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Translational symmetry breaking in holographic strange metals

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- J. Zaanen, F. Balm, and A. Beekman, *Crystal Gravity*, SciPost Physics 13, 039 (2022).[287]
- N. Chagnet, F. Balm, and K. Schalm, *Proper Quantization of the Gubser-Rocha Einstein-Maxwell-Dilaton Model Reveals an Exactly Marginal Operator*, preprint arXiv:2209.13951.[99]
- F. Balm, N. Chagnet, S. Arend, J. Aretz, K. Grosvenor, M. Janse, O. Moors, J. Post, V. Ohanesjan, D. Rodriguez-Fernandez, K. Schalm and J. Zaanen. *T-linear resistivity, optical conductivity and Planckian transport for a holographic local quantum critical metal in a periodic potential*, preprint arXiv:2211.05492, prepared for submission to Physical Review X.[213]
- N. Chagnet, F. Balm, K. Schalm and J. Zaanen, *Umklapp Hydrodynamics*, to appear (2023).

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