dysfunction of vascular smooth muscle cells, and remodeling of the extracellular matrix, as described by the European Society of Cardiology [1]. Given that this disease is primarily asymptomatic, the rupture of TAA is associated with high mortality rates [2]. Therefore, it is crucial to define new biomarkers to identify the genesis, growth, and rupture of TAA. Recent studies have suggested that the distribution of Oxygen (O$_2$) and Nitric Oxide (NO) in the aorta could be potential new biomarkers for TAA. TAA tissue exhibits O$_2$ deficiency (hypoxia) [3]. Moreover, an insufficient supply of O$_2$ to the aortic wall was linked to the genesis of abdominal aortic aneurysm (AAA) [4,5], likely due to the scarcity of vasa vasorum in this section of the aorta [6]. NO is a regulator in vascular homeostasis and was proposed as a potential key indicator for the development of TAA in patients with Marfan syndrome [7,8]. Elevated NO pathways were observed in individuals with this genetic condition [7], and NO was found to be a significant contributor to the development of TAA in animal models and patients [8]. Therefore, analyzing the behavior of these two molecules in patients with TAA could lead to the identification of direct biochemical markers that estimate the risk of disease progression and rupture.

However, the potential measurement methods for non-invasive assessment of O$_2$ and NO concentration in the lumen and aortic wall currently do not have a sufficient spatial resolution, as reported in recent studies [9–12]. As a viable alternative, we have previously demonstrated the usefulness of image-based computational fluid dynamics (CFD) in providing insights into blood flow dynamics in the aorta [13,14]. Here, we have to emphasize the subject- and patient-specific nature of simulations, where the geometry and boundary conditions should be based on actual measurements, such as 4D-flow magnetic resonance imaging (4D-flow MRI). By utilizing a patient-specific model...
based on 4D-flow MRI, we can expand the CFD model to account for the mass transfer of these species. However, it is imperative to consider the complex interplay between O$_2$, NO, and various actors in the vascular system to ensure a physiologically accurate representation of the model.

O$_2$ is transferred within the cardiovascular system by two distinct mechanisms: diffusion as free species in plasma and binding to hemoglobin, a protein in the erythrocytes. The latter process is the primary mode and contributes to over 98% of total O$_2$ transport. However, at low shear rates, O$_2$ is released from the hemoglobin, and free diffusion becomes dominant. This process is particularly pronounced in the capillaries and the proximity of the arterial walls in (the low-shear region) of the great vessels. Therefore, modeling both mechanisms simultaneously is essential [18]. Within the arterial wall, O$_2$ is supplied by both the lumen and the vasa vasorum and consumed by the tissue. For modeling NO, the focus must be on three primary mechanisms: production, transport, and consumption. First, NO production occurs mainly in the endothelial layer of the arterial wall and is moderated by local wall shear stress (WSS) [16,17] due to the activation of endothelial cells. The second mechanism involves NO transport from the endothelial layer to the smooth muscle cells and into the arterial wall, mainly driven by diffusion. In the opposite direction, NO is transported within the lumen by combined diffusion and convection. Finally, the primary NO sink is its reaction with hemoglobin to form a complex and oxidation to nitrate in the lumen. The reaction with cytoglobin is the major contributor to NO consumption in the arterial wall [16,17].

Numerous investigations have been conducted on modeling the transport processes of O$_2$ [15,18] and NO [19–23] in idealized or large arteries, such as the aorta. However, the combined effects of hemodynamics and both species were not examined in the aorta. As reported by Allen et al. hypoxia can stimulate the release of NO from red blood cells [24] and, by that, affect vasodilatation. Thus, understanding the relationship between the distribution of O$_2$ and NO can yield valuable insights into the hemodynamic regulation of arterial behavior. Finally, although most studies demonstrated the limitations of O$_2$ and NO transport in the lumen, the effect on the aortic wall and its remodeling are usually omitted due to the increased complexity of the computational model.

In this study, we put forth the hypothesis that the distribution of O$_2$ and NO in the aorta is significantly influenced by hemodynamics and the presence of an aneurysm and may serve as an indicator for aneurysm pathogenesis. To investigate this hypothesis, we simulated the interplay between blood flow and mass transfer in the aorta and its wall for two molecules: O$_2$ and NO. To model the aortic wall, we employed a single-layer approximation with averaged properties to incorporate the effect of intima, media, and adventitia. We developed a model for mass transfer of O$_2$ within the aortic and aortic wall and its consumption by the wall. In addition, we introduce a model for NO production, which is driven by local hemodynamics and biochemical reactions in the blood and aortic tissue. By using this computational framework, we were able to simulate and comprehend the processes that occur within the aorta and aortic wall in greater detail. We conducted simulations of blood flow with the mass transfer of two studied species in two case-specific geometries: a healthy control (HC) and a patient (P) with a root aneurysm. Finally, based on the analysis of hemodynamics and mass transfer properties of these two cases, we propose potential biomarkers that may indicate TAA pathogenesis.

2. Methods

2.1. Studied cases

The Medical Ethics Committee approved this study protocol of the Leiden University Medical Center (G20.149 for P and P18.034 for HC). Moreover, informed consent was signed by both of the subjects. We have studied two different subjects - a healthy control (HC, Fig. 1a) and a patient with a root aneurysm with $D_{max} = 5$ cm (P, Fig. 1b).

| Table 1 Parameters of 4D-flow MRI sequence for healthy control and patient; res. denotes resolution. |
|---------------------------------|--------|------------------|------------------|
| Velocity encoding              | [cm/s] | 150              | 160              |
| Reconstructed temporal res.    | [ms]   | 28               | 38               |
| Echo time                      | [ms]   | 2.6              | 2.7              |
| Repetition time                | [ms]   | 4.5              | 4.6              |
| Flip angle                     | [°]    | 10               | 10               |
| Acquired isotropic res.        | [mm]   | 2.5              | 2.7              |
| Field of view                  | [mm$^2$] | 430 × 70 × 280  | 350 × 80 × 220  |
| Turbo field echo factor        | [-]    | 2                | 2                |
| Parallel imaging factor        | [-]    | 2.5 × 1.2        | 2.5 × 1.2        |

Fig. 1. Pre-processed geometry of healthy control (a) and patient (b) with highlighted regions for analysis (ascending aorta—AscAo, aortic arch—Arch, descending aorta—DescAo, aortic root—AoR (for healthy control only), and thoracic aortic aneurysm—TAA (for the patient only)) and the 4D-flow MRI extracted mean velocity at the inlet with the interpolated velocity v(t) for healthy control (c) and patient (d).

2.2. MRI data

Both P (female, 67 years old, heart rate during acquisition: 48 bpm) and HC (male, 80 years old, heart rate during acquisition: 62 bpm) were examined using 4D-flow MRI on a 3T system (Elition, Philips Healthcare, Best, The Netherlands). The MRI acquisition protocol used a hemidiaphragm respiratory navigator with retrospective electrocardiogram gating. All of the additional details about the MRI sequence can be found in Table 1.

The subject-specific domain for the lumen-only simulations was obtained by segmenting the 4D-flow MRI data set using CAAS MR Solutions v5.2. (Pie Medical Imaging, Maastricht, The Netherlands). The segmentation protocol is identical for both studied subjects, and the details can be found in our previous study [14]. The segmented geometries, after additional pre-processing using the Vascular Modeling Toolkit (VMTK), can be found in Fig. 1 with highlighted locations of interest—ascending aorta (AscAo), aortic arch (Arch), descending aorta (DescAo), and for P only thoracic aortic aneurysm (TAA).

To create the domain for lumen-wall simulations, the surface of the segmented geometry was offset in the normal direction using Autodesk Meshmixer v3.5 (Autodesk, Inc., California, United States) by the uniform wall thickness $T_w = 2.20$ mm, based on values typically used in literature [25,26].
2.3. Computational model

2.3.1. Fluid dynamics

The conservation of mass and momentum for the blood flow in the aorta is:

\[
\frac{\partial p}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0
\]  
(1)

\[
\frac{\partial \rho \mathbf{v}}{\partial t} + \nabla \cdot (\rho \mathbf{v} \otimes \mathbf{v}) = -\nabla p + \nabla \cdot (\mu \nabla \mathbf{v})
\]  
(2)

where \( \mathbf{v} \) is the fluid velocity, \( \rho \) is the fluid density, \( \mu \) the fluid dynamic viscosity, and \( p \) is the pressure.

2.3.2. Mass transport of \( \text{O}_2 \)

Oxygen transport by plasma (‘passive’ oxygen transport) can be described by the dilute approximation. For this, the convection–diffusion equation for \( \text{O}_2 \) can be written as:

\[
\frac{\partial c_{\text{O}_2}}{\partial t} + \nabla \cdot (c_{\text{O}_2} \mathbf{v}) = – \nabla p_{\text{O}_2} + \nabla \cdot (D_{\text{O}_2} \nabla c_{\text{O}_2}) + \rho_{\text{O}_2}
\]

(3)

where \( c_{\text{O}_2} \) is the concentration of \( \text{O}_2 \), \( D_{\text{O}_2} \) is the \( \text{O}_2 \) diffusion coefficient in fluid, and \( \rho_{\text{O}_2} \) is the source/sink which is neglected for the case of passive oxygen transport. For the ‘active’ oxygen transport (transport of oxygen bound to hemoglobin) \( \rho_{\text{O}_2} \) reflects the complex reaction process of binding and releasing \( \text{O}_2 \) from the hemoglobin. For simplification, we assume that the concentration of free \( \text{O}_2 \) is dependent on the hemoglobin (Hb) saturation as:

\[
S = \frac{p_{\text{O}_2}^5}{p_{\text{O}_2}^5 + P_{50}^5}
\]

(4)

where \( S \) is the saturation of hemoglobin by \( \text{O}_2 \) (from 0 to 100%), \( p_{\text{O}_2} \) is the partial pressure of \( \text{O}_2 \), \( n \) the Hill’s coefficient (\( n = 2.7 \)) and \( P_{50} \) is the partial pressure of \( \text{O}_2 \) for saturation of 50% (\( P_{50} = 26.6 \) mmHg).

Using the \( \text{O}_2 \) saturation curve and concentration of saturated Hb, and performing a linearization assumption of the \( \frac{\partial S}{\partial p_{\text{O}_2}} \) term as shown by Moore and Ethier [15], the mass transfer for \( \text{O}_2 \) is defined as:

\[
\left(1 + \frac{[\text{Hb}]}{a} \frac{\alpha}{p_{\text{O}_2}} (1 - S)\right) \frac{\partial p_{\text{O}_2}}{\partial t} + \mathbf{v} \cdot \nabla p_{\text{O}_2} = \nabla \cdot \left(D_{\text{HbO}_2} \mathbf{v}ight) - \frac{\partial S}{\partial p_{\text{O}_2}} \mathbf{v} \cdot \nabla c_{\text{HbO}_2}
\]

(5)

where \( a \) is the solubility coefficient of oxygen, \( D_{\text{HbO}_2} \) is the \( \text{O}_2 \) diffusion coefficient in blood, \([\text{Hb}]\) is oxygen carrying capacity of hemoglobin in blood, and \( \alpha \) is the oxyhemoglobin diffusion coefficient in blood. In this equation, the coefficient on the right-hand side is a non-constant diffusivity of oxygen and the coefficient on the left-hand side as a non-constant carrying capacity of oxygen, respectively. The linearization assumption was shown to be a reasonable simplification of the biological processes as shown by Moore and Ethier for idealized arteries [15] and in our previous study for mass transport of \( \text{O}_2 \) in the cerebrovascular system [27].

For the \( \text{O}_2 \) transport in the aortic wall, the convection term is omitted and we model the process by only considering pure diffusion:

\[
\sigma_f \frac{\partial p_{\text{O}_2}}{\partial t} = \sigma_f \mathbf{v} \cdot (D_{\text{wO}_2} \nabla p_{\text{O}_2}) - r_{w_{\text{O}_2}}
\]

(6)

where \( \sigma_f \) is the \( \text{O}_2 \) solubility in the wall, \( D_{\text{wO}_2} \) is the \( \text{O}_2 \) diffusion coefficient in the wall, and \( r_{w_{\text{O}_2}} \) is the volumetric \( \text{O}_2 \) consumption rate by the wall.

2.3.3. Mass transport of NO

Production of NO occurs in the endothelial layer of the wall and is moderated by local WSS. We have assumed a linear dependency of NO production (\( r_{\text{NO}} \)) on WSS, defined similarly to Chen et al. [20]:

\[
r_{\text{NO}} = r_{\text{ref}} \frac{\|\mathbf{v}\|}{r_{\text{ref}}}
\]

(7)

where \( r_{\text{ref}} \) is the reference production rate, \( \|\mathbf{v}\| \) is the WSS magnitude at the wall, and \( r_{\text{ref}} \) is the reference wall shear stress. The mass transport of NO in the lumen is modeled using the convection–diffusion equation:

\[
\frac{\partial c_{\text{NO}}}{\partial t} + \mathbf{v} \cdot (c_{\text{NO}} \mathbf{v}) = \mathbf{v} \cdot (D_{\text{fNO}} \nabla c_{\text{NO}}) - r_{f_{\text{NO}}}
\]

(8)

where \( c_{\text{NO}} \) is the NO concentration, \( D_{\text{fNO}} \) is the diffusion coefficient of NO in blood, and \( r_{f_{\text{NO}}} \) is the consumption rate of NO by erythrocytes and oxygenation with oxygen, defined as:

\[
r_{f_{\text{NO}}} = k_{\text{NO}} c_{\text{NO}}^2 + k_{\text{NO}_2} c_{\text{NO}_2} c_{\text{O}_2}
\]

(9)

where \( k_{\text{NO}} \) is the auto-oxidative NO reaction rate and \( k_{\text{NO}_2} \) is the NO reaction rate with erythrocytes. The NO flux from the endothelium to the lumen (\( J_{f_{\text{NO}}} \)) was determined using:

\[
J_{f_{\text{NO}}} = A D_{f_{\text{NO}}} \frac{dc_{\text{NO}}}{dr} |_{w_{\text{endo}}}
\]

(10)

Finally, in the wall, the NO transport is assumed to be diffusion driven:

\[
\frac{\partial c_{\text{NO}}}{\partial t} + \mathbf{v} \cdot \left(D_{\text{wNO}} \nabla c_{\text{NO}}\right) = r_{w_{\text{NO}}}
\]

(11)

2.3.4. Boundary conditions and modeling of aortic wall

Fig. 2 visualizes the different domains (lumen (\( \Omega_l \)) and wall (\( \Omega_w \)) zones) and boundaries (lumen inlet (\( \Gamma_{\text{in}}^l \)), wall inlet (\( \Gamma_{\text{in}}^w \)), lumen outlet (\( \Gamma_{\text{out}}^l \)), wall outlet (\( \Gamma_{\text{out}}^w \)), outside wall (\( \Gamma_{\text{wall}} \)), and lumen-wall interface (\( \Gamma_{\text{l-wall}} \)) for lumen-only (a) and lumen-wall (b) simulations. In addition, Fig. 2 also visualizes the dominant means of \( \text{O}_2 \) and NO mass transport (either convection or diffusion) within the different zones of the computational domain.

We treated the wall as a homogeneous porous medium with modeled superficial velocity as:

\[
S_i = \left( \frac{a_{\text{w}}}{a_{\text{w}}} + C_{2w} \frac{1}{2} \left(\frac{\|\mathbf{v}\|}{r_{\text{ref}}}\right)^2 \right)
\]

(12)

where \( S_i \) is the source term for the \( i \)th (\( x \), \( y \), or \( z \)) momentum equation, \( a_{\text{w}} \) is the aortic wall permeability, and \( C_{2w} \) is the inertial resistance.

Flow boundary conditions: The inlet boundary condition (\( \Gamma_{\text{in}}^l \)) was specified as a plug velocity profile using the time-dependent velocity information at the inlet extracted from the reconstructed 4D-flow MRI. The data points for the average velocity at the inlet (\( n_{HC} = 34, n_p = 32 \)) were interpolated in time using linear interpolation, Fig. 1(c) for HC and (d) for P.

The outlet boundaries (\( \Gamma_{\text{out}}^l \)) were treated for both cases with the assumption of zero-diffusive flux (for all the flow variables) and a mass balance correction. Specifically for the HC and P, each outlet was assigned a fraction of the flow (\( u_{\text{w}} \)), which was defined as:

\[
u_{\text{w}} = \frac{Q_{\text{w}}}{Q_i} \frac{1}{\sum_{m=1}^{M} u_m}
\]

(13)

where \( Q_{\text{w}} \) is the flow at the respective outlets and \( M \) is the total number of outlets (\( M_{HC} = 3, M_P = 4 \)). The fluid-wall interface (\( \Gamma_{\text{f-w}} \)), endothelium, was treated as a simplified one-dimensional representation of a thin membrane, with specified pressure drop \( \Delta p \):

\[
\Delta p = \left( \frac{\mu}{a_{\text{f-w}}} \mathbf{v} + C_{2f-w} \frac{1}{2} \mathbf{v}^2 \right) \Delta m
\]

(14)

where \( a_{\text{f-w}} \) represents the permeability of endothelium, \( C_{2f-w} \) is the pressure jump coefficient, and \( \Delta m \) is the endothelial thickness. The
from Gijsen et al. [31]. The density of the complete mixture was defined as

\[ \rho = \sum_i Y_i \rho_i \]

where \( \rho_i \) is the density of species \( i \), and \( Y_i \) is the volume fraction of species \( i \). The power-law index was defined similarly for each species.

2.3.5. Physical properties

The boundary conditions for \( O_2 \) and \( NO \) at the boundaries shown in Fig. 2 were as follows:

(a) \( \Gamma_{ext}(O_2) \): zero normal gradient for \( O_2 \) and \( NO \)

(b) \( \Gamma_{in}(O_2) \): \( \rho_{O_2} \) = 1060 kg/m³, \( \rho_{NO} = 0 \) mmHg

(c) \( \Gamma_{ext}(NO) \): \( \rho_{NO} \) = 8.48e-10 m³/s

(d) \( \Gamma_{in}(NO) \): \( \rho_{NO} \) = 0.91e-9 m³/s

(e) \( \rho_{O_2} \) = 20 ml O₂/ml blood, \( \rho_{NO} \) = 5 ml O₂/ml blood

where \( Y_i \) and \( \rho_i \) are the mass fraction and density of species \( i \), respectively. The density for the respective species was defined as \( \rho_{blood} = 1060 \) kg/m³, \( \rho_{O_2} = 1.29 \) kg/m³, and \( \rho_{NO} = 1.34 \) kg/m³. Since \( \rho_{blood} \gg (\rho_{O_2} + \rho_{NO}) \) the effective density was close to \( \rho_{blood} \) with average fluid density \( \bar{\rho} = 1057.76 \) kg/m³. The values for all other biological parameters can be found in Table 3.

2.3.6. Mesh and numerical setup

For both of the studied cases concerning lumen-only simulations, we have created a polyhedral mesh with refinement consisting of ten layers close to the wall \( (\Gamma_{int}) \). The mesh dependency was performed for one of the cases (HC) at the peak-systolic conditions. Appendix. The final meshes consisted of approximately 2.3 mil. cells for HC and 2.2 mil. cells for P.

The mesh consisted of polyhedral elements for the lumen-wall simulations, with refinement close to the fluid-wall interface. Appendix. The final meshes for lumen-wall simulations consisted of 6.2 mil. cells for HC and 6.5 mil. cells for P.

The simulations were performed using Ansys Fluent 2019 R3 (Ansys, Canonsburg, Pennsylvania, US). The solver setup for this study was as follows: (1) pressure-based solver; (2) PISO for pressure-velocity coupling; (3) second-order upwind discretization for all quantities; (4) implicit time discretization; (5) residuals lower than 1 × 10⁻⁶.

2.3.7. Post-processing and data analysis

MROI-based WSS was estimated using CAAS MR Solutions v5.2, similarly as described in our previous publication [14]. To analyze the hemodynamics and mass transfer of species, we have calculated several (time-averaged) quantities. From the hemodynamical properties, first, the time-averaged wall shear stress \( (TAWSS) \) was calculated using the following:

\[ TAWSS = \frac{1}{T} \frac{1}{A} \int_0^T \left| \tau_w(x) \right| dt \]

where \( T \) is the cycle length. The oscillatory shear index (OSI) was calculated as follows:

\[ \text{OSI} = \frac{1}{\tau_0^0} \left( \int_0^{\tau_0} \tau_0(x) dt - \int_0^{\tau_0} \tau_w(x) dt \right) \]

\[ \int_0^{\tau_0} \tau_0(x) dt = \int_0^{\tau_0} \tau_w(x) dt \]

\[ \int_0^{\tau_0} \tau_0(x) dt \approx \frac{1}{2} \int_0^{\tau_0} \tau_w(x) dt \]

where \( \tau_0(x) \) is the instantaneous shear stress on the wall, and \( \tau_w(x) \) is the time-averaged shear stress on the wall.

\[ \tau_0(x) = \int_0^{\tau_0} \tau_0(x) dt / \tau_0 \]

\[ \tau_w(x) = \frac{1}{\tau_0} \int_0^{\tau_0} \tau_w(x) dt \]

\[ \int_0^{\tau_0} \tau_0(x) dt \approx \frac{1}{2} \int_0^{\tau_0} \tau_w(x) dt \]

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\[ \int_0^{\tau_0} \tau_0(x) dt \approx \frac{1}{2} \int_0^{\tau_0} \tau_w(x) dt \]
Table 4
The maximal, mean, and standard deviation (\(\sigma\)) of wall shear stress (WSS) for healthy control and patient based on MRI and CFD.

<table>
<thead>
<tr>
<th></th>
<th>MRI WSS(_{\text{max}}) [Pa]</th>
<th>CFD WSS(_{\text{max}}) [Pa]</th>
<th>(\sigma) [Pa]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Healthy</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Control</td>
<td>4.36</td>
<td>65.16</td>
<td>0.62</td>
</tr>
<tr>
<td>Patient</td>
<td>3.29</td>
<td>69.57</td>
<td>0.51</td>
</tr>
</tbody>
</table>

Finally, the endothelial cell activation potential (ECAP) was calculated as:

\[
\text{ECAP} = \frac{\text{OSI}}{\text{TAWSS}} \tag{19}
\]

To study the mass transfer of \(O_2\) and NO close to the wall, we have calculated the Sherwood number for species \(i\) (\(\text{Sh}_i\)) as

\[
\text{Sh}_i = \frac{1}{\nu} \frac{\partial c_i}{\partial n} \left|_w \right. - \frac{c_i}{c_{ib}} \tag{20}
\]

where \(c_i\) is the local concentration of species \(i\), \(c_{ib}\) is the bulk concentration of the species, and \(c_{iw}\) is the concentration at the wall. The time-averaged \(\text{Sh}_i\) can be written as

\[
\text{TASh}_i = \frac{1}{T} \int_0^T \text{Sh}_i \ dt \tag{21}
\]

To estimate the hypoxic area for lumen-only simulations, the species’ consumption rate within the wall must be determined. For this, the rate of species consumption can be estimated using non-dimensional Damköhler number (\(\text{Da}\)), defined as:

\[
\text{Da} = \frac{\dot{Q}_{O_2} T_a}{K \Delta O_2 p_{O_2} b} \tag{22}
\]

where \(\dot{Q}_{O_2}\) is the oxygen consumption rate of arterial tissue, \(T_a\) is the arterial wall thickness, \(a\) is the mean arterial diameter, \(K\) is Henry’s constant, \(\Delta O_2\) is the oxygen diffusion coefficient and \(p_{O_2}\) is the bulk partial pressure of oxygen. The region that suffers from hypoxia due to mass transfer limitations is characterized by the \(O_2\) transport being lower than its consumption by the wall, or \(\text{Sh}_{O_2} < \text{Da}\).

Finally, we have defined a few specific parts of the aorta used for further analysis, as shown in Fig. 1. The specific regions are: ascending aorta (AscAo), aortic arch (Arch), and descending aorta (DescAo) (for both subjects). In addition, aortic root (AoR) was defined for analysis of HC and thoracic aortic aorta (TAA) for P.

3. Results

3.1. Validation of hemodynamics in lumen

Fig. 3 shows the comparison of MRI normalized WSS (WSS/WSS\(_{\text{ave}}\)) to the CFD simulated results. WSS was normalized using the respective average values of WSS for MRI and CFD. The data are visualized at peak systole for both HC (Fig. 3(a)) and P (Fig. 3(b)).

The maximal and average values and standard deviation (\(\sigma\)) of WSS for each of the cases and methods can be seen in Table 4.

3.2. Time-averaged hemodynamics in lumen

The time-averaged quantities that quantify the hemodynamics close to the aortic wall are shown in Fig. 4 for both HC and P. We have visualized the time-averaged wall shear stress (TAWSS [Pa]), Oscillatory Shear Index (OSI [-]), and the Endothelial Cell Activation Potential (ECAP [Pa\(^{-1}\)]). For both HC and P, the color bar limits are set to the same values to allow an adequate comparison.
3.3. Mass transfer of O$_2$ and NO in lumen

To study the effects of O$_2$ and NO mass transfer in the lumen, we have calculated and visualized the time-average Sherwood number (TASh \([-\]) for the different species in Fig. 5. For O$_2$, TASh$_{O2}$ is shown for two different modes of transport are shown—passive (top) and active (bottom). The data range for the passive TASh$_{O2}$ is half of active TASh$_{O2}$.

Fig. 5(b) and (d) also show the estimated hypoxic regions for passive and active O$_2$ mass transport. The locations of hypoxia occur if the O$_2$ mass transfer towards the wall (Sh) is lower than its consumption by the wall (Da), i.e., if TASh < Da applies. We have estimated Da as defined in Eq. (22), separately for HC and P based on the average diameter of the aorta (healthy portion only for P). The estimated values were: Da$_{HC} = 290$ for HC and Da$_{P} = 304$ for P. Additionally, we have calculated the relative percentage area affected by hypoxia (A$_{hyp}$), defined as the hypoxic area per the total area, in the ascending aorta (AscAo), aortic arch (Arch) and descending aorta—DescAo. A$_{hyp}$ for both studied subjects is shown in Table 5 for passive and active O$_2$ transport.

Finally, Fig. 6(b) shows the time-averaged Sh for NO (TASh$_{NO}$ \([-\]) for both studied cases.

Next, we have visualized the circumferential average of various hemodynamic quantities (TAWSS, OSI, and ECAP) together with TASh for NO and O$_2$ (passive and active) alongside the normalized centerline length (l/$l_{max}$) for both studied subjects, Fig. 7. The centerline length was normalized by its maximum (l$_{max}$), and the different sections of the aorta are highlighted (ascending aorta—AscAo, aortic arch—Arch, descending aorta—DescAo, for H only aortic root—AoR, and for P only aneurysm—TAA); the evaluated variables are: relative percentage hypoxic area for passive (A$_{hypP}$) and active (A$_{hypA}$) transport, time-averaged wall shear stress (TAWSS), oscillatory shear index (OSI), endothelial cell activity potential (ECAP), time-averaged Sherwood number for passive oxygen transport (TASh$_{O2P}$), active oxygen transport (TASh$_{O2A}$), and nitric oxide transport (TASh$_{NO}$).

Until now, we have primarily focused on the absolute behavior of the cardiac cycle by analyzing the time-averaged quantities. While this approach allows for understanding the complete mass transfer and blood flow behavior, it may cause the concealment of specific details due to the averaging. Therefore, we have extracted data at peak systole alongside two lines (inseam and outseam) for both studied subjects, as shown in Fig. 8. We have visualized WSS with Sh for NO and active O$_2$ mass transport. The length of the inseam and outseam (l) were non-denationalized using the respective maximal values. Finally, the boundaries for the specific regions of interest are highlighted.

### Table 5

Average values of hemodynamic mass transfer properties for healthy control (HC) and patient (P) within specific sections of aorta (ascending aorta—AscAo, aortic arch—Arch, descending aorta—DescAo, for H only aortic root—AoR, and for P only aneurysm—TAA); the evaluated variables are: relative percentage hypoxic area for passive (A$_{hypP}$) and active (A$_{hypA}$) transport, time-averaged wall shear stress (TAWSS), oscillatory shear index (OSI), endothelial cell activity potential (ECAP), time-averaged Sherwood number for passive oxygen transport (TASh$_{O2P}$), active oxygen transport (TASh$_{O2A}$), and nitric oxide transport (TASh$_{NO}$).

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<thead>
<tr>
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<th>Patient</th>
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<tbody>
<tr>
<td>TAWSS [Pa]</td>
<td>0.95 0.90 0.65</td>
<td>1.06 1.49 2.06 1.63</td>
</tr>
<tr>
<td>OSI [-]</td>
<td>0.21 0.16 0.21</td>
<td>0.23 0.13 0.09 0.17</td>
</tr>
<tr>
<td>ECAP [Pa$^{-1}$]</td>
<td>0.37 0.18 0.34</td>
<td>0.25 0.29 0.06 0.13</td>
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<table>
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<tr>
<th>Mass transfer</th>
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<th>Patient</th>
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<tbody>
<tr>
<td>TASh$_{O2P}$ [-]</td>
<td>286 316 179</td>
<td>322 260 416 298</td>
</tr>
<tr>
<td>TASh$_{O2A}$ [-]</td>
<td>643 686 559</td>
<td>671 623 745 660</td>
</tr>
<tr>
<td>TASh$_{NO}$ [-]</td>
<td>311 280 432</td>
<td>301 351 199 338</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Hypoxic area</th>
<th>Healthy control</th>
<th>Patient</th>
</tr>
</thead>
<tbody>
<tr>
<td>A$_{hypP}$ [%]</td>
<td>50 43 88</td>
<td>38 58 19 47</td>
</tr>
<tr>
<td>A$_{hypA}$ [%]</td>
<td>2.2 2.6 3.9</td>
<td>1.3 3.5 0.8 1.6</td>
</tr>
</tbody>
</table>
Fig. 7. Circumferential average alongside the normalized centerline length ($\ell/\ell_{\text{max}}$) for: time-averaged wall shear stress (TAWSS [Pa]), oscillatory shear index (OSI [−]), endothelial cell activation potential (ECAP [Pa−1]), Time-averaged Sherwood number for active oxygen (TASh$_{O_2}$ [-]), and Time-averaged Sherwood number for nitric oxide (TASh$_{NO}$ [-]); for healthy control (a) and patient (b) in the lumen-only approximation of aorta; we divided the domain to highlight the ascending aorta (AscAo), aortic arch (Arch), descending aorta (DescAo), and aneurysm (TAA—for the patient only).

Fig. 8. Wall shear stress (WSS [Pa]), Sherwood number for active oxygen (Sh$_{O_2}$ [-]), and Sherwood number for nitric oxide (Sh$_{NO}$ [-]) alongside the normalized centerline length ($\ell/\ell_{\text{max}}$) extracted alongside the inseam and outseam for: healthy control (a) and patient (b) in the lumen-only approximation of aorta; the domain is divided to highlight the ascending aorta (AscAo), aortic arch (Arch), descending aorta (DescAo), and aneurysm (TAA—for the patient only).
3.4. Mass transfer of O$_2$ and NO in aortic wall

Fig. 9 shows the normalized concentration of O$_2$ ($c^{O_2}/c^{O_2}_{max} [-]$) and NO ($c^{NO}/c^{NO}_{max} [-]$) visualized at different locations of interest (A - root, B - ascending aorta, C - after arch) alongside with the velocity field with normalized velocity magnitude ($v/v_{in} [-]$) for peak systole. The concentration of both species was normalized using the inlet (maximal) $c^{O_2}_{max}$ for O$_2$ and global maximum $c^{NO}_{max}$ for NO. The velocity magnitude was normalized using the average velocity at the inlet $v_{in}$. Additionally, the data are visualized alongside the lines extracted from (A1 and C1) in Fig. 10. We visualized the data alongside a normalized diameter of the particular slice ($d/d_{max}$), with $d_{max}$ being the maximal lumen diameter of the slice.

4. Discussion

In this study, we have conducted simulations of blood flow and combined mass transfer of O$_2$ and NO in a subject-specific aorta and its wall, focusing on two cases: a healthy control (HC) and a patient (P) with a root aneurysm. The simulations were based on 4D-flow MRI measurements, from which geometry and boundary flow conditions were extracted. To examine flow dynamics in the wall, we have developed a simplified, single-layer model of the aortic wall, featuring a constant thickness and physical properties based on the average of intima, media, and adventitia.

Since the information for the blood flow was derived from a single 4D-flow MRI measurement, we used this data to validate our simulated flow field within the lumen. Comparing normalized values of WSS for
both cases at peak systole, the simulated blood flow shows similar behavior to the measured one. We note that while there are some differences between the two methods, as reported in our previous studies [13,14,27], the data from both methods agree well in capturing the global behavior of WSS including areas of local maximal and minimal values. We conclude that the blood flow data obtained from simulations adequately represent reality, as demonstrated in our earlier research [13,14].

Besides WSS within the aorta, several previous studies have focused on time-averaged hemodynamical quantities to establish potential biomarkers for the progression of TAA. In this study, we have explored potential biomarkers for the progression of TAA by examining the effects of time-averaged hemodynamical quantities such as TAWSS, OSI, and ECAP, as shown in Fig. 4, in both HC and P cases. When comparing the healthy and aneurysmal cases, the section suffering from TAA indicates few striking characteristics. For instance, TAWSS shows a global minimum in the area of TAA, similar to previously reported behavior in TAA and AAA [33,34]. Moreover, TAA also suffers from higher OSI than the healthy aorta, and the ECAP is significantly higher in the location of TAA compared to the rest of the aorta. These three characteristics indicate a potentially higher risk for additional growth or rupture due to impaired endothelial cell activity. Endothelial cells respond to non-physiological values of WSS and change in the direction of WSS during the cardiac cycle in various ways [35,36], which, among others, affects the production of different species (like NO). However, since we have only simulated two subjects, we cannot conclude whether TAWSS, OSI, and ECAP are reliable predictors of aneurysms. Instead, we suggest that these hemodynamical indicators should be further investigated in a large population study with multiple HC and patients with TAA, as we observed apparent differences between HC and P in these variables. Moreover, to determine if these biomarkers are associated with aneurysm growth, longitudinal data are necessary to be included in the analysis.

We also highlight the region of the AscAo immediately following the TAA. In this region, the artery experiences a sudden increase in TAWSS (in the transition between TAA and the ‘healthy’ part), as can be observed in Fig. 7. This behavior is also evident in the instantaneous WSS at peak systole, as depicted in Fig. 8. Additionally, a sudden increase in OSI and ECAP occurs further downstream of the TAA, as shown in Fig. 7. In contrast, such behavior is not evident in the AscAo of HC. These findings suggest that a further aberrant blood flow occurs downstream of TAA, potentially leading to additional growth, the genesis of the secondary aneurysm, or even the onset of aortic dissection (AD). Consistent with this observation, Peng et al. have demonstrated a strong correlation between the hemodynamics close to the tear in AD and aberrant blood flow, as well as high OSI [37]. Furthermore, TAA is considered a risk factor for AD [1].

In addition to hemodynamics, we also simulated the mass transfer of O$_2$ and NO in the lumen and aortic wall. Within the lumen, both species show non-uniform distribution. Moreover, we found an inverse correlation between the two species, as regions with lower O$_2$ exhibited higher NO concentration and vice-versa, as depicted in Fig. 7 for the time-averaged quantities and in Fig. 8 for instantaneous mass transfer at peak systole. We can also observe similar behavior regarding concentration boundary layer thickness within the lumen. For both cases, the boundary layer is very thin, with a sudden decrease in concentration for both species. The observed relationship can be explained by the relative thickness of the concentration boundary layer compared to the momentum boundary layer, expressed in Schmidt number (Sc). For both species, Sc is very high, with values of Sc_{NO} $\sim$ 1000 for NO and Sc_{O_2} $\sim$ 3000 for passive and active O$_2$ respectively. Thus, NO is almost instantly consumed within the lumen, and the O$_2$ concentration gradient at the wall is very steep, with minimal influence from lumen-side mass transfer limitations. Similar observations were previously reported for idealized arteries by Plata et al. for NO [19] and Moore and Ethier for O$_2$ [15], as well as for mass transfer in aorta [21].

In regard to O$_2$ mass transfer, this phenomenon is also manifested in the estimation of hypoxic regions within the aorta. The hypoxic area can be estimated by comparing the mass transfer towards the wall (Sh) with the estimated consumption of the wall (Da). In our study, the hypoxic region occurred if Sh was lower than Da = 290 for HC and Da = 304 for P. Notably, the estimated hypoxic area for passive O$_2$ is much greater than for the active O$_2$. For the latter mentioned, just one to four percent of the total aortic area suffers from estimated hypoxia. In addition, we can observe subtle differences between HC and P. The hypoxic area is lower in P, particularly in DescAo, which could also be attributed to the estimated value of Da. Moreover, Da was estimated to be lower in HC. This discrepancy in Da was influenced by the calculated average diameter (q) of the artery, which was higher for P, even though we excluded the majority of TAA from the calculations. To address this limitation, an adaptive calculation of Da should be employed.
with variable $a$ as a function of centerline distance. However, when considering only estimated hypoxia in P, no significant differences between the healthy tissue and TAA are apparent.

Nevertheless, the impact of hemodynamics on $O_2$ concentration persists. In the case of P, a distinct recirculation zone is evident just after the arch (slice C in Fig. 9). This recirculation zone causes a slight reduction in $O_2$ concentration. Similar hemodynamics-induced variations in concentration were previously observed in the stenotic region of the carotid artery [18]. Thus, monitoring areas with aberrant blood flow within the aorta is crucial, as prolonged hypoxia can trigger extracellular matrix remodeling and degradation [38] and play an essential factor in aneurysm pathogenesis [39].

The distribution of NO closely follows the TAWSS distribution in the aorta since WSS triggers NO production. Consequently, NO is unevenly distributed in the lumen and the aortic wall, as can be observed in our simulations as well as previously reported NO distribution in the aortic wall [21] and in coronary arteries [23]. Notably, the distribution of NO within the aortic wall differs significantly between P and HC, particularly near the root, as shown in Figs. 9 and 10, due to the presence of TAA. Here, the gradient in NO concentration is very high between the inner and outer curves of the aorta, with additional disruptions in the proximity of the inner curve. These variations could indicate dysfunction of the arterial wall due to uneven stimulation of smooth muscle cells within TAA, which may contribute to further growth.

We identified several limitations in our study. Firstly, we restricted our analysis to only two subjects, precluding us from drawing a statistically significant conclusion regarding the effects of limitations in $O_2$ and NO transport on aortic aneurysm development. To enable us to draw definitive conclusions, it is imperative that we expand our sample size to include a more substantial pool of healthy controls and patients, taking into account diverse locations of aortic aneurysms. Nonetheless, our study was primarily aimed at establishing a framework for modeling species transport and proposing a set of hemodynamic and biochemical indicators that could be evaluated in more significant population studies. Secondly, while numerous studies presented approaches for a multi-layer representation of (simple) arterial wall [40,41], we assumed a homogeneous single-layer aortic wall approximation. In reality, the aortic wall is composed of three layers (intima, media, and adventitia), each exhibiting unique physiological behavior. Therefore, our model lacks the capacity to determine the nature of mass transfer in each of the layers. However, we established the properties of the wall using scaled averages based on the respective properties of intima, media, and adventitia, thereby creating a model of the wall with overall average properties identical to a three-layer wall model. Thus, while we cannot provide insights into the specific behavior of each layer, we can reasonably capture the understanding of joined dynamics, especially for identifying hypoxia. Thirdly, we assumed a plug velocity profile at the inlet instead of a realistic one. However, our prior research has shown that if the root of the aorta is segmented correctly (as in our studied domains), the differences between the plug velocity profile and actual velocity profile are minimal [42]. Finally, the most significant limitation of our study is the absence of validation of $O_2$ and NO concentration within the aortic wall and lumen with direct measurements. The lack of validation originates from the current limitations of available methods for (in)direct non-invasive examination of these species in human arteries [9–12]. While an indirect comparison of our results can be made with invasive experiments that report on the concentration of $O_2$ using the hot cathode method on animal models [43,44], a direct comparison is not presently possible.

5. Summary and conclusions

This study aimed to simulate the mass transfer of $O_2$ and NO in the aorta of healthy control (HC) and patient (P) with root thoracic aortic aneurysm (TAA). To achieve this, a complex model was developed for the mass transfer of both species, incorporating hemoglobin-based transfer of $O_2$ in the domain, production of NO based on the local variation of WSS, and mass transfer (via diffusion) and consumption of both species in the arterial wall. The arterial wall was constructed with a single-layer assumption with homogeneous physical properties based on the average behavior of intima, media, and adventitia. Both simulations (HC and P) were based on 4D-flow MRI, with geometry and boundary conditions at the inlet and outlet directly based on the measurements. The simulated velocity field and WSS were validated against measured data, demonstrating good agreement.

The study revealed significant differences in hemodynamics between P and HC in and around the root, where P developed TAA. In these regions, WSS was markedly lower, while OSI and ECAP were elevated for P, whereas HC showed a more uniform distribution of these parameters. The distribution of $O_2$ and NO varied spatially in both the lumen and aortic wall, with apparent differences between healthy tissue and TAA in NO concentrations. In contrast, the concentration of $O_2$ was not influenced by the presence of TAA. However, the study demonstrated how aberrant blood flow could lead to hypoxia, indicating that $O_2$ should be monitored as a potential precursor for TAA pathogenesis.

In conclusion, the findings suggest that the studied quantities could be used as hemodynamical and biochemical predictors for TAA pathogenesis. However, due to the limited number of cases investigated, no statistically significant conclusions can be drawn. The authors propose that these hemodynamical and biochemical indicators be investigated in extensive population studies with multiple HC and patients with TAA, including longitudinal data. Such research could enhance the understanding of the aortic lumen and wall processes and ultimately improve the diagnosis and treatment of TAA.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Funding

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Data availability

The data supporting this article have been uploaded to the data repository Dryad (https://doi.org/10.5061/dryad.2rbnzs7sq).

Appendix. Mesh dependency

Our mesh dependency analysis focused on two aspects:

1. Lumen-only - dependency of the simulated results on the varying size of volume mesh for lumen-only geometry
2. Lumen-wall - dependency of the simulated results on the varying number of extruded layers close to the lumen-wall interface for simulations with wall included

In this section, we will elaborate on these mesh dependency studies. As part of the analysis, we have calculated the Grid Convergence Index (GCI) to quantify findings, as presented in Table A.6 for both cases.

Lumen-only

To perform the mesh dependency study, we have created three meshes: coarse ($\approx 1$ mil. polyhedral elements), medium ($\approx 2$ mil. polyhedral elements), and fine ($\approx 4$ mil polyhedral elements). After performing simulations, we compared WSS, as shown in Fig. A.11 at the surface (with detail on ascending aorta), and its local variation alongside an extracted line, as shown in Fig. A.12. We can see that the three meshes agree well upon qualitative analysis, with only a small variation.
detail on the ascending aorta and in Fig. A.14 for the local variation in mesh sensitivity analysis, as shown in Fig. A.13 for the surface with WSS alongside an extracted line. We have interpolated on the vasa vasorum, where we have performed the interface. Subsequently (for visualization and analysis purposes), WSS simulations to test the meshes and calculated WSS on the lumen-wall coarse, medium, and fine mesh, respectively. We performed blood flow of the lumen-wall interface, with two, five, and ten layers for the were the number of extruded layers (the wall side) in the proximity from the lumen-only analysis. The differences between the meshes created three meshes with volume settings based on the medium mesh is for the lumen-only approximation, using coarse, medium, and fine mesh.

Lumen-wall

We have adopted a different approach to the mesh sensitivity analysis for the case when the wall is included in the simulations. Here, we created three meshes with volume settings based on the medium mesh from the lumen-only analysis. The differences between the meshes were the number of extruded layers (the wall side) in the proximity of the lumen-wall interface, with two, five, and ten layers for the coarse, medium, and fine mesh, respectively. We performed blood flow simulations to test the meshes and calculated WSS on the lumen-wall interface. Subsequently (for visualization and analysis purposes), WSS was interpolated on the vasa vasorum, where we have performed the mesh sensitivity analysis, as shown in Fig. A.13 for the surface with detail on the ascending aorta and in Fig. A.14 for the local variation in WSS alongside an extracted line.

Table A.6

<table>
<thead>
<tr>
<th>Lumen-only</th>
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<tbody>
<tr>
<td>WSS₃ [Pa]</td>
<td>4.51</td>
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<td>WSS₂ [Pa]</td>
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<td>Asymptotic?</td>
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</tr>
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</table>

Fig. A.11. Wall shear stress (WSS [Pa]) for the healthy control with lumen-only approximation, using a coarse, medium, and fine mesh.

Fig. A.12. Extracted local Wall shear stress (WSS [Pa]) alongside the line visualized in (a) with normalized length l/lₘₐₓ, [-] where lₘₐₓ is the total distance of the line, for the healthy control with lumen-only approximation, using coarse, medium, and fine mesh.

References


