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Numerical exploration of statistical physics

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The cover was created by me, representing the synergy of the whole thesis in a single image.

To myself and my family.

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