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## Dynamics of coupled quantum systems

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# Dynamics of Coupled Quantum Systems

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**Vladimir Ohanesjan**  
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Cover: Abstract impression of two interacting Sachdev-Ye-Kitaev systems, produced with AI assistance.

*To my love, Renata.*



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