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Dynamics of coupled quantum systems

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Dynamics of Coupled Quantum Systems

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Cover: Abstract impression of two interacting Sachdev-Ye-Kitaev systems, produced with AI assistance.

To my love, Renata.

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