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## Spectral imaging and tomographic reconstruction methods for industrial applications

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# **Spectral imaging and tomographic reconstruction methods for industrial applications**

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