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## **This is life: some thoughts on self-organized structure formation in active liquids and biological systems**

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