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## Logarithmic approach to the double ramification cycle

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# **Logarithmic approach to the double ramification cycle**

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