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Leiden  
The Netherlands

## Algorithm selection and configuration for Noisy Intermediate Scale Quantum methods for industrial applications

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# Algorithm selection and configuration for Noisy Intermediate Scale Quantum methods for industrial applications

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door

Charles Moussa  
geboren te Saint-Claude, Guadeloupe, France  
in 1993

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Dr. M. Möller (Delft University of Technology)

*To my dear family and friends.*

“Great things are done by a series of small things brought together.”

Vincent Van Gogh, 1882

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