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Hysterons and pathways in mechanical metamaterials

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Hysterons and Pathways in Mechanical Metamaterials

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The cover shows the transition pathways of a biholey mechanical metamaterial with three hysteron.

To my family.

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