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The Synchrony of Production & Escape: Half the Bright Ly α Emitters at $z \approx 2$ have Lyman Continuum Escape Fractions $\approx 50\%$

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ABSTRACT

The ionizing photon escape fraction (LyC f_{esc}) of star-forming galaxies is the single greatest unknown in the reionization budget. Stochastic sightline effects prohibit the direct separation of LyC leakers from non-leakers at significant redshifts. Here we circumvent this uncertainty by inferring f_{esc} using resolved ($R > 4000$) Ly α profiles from the X-SHOOTER Ly α survey at $z = 2$ (XLS- $z2$). With empirically motivated criteria, we use Ly α profiles to select leakers ($f_{\text{esc}} > 20\%$) and non-leakers ($f_{\text{esc}} < 5\%$) from a representative sample of $> 0.2L^*$ Lyman- α emitters (LAEs). We use median stacked spectra of these subsets over $\lambda_{\text{rest}} \approx 1000 - 8000\text{\AA}$ to investigate the conditions for LyC f_{esc} . Our stacks show similar mass, metallicity, M_{UV} , and β_{UV} . We find the following differences between leakers vs. non-leakers: (i) strong nebular CIV and HeII emission vs. non-detections, (ii) [OIII]/[OII] ≈ 8.5 vs. ≈ 3 , (iii) H α /H β indicating no dust vs. $E(B - V) \approx 0.3$, (iv) MgII emission close to the systemic velocity vs. redshifted, optically thick MgII, (v) Ly α f_{esc} of $\approx 50\%$ vs. $\approx 10\%$. The extreme EWs in leakers ([OIII]+H $\beta \approx 1100\text{\AA}$ rest-frame) constrain the characteristic timescale of LyC escape to $\approx 3 - 10$ Myr bursts when short-lived stars with the hardest ionizing spectra shine. The defining traits of leakers – extremely ionizing stellar populations, low column densities, a dust-free, high ionization state ISM – occur simultaneously in the $f_{\text{esc}} > 20\%$ stack, suggesting they are causally connected, and motivating why indicators like [OIII]/[OII] may suffice to constrain f_{esc} at $z > 6$ with *JWST*. The leakers comprise half our sample, have a median LyC $f_{\text{esc}} \approx 50\%$ (conservative range: 20 – 55%), and an ionising production efficiency $\log(\xi_{\text{ion}}/\text{Hz erg}^{-1}) \approx 25.9$ (conservative range: 25.7 – 25.9). These results show LAEs – the type of galaxies rare at $z \approx 2$, but that become the norm at higher redshift – are highly efficient ionizers, with extreme ξ_{ion} and prolific f_{esc} occurring in sync.

Key words: cosmology: observations – cosmology: dark ages, reionization, first stars – galaxies: high-redshift – intergalactic medium – ultraviolet: galaxies

1 INTRODUCTION

The Epoch of Reionization (EoR) was the last major phase transition of the Universe, when the first stars and galaxies announced their presence by ionizing the vast oceans of neutral Hydrogen (HI) they were born within (e.g. Loeb & Furlanetto 2013). While the timeline of reionization is increasingly well-constrained ($z \approx 6 - 9$, e.g., Fan

et al. 2006; Planck Collaboration et al. 2018; Mason et al. 2019), the protagonists of reionization remain elusive. Quasars, due to their rapidly fading numbers with increasing redshift, are unlikely to have played a significant role (e.g., Matsuoka et al. 2018; Kulkarni et al. 2019; Shen et al. 2020). Star-forming galaxies are the likeliest candidates, but whether the ionizing photon budget arose from a multitude of ultra-faint galaxies (“democratic reionization”, e.g., Finkelstein et al. 2019) or a rarer set of bright galaxies (“reionization by oligarchs”, e.g., Naidu et al. 2020) is a key open question with wide-ranging physical (e.g., reionization topology) and practical (e.g., survey design) implications (Hutter et al. 2021).

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The ionizing photon budget is typically parametrized as a product of three quantities (e.g., Madau et al. 1999; Robertson et al. 2013; Duncan & Conselice 2015) – the UV star-formation density (ρ_{UV}), a conversion factor between the UV luminosity and number of ionizing photons (ξ_{ion}), and the fraction of these photons that make it to the intergalactic medium (IGM) to ionize it (f_{esc}). ρ_{UV} is well-constrained down to $M_{UV} \approx -15$ during the EoR (e.g., Bouwens et al. 2021) with a clear path to fainter magnitudes with *JWST* (e.g., Labbe et al. 2021). Prospects of constraining ξ_{ion} are also bright (e.g., Chevillard et al. 2018). On the other hand, due to the opacity of the intervening intergalactic medium (IGM), f_{esc} may never be directly observed at $z \gtrsim 4$ (e.g., Inoue et al. 2014). Progress must therefore rely on measuring and understanding f_{esc} at lower redshifts.

In recent years, direct f_{esc} studies have largely concentrated on two redshift windows set by available UV instrumentation – one at $z \approx 0.3$ where Lyman continuum (LyC) is accessible to *HST/COS* (e.g., Izotov et al. 2016a, 2018b, 2021a; Wang et al. 2019, 2021), and another at $z \approx 2 - 4$ accessible to ground-based facilities and *HST/WFC3* UVIS (e.g., Jones et al. 2018; Smith et al. 2020; Ji et al. 2020; Meštrić et al. 2020; Marques-Chaves et al. 2021; Davis et al. 2021; Prichard et al. 2021). The $z \approx 0.3$ COS efforts were first undertaken at a time when only a handful of robust LyC leakers had been identified, and it was unclear whether LyC leakage even occurred among the $\gtrsim 0.5L^*$ galaxies for which f_{esc} measurements were feasible (e.g., Izotov et al. 2016a,b). Their selection functions prioritized rare galaxies with a high theorized probability of non-zero f_{esc} (e.g., compact, extreme $[O III]/[O II]$, elevated $H\beta$ EW starbursts, i.e., “Green Peas”). These programs have been remarkably successful in proving f_{esc} does occur among fairly luminous galaxies and in producing a sample of ≈ 20 galaxies with robust LyC constraints (e.g., Izotov et al. 2016a, 2018b, 2021a). However, the complex selection function and unknown number densities make generalizing these findings to higher redshifts and into the EoR difficult.

LyC studies at higher redshifts ($z \approx 2 - 4$) have simpler selection functions, but are hampered by drastic IGM line of sight variations (e.g., Inoue et al. 2014). Ideally, we would like to perform a controlled comparative experiment by constructing leaker and non-leaker stacks, and then contrasting their features to isolate indicators of f_{esc} . However, it is generally difficult to decide whether any individual detection/non-detection is due to high/low f_{esc} or due to a particularly transparent/opaque line of sight. To put numbers to the scale of the problem – for a randomly sampled IGM sightline, the difference between the 10th and 90th percentile transmission is $> 50\times$ at $z \approx 3$ (0.01 vs. 0.60, Steidel et al. 2018). Selecting apparent high f_{esc} and low f_{esc} leakers by applying mean IGM corrections amounts to comparing galaxies lying along transparent sightlines vs. opaque sightlines rather than high f_{esc} vs. low f_{esc} sources (e.g., Bassett et al. 2021). These ambiguities due to the IGM transmission are further compounded by viewing angle biases that hydrodynamical simulations show to be important due to the strong anisotropy of LyC f_{esc} (e.g., Gnedin et al. 2008; Wise & Cen 2009; Wise et al. 2014; Cen & Kimm 2015; Paardekooper et al. 2015). For instance, a galaxy may have high f_{esc} , but via holes pointed away from the observed sightline (e.g., Fletcher et al. 2019; Nakajima et al. 2020; Saxena et al. 2021).

Clearly, constructing pure, representative subsamples of leakers and non-leakers from direct LyC observations is challenging at high- z . Nonetheless, stacking sufficient ($\gtrsim 50$ at $z \approx 3$) galaxies from independently sampled sightlines is expected to produce a robust population-averaged f_{esc} (e.g., Steidel et al. 2018). The

current consensus is an average $f_{esc} \approx 5 - 10\%$ for $\gtrsim 0.5L^*$ Lyman-break galaxies (LBGs) at $z \approx 3$ (e.g., Marchi et al. 2017; Naidu et al. 2018; Pahl et al. 2021). The question then is, how do we translate this constraint on $z \approx 3$ LBGs to EoR LBGs. These are very different populations, with important properties such as the star-formation surface density (Σ_{SFR}), proposed to be causatively linked to f_{esc} (e.g., Heckman et al. 2011; Sharma et al. 2016; Naidu et al. 2020), rising $\approx 0.5 - 1$ dex higher (e.g., Oesch et al. 2010; Shibuya et al. 2019) as galaxies grow burstier towards the EoR (e.g., Faucher-Giguère 2018; Tacchella et al. 2020).

In this work, we propose resolved Lyman- α ($Ly\alpha$) emission-line spectroscopy is the panacea to the challenges around LyC f_{esc} . The resonant nature of $Ly\alpha$, which makes it highly sensitive to HI in the IGM, is routinely exploited to constrain the timeline of reionization (e.g., Stark et al. 2011; Pentericci et al. 2014; Mason et al. 2018). This resonant nature also renders the $Ly\alpha$ line profile sensitive to the HI distribution *within* galaxies. From the emergent sample of LyC leakers it is clear that $Ly\alpha$ profiles are the highest fidelity tracers of f_{esc} , both at low and high redshifts, and across several dex in physical properties like stellar mass, specific SFR, Σ_{SFR} , and $E(B - V)$ (e.g., Verhamme et al. 2017; Izotov et al. 2018b, 2021a; Vanzella et al. 2020). From a theory point of view, the interpretation is intuitive and well-understood – line profiles with tightly spaced narrow blue and red peaks, with flux emitted close to the systemic redshift (z_{sys}), signal a transparent, porous ISM with clear passages for $Ly\alpha$ (and LyC) escape. On the other hand, broad lines, widely separated peaks, and no photons at z_{sys} signal an ISM through which $Ly\alpha$ (and LyC) photons struggled to escape (e.g., Verhamme et al. 2015; Gronke et al. 2015a; Dijkstra et al. 2016; Kimm et al. 2019; Kakiichi & Gronke 2021).

There are significant advantages to studying LyC with $Ly\alpha$ profiles. The IGM, which severely hampers direct LyC observations, has little effect on $Ly\alpha$ profiles at $z \approx 2 - 3$ (e.g., Hayes et al. 2021) so any individual galaxy can be robustly classified as a likely leaker or a non-leaker. Perhaps most importantly, LyC constraints based on $Ly\alpha$ profiles can be extrapolated to higher redshifts with some confidence because LAEs at $z \approx 2 - 6$ are fundamentally similar – in e.g., their sizes (e.g., Malhotra et al. 2012; Paulino-Afonso et al. 2018), UV slopes (e.g., Santos et al. 2020), and $Ly\alpha$ line profiles corrected for IGM absorption (e.g., Hayes et al. 2021). Further, $Ly\alpha$ LFs are almost unevolving across $z \approx 2 - 6$, therefore a luminosity-limited survey at $z \approx 2$ would have a similar proportion of bright and faint LAEs as at higher redshifts (e.g., Sobral et al. 2018; Herenz et al. 2019; Ouchi et al. 2020).

Realizing the potential of resolved $Ly\alpha$ requires surveys with high spectral resolution at the $Ly\alpha$ wavelength ($R > 4000$, e.g., Verhamme et al. 2015) along with precise z_{sys} . Further, to ensure the generalizability of the results to higher redshifts, the selection function must be well known and ideally simple. The luminosity-limited ($L_{Ly\alpha} > 0.2L^*$) X-SHOOTER $Ly\alpha$ Survey at $z = 2$ (XLS- $z2$, Matthee et al. 2021), based on the narrow-band CALYMHHA Survey (Matthee et al. 2016; Sobral et al. 2017b), fulfils exactly these requirements. In this paper we use XLS- $z2$ to extract the first statistical constraints on LyC f_{esc} via resolved $Ly\alpha$ profiles. In a companion paper (Matthee & Naidu et al. 2021) we use these constraints to show how LAEs explain the evolution of the cosmic ionizing emissivity from $z \approx 2 - 8$.

A plan for this paper follows – in §2 we describe the XLS- $z2$ sample, in §3 we motivate the $Ly\alpha$ -profile based selection criteria for the “Low Escape” ($f_{esc} < 5\%$) and “High Escape” ($f_{esc} > 20\%$) stacks that we produce in §4. In §5 we describe the physical conditions for LyC f_{esc} based on the differences between these stacks,

in §6 we estimate the f_{esc} of our High Escape stack. We place our results in a broader context, while addressing concerns and caveats in §7, and end with a summary in §8. Throughout this work we reference L^* , the characteristic luminosity in Schechter function parametrizations of luminosity functions (LFs). In the context of Ly α LFs, the L^* is as per the Sobral et al. (2018) $z \approx 2 - 6$ consensus LFs ($\log L_{\text{Ly}\alpha}/\text{erg s}^{-1} \approx 43$). Magnitudes are in the AB system (e.g., Oke & Gunn 1983). For summary statistics, unless otherwise mentioned, we report medians with errors on the median from bootstrapping (16th and 84th percentiles). We assume a flat Λ CDM concordance cosmology with $\Omega_M = 0.3$, $\Omega_\Lambda = 0.7$ and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2 SAMPLE & DATA

2.1 $z \approx 2$ Sample

Our sample is drawn from the X-SHOOTER Ly α Survey at $z \approx 2$ (XLS- z 2), which is a deep spectroscopic survey of 35 LAEs (Matthee et al. 2021). The sample spans luminosities $0.2 - 10 \times L_{\text{Ly}\alpha}^*$ and $0.2 - 6 \times L_{\text{UV}}^*$ with a median rest-frame Ly α equivalent width (EW) of 82 Å. The majority of these LAEs have originally been discovered in wide-field narrow-band surveys in well-known extragalactic fields (e.g. Sobral et al. 2017a). Active Galactic Nuclei (AGN) were removed based on X-Ray and radio data (Calhau et al. 2020), and spectroscopy (Sobral et al. 2018). Most of the LAEs in the sample are Ly α -flux limited selected. A handful have been pre-selected based on the UV continuum in combination with a high ionisation state (i.e. [OIII]/H β) or the presence of high ionisation UV lines such as CIII] (see Matthee et al. 2021 for details). However, these properties are ubiquitous among typical $z \approx 2$ LAEs so we see no reason to exclude them from our sample. The luminosities of these LAEs are typical for the objects discovered in deep narrow-band surveys (e.g. Gawiser et al. 2007; Ouchi et al. 2008) and VLT/MUSE observations with ≈ 1 hour depth (e.g. MUSE-wide; Herenz et al. 2019).

In this paper we analyse 26 out of the 35 LAEs from XLS- z 2 (Table 1). The following objects were excluded from our analysis: XLS-1 because it was identified as an AGN, XLS-9 and XLS-13 as no systemic redshift was measured owing to their faintness, XLS-30 because its data does not cover the H α line, XLS-7, 8, 29, 31 because their Ly α EW is < 25 Å (the standard definition that Ly α LFs adopt for ‘‘LAE’’, e.g., Sobral et al. 2018) and XLS-27 because its Ly α line is significantly offset (by 9 kpc) from the rest-frame optical lines. We split the remaining 26 LAEs in subsets determined by their Ly α line-profile.

The sample of 26 sources we study here is representative of $L_{\text{Ly}\alpha} > 0.2L^*$ LAEs at $z \approx 2$. The median Ly α f_{esc} is $30 \pm 5\%$, in excellent agreement with measurements of typical LAEs that also find $\approx 30\%$ (Hayes et al. 2010; Song et al. 2014; Trainor et al. 2016; Sobral et al. 2017b; Harikane et al. 2018; Matthee et al. 2021). The median Ly α EW is 95 ± 16 Å, consistent with published EW distributions at similar redshifts (e.g., Gronwall et al. 2007; Hashimoto et al. 2017; Santos et al. 2020).

2.2 Data

The unique feature of XLS- z 2 is the combination of wide wavelength coverage ($\lambda_{\text{rest}} \approx 1000 - 8000$ Å at $z \approx 2$) with high spectral resolution for the Ly α line ($R \approx 4000 - 5000$) thanks to the X-SHOOTER echelle spectrograph on the VLT (Vernet et al. 2011).

The exposure times are ≈ 3 hours on average, which enables simultaneous measurements of systemic redshifts (through the rest-frame optical [OIII] and H α lines) along with sensitive Ly α spectroscopy. Redshift ≈ 2 is the lowest redshift where Ly α can be measured from the ground and the highest redshift where H α falls in the K band, enabling convenient estimates of Balmer decrements and Ly α escape fractions (e.g., Sobral & Matthee 2019). Another advantage at $z \approx 2$ is that the impact of the IGM on Ly α is negligible (e.g. Laursen et al. 2011; Hayes et al. 2021). The spectral resolution of XLS- z 2 is a factor $\gtrsim 3$ and $\gtrsim 5$ higher than the data used by Kulas et al. (2012) and Trainor et al. (2015) respectively, who previously studied Ly α profiles at $z \approx 2$ and is comparable to the study of a smaller sample ($N = 6$) by Hashimoto et al. (2015).

We use both 1D and 2D spectra in this analysis. Measurements in individual sources and stacks are based on 1D spectra extracted based on the position and size of the UV-continuum. The stacking has been performed in 2D (see Matthee et al. 2021 for details on the data reduction, spectral extraction and stacking procedures).

2.3 Ly α profile statistics

The individual Ly α profiles are shown in Appendix A. The typical integrated signal-to-noise ratio of the Ly α line is 20. A multiple peaked Ly α line is detected in 19/26 LAEs (i.e. 73%). As the blue peak is in all cases fainter than the red peak (typically containing $\approx 17\%$ of the total Ly α flux), it is possible, but unlikely given Ly α signal to noise ratio (SNR) >20 , that some blue peaks are missed due to their faintness. Out of the multiple peaked systems, 2/19 show three peaks with a clear peak at the systemic velocity (XLS-2 and XLS-21). Two multiple peaked LAEs show additional faint absorption profiles, either in the blue peak or in the red peak (XLS-18, XLS-33). One of the 7 single-peaked LAEs shows a relatively symmetric Ly α line at the systemic velocity (XLS-20).

2.4 Literature Sample of Lyman Continuum leakers

We design our criteria to select likely leakers and non-leakers based on Ly α profiles by constructing empirical criteria based on literature galaxies which have both direct LyC measurements as well as resolved ($R \gtrsim 4000$) Ly α profiles.

The bulk of our literature calibration sample is comprised of 20 $z \approx 0.3$ GPs studied with *HST*/COS compiled in Izotov et al. (2021a). LyC is directly measured at > 850 Å for these sources along with Ly α . The Ly α luminosities of the XLS- z 2 sample are well-matched to the luminosities of these low- z LyC leakers. Importantly for Ly α comparisons, the physical scale at $z \approx 0.3$ probed by the COS apertures is very similar to the physical scale ($\approx 7 - 10$ kpc) at $z \approx 2$ probed by the XLS z 2 slits. This ensures similar central regions of the Ly α emission are being captured. Also note that the spectral resolution for the XLS- z 2 Ly α profiles are comparable to the resolution of the *HST*/COS spectra of the GPs (Orlítóva et al. 2018), such that there is no differential effect. These GPs span $f_{\text{esc}} \approx 0\%$ to $f_{\text{esc}} \approx 70\%$, with four sources showing $f_{\text{esc}} > 20\%$.

At higher redshifts, while several LyC leaker candidates have been identified, very few have resolved Ly α measurements. These sources are: Ion2 ($z = 3.2$, Vanzella et al. 2016), Ion3 ($z = 4.0$, Vanzella et al. 2018), Sunburst Arc ($z = 2.4$, Rivera-Thorsen et al. 2019), GS-30668/XLS-26 ($z = 2.1$, Naidu et al. 2017, Matthee et al. 2021), GS-15601 ($z = 3.27$, J. Kerrut, in prep.). While few in number, all these sources show Ly α profiles with prominent emission at the systemic velocity resembling the highest f_{esc} $z \approx 0.3$ Green

Table 1. Ly α properties of our parent sample, split by their inferred LyC f_{esc} . The Ly α escape fraction ($f_{\text{esc,Ly}\alpha}$) is computed as $L_{\text{Ly}\alpha}/8.7 \times L_{\text{H}\alpha,\text{int}}$. (see e.g. Hayes 2015), where $L_{\text{H}\alpha,\text{int}}$ is the H α luminosity corrected for dust attenuation using the Balmer decrement and a Cardelli et al. 1989 attenuation law. The peak separation (v_{sep}) and central escape fraction (f_{cen}) are discussed in §3.1. † = No Blue Peak detected, * = Triple peak

ID	$f_{\text{esc,Ly}\alpha}$	$v_{\text{sep}}/\text{km s}^{-1}$	f_{cen}
High Escape			
(LyC $f_{\text{esc}} > 20\%$)			
XLS-2	$0.35^{+0.14}_{-0.23}$	$424 \pm 32^*$	0.162 ± 0.007
XLS-3	$0.77^{+0.32}_{-0.45}$	184 ± 13	0.243 ± 0.016
XLS-11	$0.55^{+0.38}_{-0.37}$	368 ± 15	0.287 ± 0.005
XLS-14	$0.40^{+0.24}_{-0.24}$	†	0.135 ± 0.037
XLS-17	$1.11^{+0.15}_{-0.12}$	246 ± 15	0.109 ± 0.004
XLS-18	$0.10^{+0.06}_{-0.04}$	†	0.110 ± 0.004
XLS-19	$0.32^{+0.35}_{-0.19}$	445 ± 15	0.208 ± 0.015
XLS-20	$0.27^{+0.37}_{-0.25}$	†	0.501 ± 0.013
XLS-21	$0.16^{+0.04}_{-0.06}$	$528 \pm 35^*$	0.233 ± 0.003
XLS-23	$0.41^{+0.19}_{-0.19}$	370 ± 14	0.314 ± 0.002
XLS-24	$0.64^{+0.40}_{-0.52}$	365 ± 17	0.153 ± 0.002
XLS-26	$0.25^{+0.13}_{-0.13}$	389 ± 16	0.364 ± 0.007
XLS-28	$0.35^{+0.09}_{-0.12}$	†	0.357 ± 0.013
Intermediate Escape			
(5% < LyC $f_{\text{esc}} < 20\%$)			
XLS-4	$0.43^{+0.67}_{-0.39}$	†	0.059 ± 0.017
XLS-5	$0.22^{+0.24}_{-0.17}$	336 ± 15	-0.006 ± 0.008
XLS-10	$0.02^{+0.27}_{-0.02}$	†	0.062 ± 0.014
XLS-34	$0.14^{+0.10}_{-0.08}$	635 ± 15	0.090 ± 0.003
Low Escape			
(LyC $f_{\text{esc}} < 5\%$)			
XLS-6	$0.71^{+0.36}_{-0.26}$	459 ± 16	0.006 ± 0.008
XLS-12	$0.07^{+0.04}_{-0.03}$	†	0.047 ± 0.007
XLS-15	$0.94^{+0.59}_{-0.37}$	412 ± 18	0.050 ± 0.009
XLS-16	$0.26^{+0.08}_{-0.09}$	611 ± 21	-0.020 ± 0.018
XLS-22	$0.32^{+0.09}_{-0.11}$	372 ± 15	0.004 ± 0.003
XLS-25	$0.21^{+0.10}_{-0.06}$	560 ± 15	0.037 ± 0.003
XLS-32	$0.04^{+0.05}_{-0.02}$	610 ± 29	-0.033 ± 0.011
XLS-33	$0.09^{+0.03}_{-0.03}$	417 ± 15	0.009 ± 0.003
XLS-35	$0.13^{+0.03}_{-0.04}$	470 ± 15	0.039 ± 0.002

Peas (see bottom panel of Fig. 1). This strongly suggests that systemic Ly α emission accompanies high LyC f_{esc} . A source detected in LyC at $z > 2$ despite the stochasticity of IGM transmission is likely to have high LyC f_{esc} (e.g., Bassett et al. 2021). Indeed, all these sources have an estimated $f_{\text{esc}} > 20\%$, thus complementing the GP sample at the high LyC f_{esc} end.

3 CLASSIFYING LYMAN CONTINUUM LEAKERS AND NON-LEAKERS WITH LY α PROFILES

Empirically, the Ly α line profile is the best predictor of LyC f_{esc} in galaxies in the local Universe (Izotov et al. 2018b, 2021a). We use line profiles to split the XLS- z 2 sample in subsets – “High Escape” (LyC $f_{\text{esc}} > 20\%$, “leakers”) and “Low Escape” (LyC $f_{\text{esc}} < 5\%$, “non-leakers”) based on a set of selection criteria that we design in this section. The motivation for $f_{\text{esc}} \approx 20\%$ is that this is approximately the average f_{esc} required for $M_{\text{UV}} \lesssim -15$ star-forming galaxies to produce reionization in typical calculations (e.g., Robertson et al. 2015; Naidu et al. 2020), whereas galaxies with $f_{\text{esc}} \approx 5\%$ are not relevant to the emissivity since even if all galaxies at e.g., $z \approx 7$ had $f_{\text{esc}} \approx 5\%$ they would be unable to produce reionization. We do not focus on galaxies with intermediate f_{esc} between these

two limits since we do not have sufficient sources ($N=4$) to construct stacks with meaningful SNR.

We emphasize that our goal here is to place galaxies in broad f_{esc} bins that are clean and complete. We do not argue that the f_{esc} distribution is bimodal, but as f_{esc} is non-linearly related to (parametrisations of) the shape of the Ly α profile, the expected f_{esc} of the two stacks are very different. In what follows we describe our newly developed selection criteria and motivate these based on theoretical and empirical grounds.

3.1 Ly α Peak Separation (v_{sep}) and Central Escape Fraction (f_{cen}) as tracers of LyC f_{esc} : Motivation

Due to resonant scattering, the Ly α line profile is expected to be a tracer of the kinematics, column density, and distribution of neutral HI within a galaxy (e.g., Neufeld 1990; Verhamme et al. 2006; Gronke et al. 2015b; Dijkstra et al. 2016; Kakiichi & Gronke 2021). If the ISM is porous with abundant low column density channels, Ly α photons escape with minimal scattering. Radiative transfer simulations show homogeneous, expanding media that cover HII regions with low column densities ($N_{\text{HI}} \lesssim 10^{18} \text{ cm}^{-2}$) give rise to narrow, tightly separated red and blue peaks. In clumpy, multi-phase systems with non-unity covering fractions (i.e., so-called riddled ionization-bounded HII regions), Ly α photons escape directly at the systemic velocity across clear lines of sight (Hansen & Oh 2006; Verhamme et al. 2015; Gronke et al. 2016; Gronke 2017). On the other hand, dense HI distributions force Ly α photons to scatter till they shift out of resonance. This struggle to escape manifests in a broad profile, little flux at the systemic velocity, and widely separated blue and red peaks.

In the sample of $z \approx 0.3$ LyC leakers the Ly α red and blue peak separation (v_{sep}) has been identified as the most faithful tracer of f_{esc} (e.g., Verhamme et al. 2017; Izotov et al. 2016a,b, 2018a,b, 2021a). This trend is illustrated in the top row of Figure 1 where narrower v_{sep} accompanies higher LyC f_{esc} and quantified as follows (Izotov et al. 2018b) with v_{sep} in km s^{-1} :

$$f_{\text{esc}} = 3.23 \times 10^4 v_{\text{sep}}^{-2} - 1.05 \times 10^2 v_{\text{sep}}^{-1} + 0.095. \quad (1)$$

However, v_{sep} measurements rely on the detection of a clear red and blue peak – fainter blue peaks may be missed due to poor SNR. Further, the applicability of v_{sep} is ambiguous when multiple peaks or systemic emission are seen in the profile. As a result, v_{sep} is an inapplicable metric for a large fraction of $f_{\text{esc}} > 20\%$ leakers. We show this in Figure 2, where we compile v_{sep}^1 for all known LyC leakers with high resolution, ($R \gtrsim 4000$) Ly α measurements and robust systemic redshifts². All the $z \approx 2 - 4$ LyC leakers observed with high-resolution spectroscopy show complex profiles characterized by flux at line center in addition to red and blue peaks (bottom row, Figure 1). These sources include GS-30668/XLS-26 ($z = 2.2$, Naidu et al. 2017), the Sunburst Arc³ ($z = 2.4$, Rivera-Thorsen et al. 2019), Ion2 ($z = 3.2$, Vanzella et al. 2016), GS-15601 ($z = 3.3$, J.

¹ In computing v_{sep} for a source like the Sunburst Arc (Figure 1) we set aside the central emission and measure the difference between the closest red and blue peaks. If instead v_{sep} was defined as $\max(\text{flux}, v > 0) - \max(\text{flux}, v < 0)$ we would end up with $v_{\text{sep}} \approx 0$ (and an implied unphysical $f_{\text{esc}} \approx 100\%$) for all the $z \approx 2 - 4$ sources. This ambiguity is precisely the motivation for introducing f_{cen} .

² The sources J1333+6246, J1442-0209, J1503+3644 are excluded because inspection of their Ly α profiles showed their systemic redshifts to be untrustworthy, see also Orlitová et al. (2018).

³ We note that the Ly α line-profile of the Sunburst Arc corresponds to

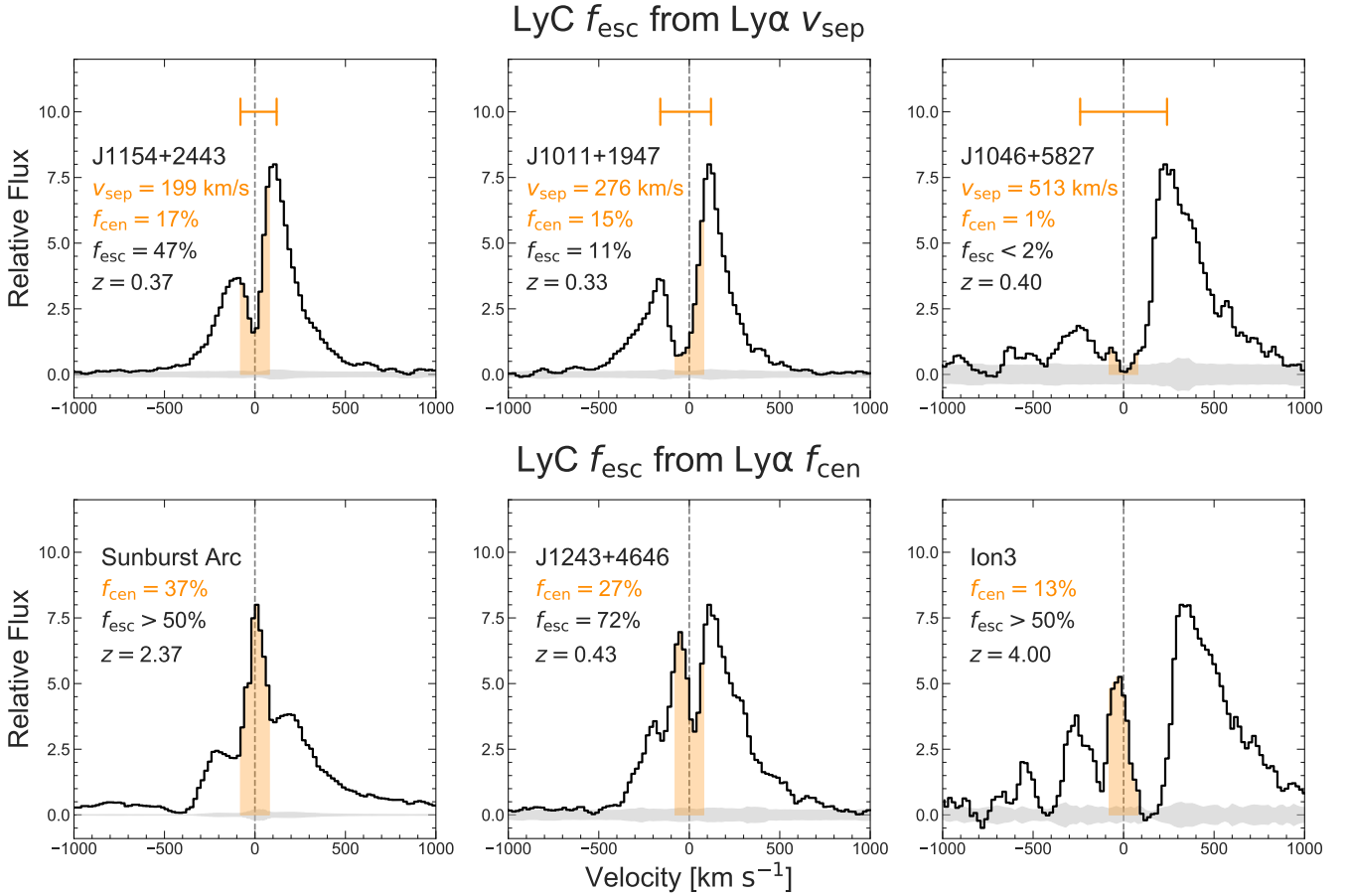


Figure 1. Ly α line profiles for a selection of galaxies with direct LyC f_{esc} measurements. Each panel lists the name of the source, the metric linked to LyC f_{esc} (v_{sep} , f_{cen}), and finally the directly measured LyC f_{esc} . Measured escape fractions are listed as lower limits for high- z sources due to the unknown IGM transmission along any particular line of sight. **Top:** The Ly α peak separation (v_{sep}), depicted as an orange capped line, is an effective predictor of f_{esc} for the $z \approx 0.3$ Green Peas – the larger the v_{sep} , the lower the f_{esc} (Eq. 1). **Bottom:** For most LyC leakers with $f_{\text{esc}} > 20\%$, v_{sep} is ill-defined and unable to predict f_{esc} . These sources exhibit direct Ly α escape at the systemic velocity along with narrow lines. To capture this, we introduce a new parameter, the central escape fraction (f_{cen}), which measures the fraction of the total Ly α flux emitted $\pm 100 \text{ km s}^{-1}$ from the systemic velocity (shaded orange region, Eq. 2).

Kerrut, private comm.), and Ion3 ($z = 4.0$, Vanzella et al. 2018). The three Green Peas with $f_{\text{esc}} > 20\%$ also show significant line centre emission (e.g., J1243+4646, Figure 1). Complex profiles that are not just a blue+red peak combination are a routine feature at high f_{esc} . For these sources v_{sep} is ill-defined (e.g., in the Sunburst Arc) and/or drastically underestimates f_{esc} (e.g., Ion3).

In these cases v_{sep} is a poor tracer of LyC f_{esc} because the observed Ly α profiles are likely a combination of two distinct modes of Ly α escape (e.g., Rivera-Thorsen et al. 2017): (i) scattering, resonant escape through relatively higher column density HI that results in red and blue peaks, (ii) direct escape through porous channels that manifests as central Ly α . Since v_{sep} is sensitive only to the scattering escape mode, we introduce a new parameter, the “central escape fraction” (f_{cen}), that traces the direct escape mode as well. We define f_{cen} as the fraction of Ly α emission within ± 100

km s^{-1} of the systemic velocity, i.e.,

$$\text{Central Escape Fraction } (f_{\text{cen}}) = \frac{\text{Ly}\alpha \text{ flux at } \pm 100 \text{ km s}^{-1}}{\text{Ly}\alpha \text{ flux at } \pm 1000 \text{ km s}^{-1}}, \quad (2)$$

where we found that the $\pm 1000 \text{ km s}^{-1}$ velocity window captures the total flux for all XLS-z2 sources. Theoretical profiles (e.g., Behrens et al. 2014; Verhamme et al. 2015; Dijkstra et al. 2016) suggest f_{cen} should track the relative abundance of low-opacity escape channels which can facilitate prolific LyC f_{esc} . Note that the denominator in Eq. 2 ensures that if only a small amount of flux is escaping at line centre, the f_{cen} (and the implied f_{esc}) is meagre. For instance, if central emission occurs on top of a double-peak profile, their relative weights are accounted for (contrast the $\approx 3\times$ higher f_{cen} of the Sunburst Arc with that of Ion3 in Figure 1). An advantage of f_{cen} is that one does not need to identify the exact locations of red or blue peaks, which can be ambiguous for multi-peaked profiles or when the fainter (typically blue) peak is below the detection threshold.

We caution that the specific choice of $\pm 100 \text{ km s}^{-1}$ is empirical and will be resolution dependent. However, the spectral resolution for the XLS-z2 observations and the sources used to calibrate the criteria are all very similar. We also caution that for low EW sources continuum subtraction errors can render f_{cen} uncertain, so this cri-

the profile of the LyC-leaking knot within the galaxy (see also Vanzella et al. 2021). It has a Ly α EW of 103 Å (Emil Rivera-Thorsen, private communication).

Literature LyC Leakers

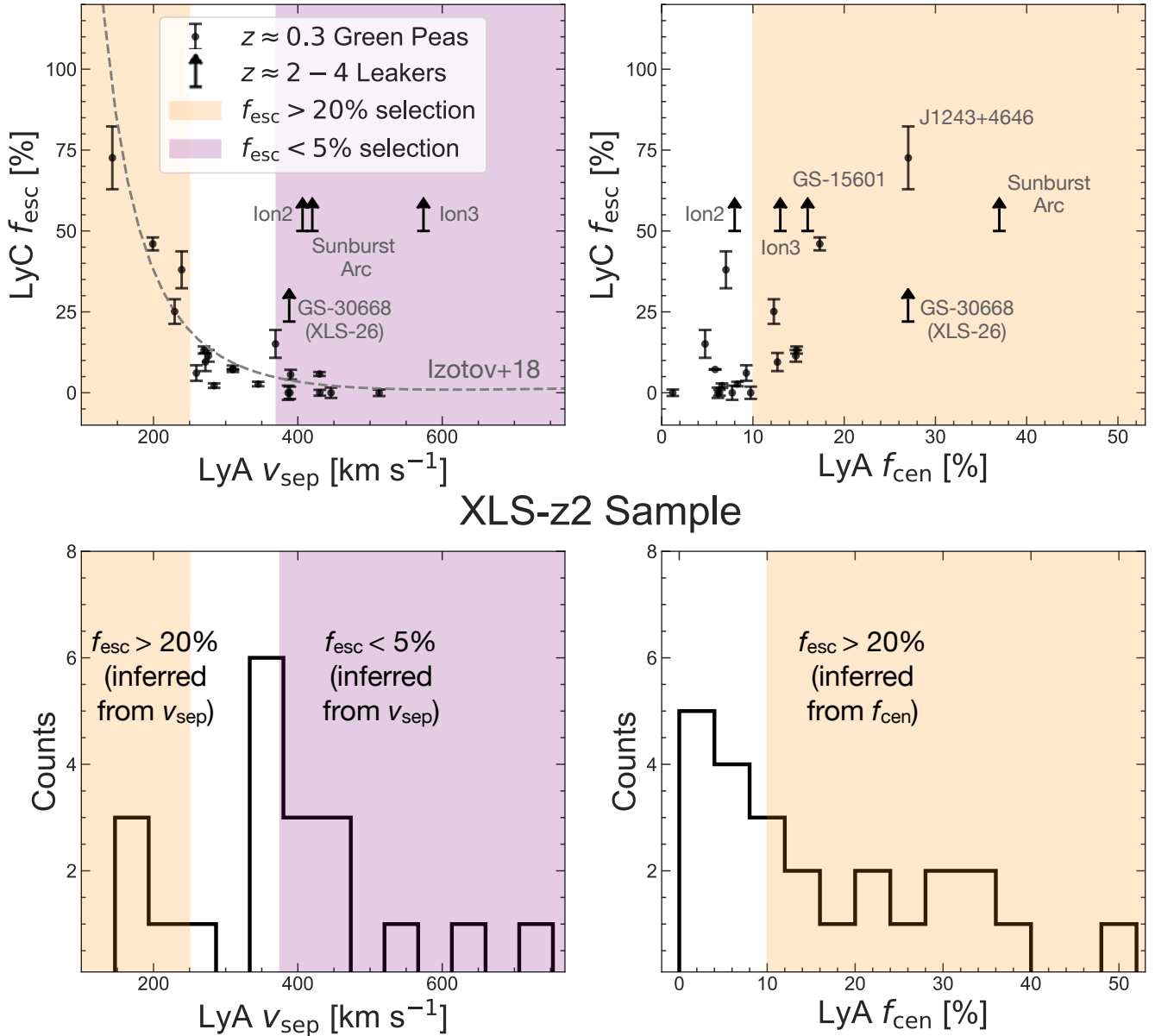


Figure 2. Discriminating between leakers and non-leakers using Ly α profiles. **Top Left:** LyC f_{esc} as a function of Ly α peak separation (v_{sep}) for the $z \approx 0.3$ Izotov et al. (2021a) Green Pea compilation and all the $z \approx 2 - 4$ leakers with high-resolution Ly α spectra. The fit from Izotov et al. (2018b) is shown with a dashed line. While successful at predicting LyC f_{esc} for the Green Peas, the Ly α v_{sep} fails to identify *all* the $z \approx 2 - 4$ sources as having $f_{\text{esc}} > 20\%$ because the systemic Ly α emission in these sources is not captured by v_{sep} (Figure 1 bottom). **Top Right:** To complement v_{sep} we introduce the Ly α central escape fraction (f_{cen}) that measures the fraction of the total Ly α flux emitted at $\pm 100 \text{ km s}^{-1}$ around the systemic redshift (§3.1). f_{cen} selects almost all the $z \approx 2 - 4$ sources missed by v_{sep} as having $f_{\text{esc}} > 20\%$. Combined, the f_{esc} and v_{sep} selection of $f_{\text{esc}} > 20\%$ sources (orange) is $\approx 90\%$ complete and $\approx 80\%$ pure, whereas the $f_{\text{esc}} < 5\%$ selection (purple) is 80% complete and 100% pure. **Bottom:** Distributions of v_{sep} and f_{cen} for the XLS-z2 sample, with selection criteria for the High Escape (purple) and Low Escape (orange) stacks informed by literature sources in the top row.

terion in specifically applicable to LAEs (Ly α EW $> 25\text{\AA}$). In the following section we provide an empirical verification of the utility of our definition of f_{cen} .

3.2 Designing and validating f_{cen} & v_{sep} selection criteria

Here we use known LyC leakers from the literature to design our joint f_{cen} & v_{sep} selection criteria in order to identify High Escape ($f_{\text{esc}} > 20\%$) and Low Escape ($f_{\text{esc}} < 5\%$) galaxies. We obtained the Ly α spectra for these sources from the Ly α Spectral Database (LASD, Runnholm et al. 2021) or via private communication. A

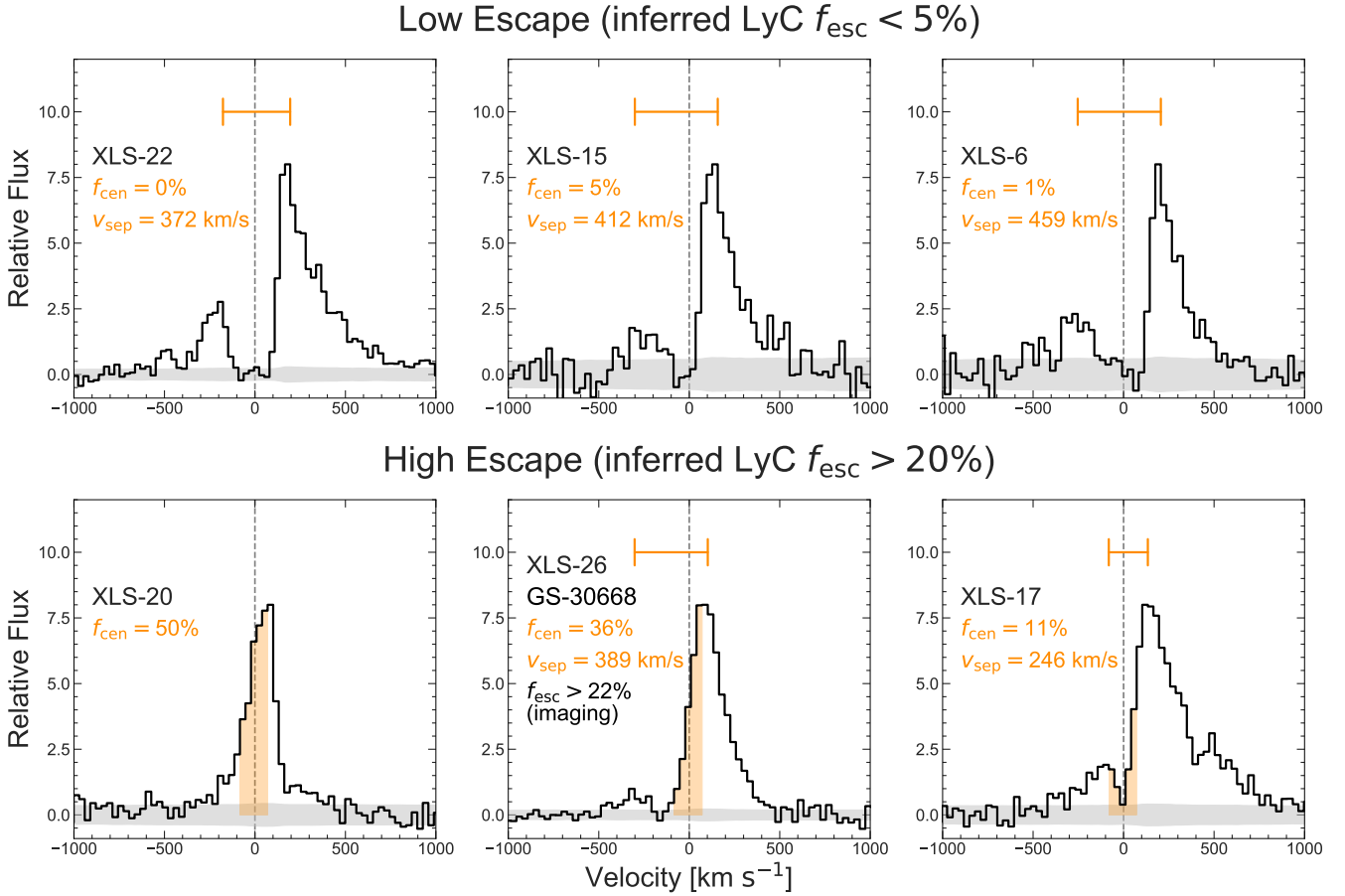


Figure 3. Sources from the XLS-z2 Low Escape (top) and High Escape (bottom) subsets. The LyC f_{esc} of these sources is inferred purely based on their Ly α profiles (v_{sep} and f_{cen}). Low Escape sources are characterized by widely separated peaks, broad lines, and little flux emitted around line centre. High Escape sources on the other hand have large f_{cen} and narrow lines. XLS-26 (bottom-centre) is a known LyC leaker (GS-30668) and acts as a useful cross-check on our selection. Notably, sources like XLS-26/GS-30668 would have been erroneously classed as non-leakers based on v_{sep} , but highly precise systemic redshifts reveal they have systemic Ly α emission and thus high f_{cen} .

selection criterion of $f_{\text{cen}} > 10\%$ reliably identifies the bulk (7 out of 9) of literature sources with $f_{\text{esc}} > 20\%$. This adopted f_{cen} cut not only selects sources with obvious Ly α at line centre like the Sunburst Arc, but also picks up sources with narrow lines and/or tight peak separations (e.g., J1154+2443, Figure 1).

When complemented with a $v_{\text{sep}} < 250 \text{ km s}^{-1}$ criterion, corresponding to $f_{\text{esc}} > 20\%$ (Eqn.1, top-left, Figure 2), Ion2 is the only source missed (i.e., the only “false negative”). As for false positives, three Green Peas with marginally lower than expected LyC $f_{\text{esc}} \approx 10 - 15\%$ are picked up – one of these, J1011+1947, has a Ly α $f_{\text{esc}} < 20\%$ and so is readily identified as a contaminant. To summarize, the following empirically motivated criterion:

$$\text{High Escape } (f_{\text{esc}} > 20\%) : (f_{\text{cen}} > 10\%) \text{ or } (v_{\text{sep}} < 250 \text{ km s}^{-1}) \quad (3)$$

when applied to literature LyC leakers produces a sample of $f_{\text{esc}} > 20\%$ sources that is $\approx 90\%$ complete and $\approx 80\%$ pure.

For selecting galaxies with $f_{\text{esc}} < 5\%$, from the top row of Figure 2 we observe that once the high f_{cen} sources are set aside, an entirely pure and $\approx 80\%$ complete sample can be selected as follows:

$$\text{Low Escape } (f_{\text{esc}} < 5\%) : (f_{\text{cen}} < 10\%) \text{ and } (v_{\text{sep}} > 375 \text{ km s}^{-1}).$$

(4)

It is remarkable that these simple empirical selections based purely on Ly α work so effectively given the intricate, multi-phase physics that drives f_{esc} (e.g., Paardekooper et al. 2015; Ma et al. 2016; Rosdahl et al. 2018). For instance, at first glance, v_{sep} and f_{cen} appear sensitive only to HI, and not to dust attenuation, which is the other key inhibitor of LyC f_{esc} (e.g., Chisholm et al. 2018). However, in §5 we argue that low column densities, and low attenuation are likely causally interlinked, and thus v_{sep} and f_{cen} implicitly select for low dust. In §5 we present several such independent spectroscopic points of evidence that inspire confidence in the robustness of the High and Low f_{esc} selections.

3.3 Applying f_{cen} and v_{sep} selections to XLS-z2

We have listed f_{cen} and v_{sep} measurements for our XLS-z2 sample in Table 1 along with Ly α escape fractions measured from the Ly α /H α ratio that is dust-corrected via Balmer decrements. Importantly for f_{cen} , systemic redshifts precise to $< 10 \text{ km s}^{-1}$ are measured thanks to the strong [OIII] doublet and its known intrinsic line ratio (see Matthee et al. 2021 for details). H α , H β , and in some cases nebular UV lines such as He II are further used as a cross-check on the

systemic redshift. The peak separation is measured by searching for maxima on either side of the systemic redshift. Faint blue peaks (and hence v_{sep}) are unreliable or undetected for a few high f_{cen} sources. This is not cause for concern – in §3.2 we showed all but one of the literature leakers with tight v_{sep} were picked up by the f_{cen} selection.

Applying Eqns. 3 & 4 we construct a sample of 13 High Escape ($f_{\text{esc}} > 20\%$) and 9 Low Escape ($f_{\text{esc}} < 5\%$) sources. 4 sources have intermediate f_{esc} and are not the subject of this analysis as their stacked spectrum has low SNR due to the small number of stacked sources. All sources in the parent sample are placed in one of these three bins. In Figure 3 we show a selection of sources from the Low Escape and High Escape samples. The Low Escape galaxies show little to no flux around line centre and broad, widely separated peaks. In the High Escape sample, XLS-20 is an even more extreme version of the Sunburst Arc, with $\approx 50\%$ of its Ly α emitted at line centre, while XLS-17 resembles the Green Peas with tight peak separation.

The four sources classified as High Escape based on v_{sep} also have high $f_{\text{cen}} > 10\%$. However, five f_{cen} -selected sources appear to have relatively wide v_{sep} of $\approx 400 \text{ km s}^{-1}$ (Table 1). XLS-26 (Figure 3) is the archetype of such sources. We emphasize again that the systemic redshifts for all our f_{cen} selected sources are highly secure – e.g., for XLS-26 the z_{sys} is confirmed with several lines across multiple X-SHOOTER arms (H α , H β , [O III] λ 4960, 5008Å, He II λ 1640, O III λ 1666Å). In these five cases we may be witnessing significant direct Ly α escape, so v_{sep} is under-estimating the LyC f_{esc} (see §3.2). Higher resolution spectra might reveal a clear central peak superimposed on blue and red peaks in these sources. Supporting this interpretation, we note that XLS-26 was identified as a likely LyC leaker with $f_{\text{esc}} = 60^{+40}_{-38}\%$ (“GS-30668” in Naidu et al. 2017) with direct LyC imaging from the Hubble Deep UV Survey (Oesch et al. 2018, which also incorporates earlier UV imaging from Rafelski et al. 2015). Since its f_{esc} was based on a probabilistic method (similar to the search that yielded Ion2, Vanzella et al. 2015), GS-30668 was presented as a likely candidate pending spectroscopic follow-up. Since then, MUSE-HUDF (Bacon et al. 2017; Nanayakkara et al. 2019) and X-SHOOTER follow-up (this work) have validated its highly ionizing nature – it is a He II, C III, and C IV emitter with [O III]/[O II] > 10 and extreme rest-frame EW([O III]+H β) $\approx 3400 \text{ \AA}$.

Our selection criteria imply $50 \pm 10\%$ (binomial error based on sample size) of the $L > 0.2L^*$ Ly α emitters at $z \approx 2$ are LyC leakers with $f_{\text{esc}} > 20\%$ (Table 1). As discussed in §2, the XLS- $z2$ sample is representative of $L > 0.2L^*$ LAEs. In the following section we contrast the average properties of $f_{\text{esc}} > 20\%$ and $f_{\text{esc}} < 5\%$ sources using their stacked rest-frame UV to optical spectra. It is important to note that we are contrasting High Escape LAEs and Low Escape LAEs – the differences between High Escape LAEs and non-LAEs (i.e., Ly α EWs $< 25 \text{ \AA}$) are likely even more pronounced than what we describe here.

4 SPECTRAL STACKS

To bring out faint spectral features we construct *median*-stacked X-SHOOTER spectra of the High and Low Escape subsamples over the $\lambda_{\text{rest}} = 1000 - 8000 \text{ \AA}$ range. The stacking methodology follows Matthee et al. (2021) whose approach we summarise here. Individual 2D spectra are shifted to the rest-frame and centered on the spatial peak of the Ly α line and the flux densities are converted to luminosity densities before the spectra are continuum normal-

ized and median-combined.⁴ An error spectrum is obtained using bootstrap-resampling. The 1D spectrum is then optimally-extracted assuming a gaussian profile. The full width half maximum (FWHM) of the gaussian profile is wavelength-dependent as determined by fits to the spatial extent of the UV continuum and rest-frame optical nebular lines. Key spectral windows of the resulting stacked spectra are presented side by side in Figure 4 with each row highlighting specific features.

An array of quantities measured from the stacks are summarized in Table 2. The emission-line luminosities, EWs, and line-ratios are derived following Matthee et al. (2021). Due to the complex shape of the Ly α line, its line-luminosity is measured by simply integrating the flux within $\pm 1000 \text{ km s}^{-1}$ from the systemic velocity, while the continuum level is estimated over the 1270-1300 Å interval in order to avoid interstellar absorption features. The luminosities of other faint UV lines ($\lambda < 3000 \text{ \AA}$) are measured by fitting single gaussian profiles where the FWHM can vary within 50-250 km s^{-1} and the continuum level is estimated using a rolling-median of the flux around the specific emission-line. For doublets, the widths and centroids are fixed to each other. For the rest-frame optical lines where the signal to noise is typically significantly higher, we notice that some lines show complex kinematics, such as a broad component (see Matthee et al. 2021 for examples in individual sources). Therefore we measure their line-luminosities non-parametrically using a curve-of-growth approach by integrating the flux in increasing windows with width ± 60 to $\pm 400 \text{ km s}^{-1}$ (or until convergence within the uncertainties). Uncertainties on line-luminosities, EWs and luminosity-ratios are obtained by redoing the measurements on data that is perturbed with the propagated noise level 1000 times. For non-detections of UV lines in the Low Escape stack upper limits were estimated by assuming the FWHM of the [O III] $_{5008}$ line of 150 km s^{-1} . These widths are validated in the UV lines that are detected. Due to their low detection S/N, absorption line EWs are measured non-parametrically by integrating the flux in a window between $-500 < \Delta v < +100 \text{ km s}^{-1}$ from the systemic redshift. This window is determined based on the typical velocity profile of absorption lines in deeper stacks of LAEs at $z \approx 2$ (Trainor et al. 2015; Matthee et al. 2021).

Stellar masses and rest-frame UV luminosities are obtained from spectral energy distribution (SED) fitting using the MAGPHYS code (da Cunha et al. 2008) applied to aperture-corrected photometry from Santos et al. (2020) spanning $\approx 0.3 - 5 \mu\text{m}$ in the well-studied COSMOS field. Nebular attenuation, $E(B-V)$, is estimated from the Balmer decrement based on H α /H β following Reddy et al. (2020). For further details we refer readers to Matthee et al. (2021).

5 RESULTS: THE CONDITIONS FOR LYMAN CONTINUUM ESCAPE

In this section we explore the physical differences between the High Escape and Low Escape stacks. First, we point out similarities: within errors, the stellar mass (M_{\star}), UV luminosity (M_{1500}), and UV slope (β_{UV}) show no significant difference (Table 2). This implies that for LAEs the Ly α line-profile and the inferred f_{esc} do not strongly depend on these properties. Now, based on the differences

⁴ We have also created stacked spectra centred on the UV continuum emission but find only small changes within the uncertainties of the measurements listed in Table 2. This is because typical spatial offsets between Ly α and the UV continuum are small and our spectral extraction window accounts for variations in the shape of the (stacked) UV continuum light distribution.

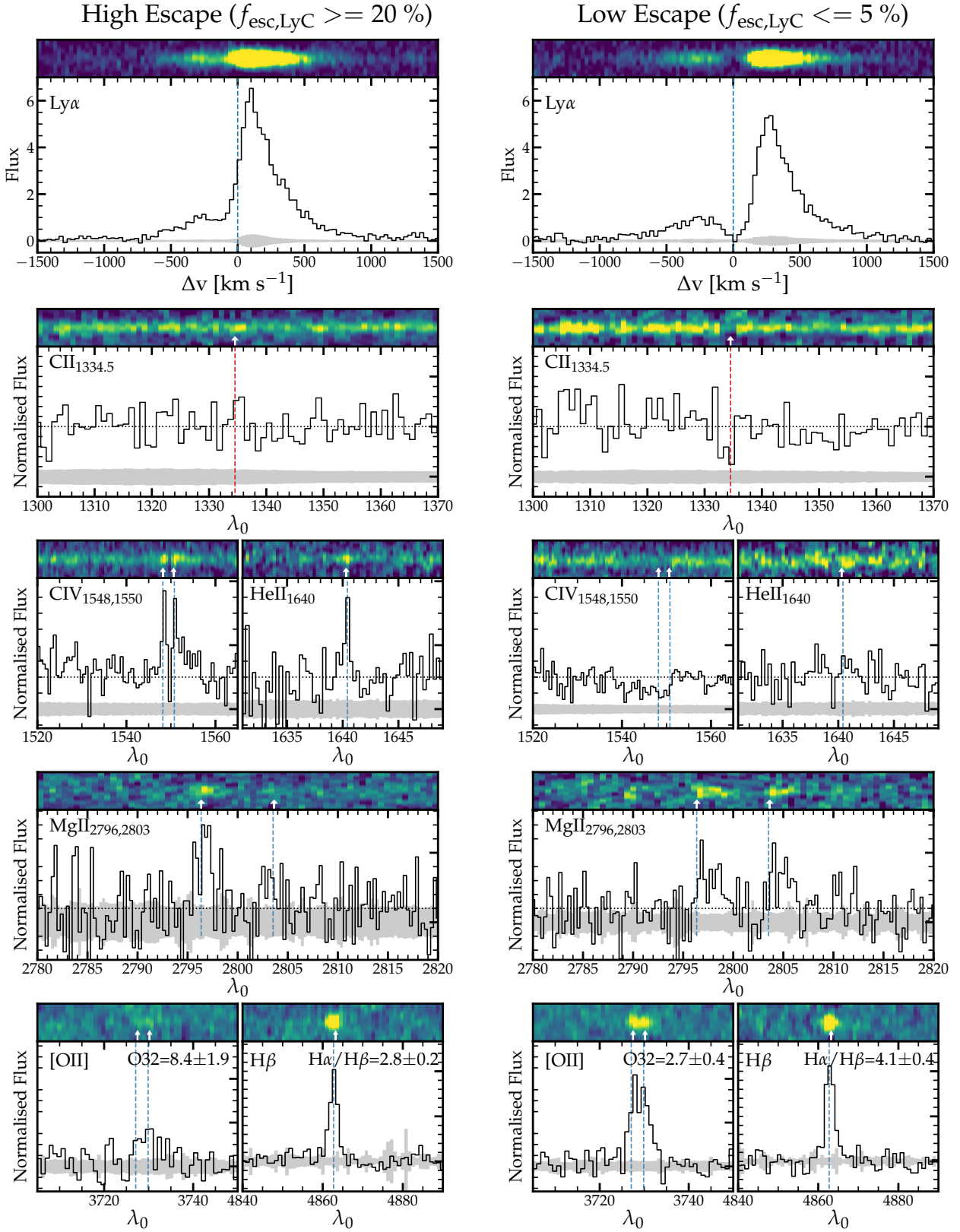


Figure 4. Median-stacked X-SHOOTER spectra for the High Escape (left) and Low Escape (right) subsets that are selected purely on Ly α line profiles (top row). Each panel is centred on a spectral feature labeled in the top-left corner. Panels are arranged in order of increasing wavelength (top to bottom). All features are nebular emission, except for CII in the second row, which is an interstellar absorption line. Gray shaded regions mark the 1σ noise level. The locations of emission-lines are marked with vertical blue dashed lines, while red lines mark absorption features. The black horizontal dotted line shows the normalisation level for the second to fourth row. For the fifth (bottom) row, the flux levels are normalised to the [OIII] (left) and H β (right) flux, respectively.

Table 2. Summary of measured properties for the High Escape and Low Escape stacks. We report medians and bootstrapped errors on medians (16th and 84th percentile). Upper limits are 99th percentile values from bootstrapping. EWs are in the rest-frame. All emission-line ratios are dust-corrected.

Basic Properties	High Escape ($f_{\text{esc}} > 20\%$)	Low Escape ($f_{\text{esc}} < 5\%$)
$\log_{10}(M_{\star}/M_{\odot})$	9.2 ± 0.2	9.4 ± 0.2
M_{1500}	-19.7 ± 0.3	-20.2 ± 0.3
β	-2.10 ± 0.21	-1.95 ± 0.16
Production		
$\text{EW}_{\text{HeII}1640}/\text{\AA}$	$1.9^{+0.8}_{-0.5}$	< 0.9
$\text{EW}_{\text{OIII}1661+1666}/\text{\AA}$	$2.2^{+0.3}_{-0.7}$	1.6 ± 0.5
$\text{EW}_{\text{CIII}1907+1909}/\text{\AA}$	$6.8^{+3.3}_{-2.1}$	$6.4^{+1.9}_{-1.8}$
$\text{EW}_{[\text{OIII}]4960+5008}/\text{\AA}$	820 ± 260	670 ± 160
$\text{EW}_{\text{H}\alpha}/\text{\AA}$	720 ± 200	430 ± 110
$\log_{10}(\xi_{\text{ion}}/\text{Hz erg}^{-1})$	$25.57^{+0.03}_{-0.03}$ ($f_{\text{esc}}=0.0$)	$25.55^{+0.06}_{-0.07}$
	$25.87^{+0.03}_{-0.03}$ ($f_{\text{esc}}=0.5$)	
Escape		
$f_{\text{esc,Ly}\alpha} = \frac{L_{\text{Ly}\alpha}}{8.7L_{\text{H}\alpha,\text{int}}}$	$47^{+3}_{-8} \%$	$9^{+2}_{-2} \%$
$R_{\text{MgII}} = \frac{\text{MgII}2796}{\text{MgII}2803}$	-	$0.9^{+0.4}_{-0.3}$
$v_{\text{Ly}\alpha,\text{red}}/\text{km s}^{-1}$	$+106 \pm 3$	$+254 \pm 4$
$v_{\text{CIV}}/\text{km s}^{-1}$	$+60 \pm 20$	-
$v_{\text{MgII}}/\text{km s}^{-1}$	$+30 \pm 10$	$+130 \pm 10$
Production & Escape		
$\text{EW}_{\text{Ly}\alpha}/\text{\AA}$	111 ± 6	61 ± 3
$\text{EW}_{\text{CIV}1548+1550}/\text{\AA}$	2.0 ± 0.4	< 1.4
$\text{EW}_{\text{MgII}2796}/\text{\AA}$	$6.7^{+2.5}_{-2.0}$	5.7 ± 1.8
$\text{EW}_{\text{MgII}2803}/\text{\AA}$	< 3.4	$6.1^{+1.7}_{-1.5}$
ISM conditions		
$E(B - V)$	$0.00^{+0.07}_{-0.00}$	$0.34^{+0.10}_{-0.09}$
$\text{O32} = \frac{[\text{OIII}]5008}{[\text{OII}]3727,3729}$	$8.4^{+2.2}_{-1.6}$	$2.7^{+0.4}_{-0.3}$
$\text{O3Hb} = \frac{[\text{OIII}]5008}{\text{H}\beta}$	$4.3^{+0.6}_{-0.5}$	$6.0^{+0.5}_{-0.5}$
$\text{Ne3O2} = \frac{[\text{NeIII}]3870}{[\text{OII}]3727,3729}$	$0.7^{+0.3}_{-0.2}$	$0.3^{+0.1}_{-0.1}$
$\text{R23} = \frac{[\text{OIII}]4960,5008 + [\text{OII}]3727,3729}{\text{H}\beta}$	$6.3^{+0.9}_{-0.7}$	$10.3^{+1.2}_{-1.0}$
$\text{N2Ha} = \frac{[\text{NII}]6584}{\text{H}\alpha}$	< 0.08	< 0.03
$12+\log(\text{O}/\text{H})$	8.2 ± 0.3	8.1 ± 0.1

between the stacks we aim to understand the differing physical conditions between leakers and non-leakers. In what follows we split the results in groups of features pertaining to the production of ionizing photons, the ISM they are radiated into, and finally the ease with which they are able to escape their parent galaxy.

5.1 Production: High Escape accompanies extreme ξ_{ion} and hard ionizing spectra revealed by He II and C IV emission

Here we focus on the ionizing photons produced by the stellar populations powering our stacks *before* they make it into the ISM. Based on rest-frame optical and UV line ratios (e.g., $[\text{OIII}]/\text{H}\beta$, CIV/CIII , $\text{CIV}/\text{HeII}\lambda 1640$), we find that both stacks have emission-lines that are photoionised by young stars and not by AGN activity (e.g., Kauffmann et al. 2003; Juneau et al. 2014; Feltre et al. 2016).

For stellar populations, a canonical quantity in the context of ionizing photon production is ξ_{ion} , the Hydrogen ionizing photon production efficiency, which is cast in terms of the rate of Hy-

drogen ionizing photons ($N(\text{H}^0)$) produced per unit (intrinsic) UV luminosity (L_{1500}). We derive this quantity in terms of the dust-corrected H α and UV luminosities using the Balmer decrement (e.g., Bouwens et al. 2016; Matthee et al. 2017; Shivaeei et al. 2018):

$$\xi_{\text{ion}} = \frac{N(\text{H}^0)}{L_{1500}} = \frac{L(\text{H}\alpha)}{(1 - f_{\text{esc}}) L_{1500}} \frac{1}{7.4 \times 10^{11} \text{s}^{-1} / \text{erg s}^{-1} \text{Hz}^{-1}}. \quad (5)$$

We measure a $\log(\xi_{\text{ion}}/\text{Hz erg}^{-1}) = 25.55^{+0.06}_{-0.06}$ in the low f_{esc} stack (assuming LyC $f_{\text{esc}}=0\%$), and $\log(\xi_{\text{ion}}/\text{Hz erg}^{-1}) = 25.87^{+0.03}_{-0.03}$ in the high f_{esc} stack (assuming LyC $f_{\text{esc}}=50\%$, see §6; for $f_{\text{esc}}=0\%$ we find $25.57^{+0.03}_{-0.03}$). For the low escape stack ($E(B - V) \approx 0.3$) we caution the dust correction is uncertain on a 0.3 dex level due to the unknown stellar-to-nebular attenuation and differences across dust curves (e.g., Shivaeei et al. 2018), while this is not a concern for the leakers which have $E(B - V) \approx 0$.

The High Escape stack also appears to have a harder ionizing spectrum. Prominent narrow C IV $\lambda 1548$, $\lambda 1550$ and He II $\lambda 1640$ emission is detected at SNR of 4.7 and 3.5, respectively, while there is no sign of these lines among the non-leakers (third row, Figure 4; Figure 5). The He II EW is at least a factor 2 \times higher among the leakers. Strong He II emission is clear evidence for the production of photons with > 54.4 eV (e.g., Shirazi & Brinchmann 2012; Berg et al. 2018; Nanayakkara et al. 2019; Saxena et al. 2020). That these features are seen in the *median* stack implies such hard ionizing photons occur routinely among LyC leakers. To put the shape of the SED in perspective, the effective ionizing spectral slope, α^5 , of the BPASS burst SEDs that produce the observed H α EWs accounting for an $f_{\text{esc}} \approx 50\%$ (e.g., Stanway et al. 2020) is *shallower* than the slopes typically adopted for AGN ($\alpha \approx -1.3$ vs. $\alpha \approx -1.7$, e.g., Becker & Bolton 2013). However, note that α only effectively captures the total number of Hydrogen ionizing photons, and typical quasar SEDs (e.g., Lusso et al. 2015) still produce a higher number of Helium ionizing photons at fixed M_{UV} .

5.2 Production & Escape: hints from C IV

The *simultaneous* detection of nebular C IV emission alongside He II (§5.1) in leakers is evidence that $< 260\text{\AA}$ photons are not only being produced but might also be escaping the ISM (Berg et al. 2019). The resonant C IV line, analogous to Ly α , is sensitive to the column density of high-ionization gas. This imprint of the column density on C IV may be seen among the MUSE He II emitters (Nanayakkara et al. 2019), only a small fraction of which show C IV in emission while the majority show interstellar absorption and/or stellar wind features (e.g. Plat et al. 2019). This is despite C IV requiring a lower ionization energy than He II (47.9 eV versus 54.4 eV, Draine 2011), and despite the presence of sufficient Carbon in the ISM (C III] is detected). In these sources C IV may be suffering significant absorption and scattering – $< 260\text{\AA}$ photons are being produced but likely fail to escape the ISM. However, tellingly, one of the highest EW C IV emitters in the MUSE He II emitter sample is the $z \approx 2.2$ LyC leaker XLS-26/GS-30668/MUSE-1273 that we discussed earlier in the context of central Ly α escape in §3 (Figure 3). A similar scenario as in XLS-26 occurs in the High Escape

⁵ α is defined such that integrating $f_{\nu} \propto \nu^{\alpha}$ for $< 912\text{\AA}$ matches the total number of $< 912\text{\AA}$ ionizing photons computed by integrating the model SED (e.g., Becker & Bolton 2013).

stack, where nebular C_{IV} emission appears alongside He II. The C_{IV} doublet ratio indicates some absorption in the ISM – the blue line is weaker than the expectation for pure emission based on the relative oscillator strengths. The line is observed relatively close to the systemic velocity ($+60 \pm 20 \text{ km s}^{-1}$) implying little scattering.

5.3 ISM: large differences in attenuation at comparable metallicity

Once the ionizing photons leave their sites of production their fate is decided by the contents, density, and geometry of the ISM they encounter. The gas-phase metallicities of our stacks are similar within errors : $12 + \log \text{O}/\text{H}$ of 8.2 ± 0.3 versus 8.1 ± 0.1 . We measure this with a composite of strong-line indicators – R_{23} , $[\text{O III}]/[\text{O II}]$, $[\text{O III}]/\text{H}\beta$, $[\text{Ne III}]/[\text{O II}]$ – calibrated on high-redshift analogues in the local Universe (Bian et al. 2018). We caution that for the High Escape group, R_{23} and $[\text{O III}]/\text{H}\beta$ yield much (0.5 dex) higher metallicity ($12 + \log \text{O}/\text{H} \approx 8.4$) compared to the other two indicators. This is potentially because these two indicators are bi-valued and lose sensitivity around sub-solar ($\lesssim 20\%$) metallicity ranges (e.g., Pérez-Montero et al. 2021). For the Low Escape group the indicators are in better agreement.

Dust is expected to be a key inhibitor of LyC f_{esc} (e.g., Inoue et al. 2001; Chisholm et al. 2018). The Low Escape stack has a Balmer decrement of 4.1 ± 0.4 indicating widespread dust attenuation among the non-leakers. On the other hand, in the High Escape stack the Balmer decrement is indistinguishable from the expected value for case B recombination (2.8 ± 0.2) in gas with electron temperatures 10-15 kK indicating essentially dust-free pathways for LyC escape, at least outside the HII regions in which the ionizing photons were produced, as the Balmer decrement is insensitive to the attenuation law at $\lambda < 912 \text{ \AA}$ (Israel & Kennicutt 1980; Reines et al. 2008). Understanding the dust law at $\lambda < 912 \text{ \AA}$ is important, now that we know LyC leakers produce copious photons far below the Lyman edge (see §6.3). We emphasize that there is no explicit information on the attenuation in our stacking criteria ($\text{Ly}\alpha$ v_{sep} and f_{cen}), so the Balmer decrements are a clear, independent validation that High Escape is associated with low (negligible) attenuation.

5.4 ISM: super star cluster-like extreme ionization state in leakers revealed by elevated $[\text{O III}]/[\text{O II}] > 8$

The ionization parameter (U) – the ratio of the number density of ionizing photons to the number density of Hydrogen gas – is typically used to characterize the state of photoionized gas in galaxies (e.g., Sanders et al. 2015). In our stacks, Ne3O2 ($[\text{Ne III}]_{3870}/[\text{O II}]_{3727,3729}$) and $[\text{O III}]/[\text{O II}]$ are tracers of the ionization parameter (e.g., Levesque & Richardson 2014; Strom et al. 2017; Maiolino & Mannucci 2019).

One of the most striking differences between the two stacks is the $[\text{O III}]/[\text{O II}]$ ratio (bottom row, Figure 4; Figure 5) – $8.4^{+2.2}_{-1.6}$ in the High Escape stack versus $2.7^{+0.4}_{-0.3}$. This translates to a $\log U = -2.3$ (-2.6) for the High (Low) Escape stacks adopting the Strom et al. (2018) calibration appropriate for $z \approx 2$. Likewise, the Ne3O2 ratio also implies $\log U = -2.3$ (-2.5) for the High (low) Escape subsets. The $\log U = -2.3$ of our High Escape stack is among the highest observed for a population, close to the theoretical/observational threshold in the $z \approx 0$ Universe (Dopita et al. 2006; Kewley et al. 2019; Pérez-Montero et al. 2021), comparable to confirmed LyC leakers at $z \approx 0.3$ (Guseva et al. 2020), and ≈ 0.5

dex higher than continuum-selected samples at $z \approx 2-3$ (e.g., Strom et al. 2018; Topping et al. 2020).

As a population, the elevated ionization state of the High Escape stack is comparable to the largest star clusters (Kewley et al. 2019), the so-called “super star clusters”, which routinely show $\log U \approx -2.3$ (e.g., Indebetouw et al. 2009; Leitherer et al. 2018; Micheva et al. 2019). These compact (order 10 pc), $\approx 10^6 M_{\star}$ complexes of young (order 10 Myrs), massive stars may be the key sites for LyC production and escape (e.g., Vanzella et al. 2019, 2021; Östlin et al. 2021).

5.5 Escape: Optically thin gas traced by $\text{Ly}\alpha$ f_{esc}

The stacked $\text{Ly}\alpha$ profiles (top panel, Figure 4), by design, show the expected signatures – the High Escape sources have an $f_{\text{cen}} \approx 0.27$ and a red-peak that is $\approx 100 \text{ km s}^{-1}$ from line centre (see Table 2), indicating low column densities, ionized channels, and modest scattering (§3.1). The Low Escape stack on the other hand has little flux emitted at line center ($f_{\text{cen}} \approx 0.03$), and its red peak is observed at $\approx 250 \text{ km s}^{-1}$ from the systemic velocity, indicating considerably more scattering than the High Escape stack. The peak separation (v_{sep}) is not well-defined in either case because the location of the blue peak is ambiguous.

Now we dwell on other aspects of the $\text{Ly}\alpha$ line that did not go into our selection of the subsets. The $\text{Ly}\alpha$ f_{esc} , which is computed by comparing the observed $\text{Ly}\alpha$ luminosity with the dust-corrected $\text{H}\alpha$ luminosity, provides a useful upper bound on the LyC f_{esc} . This is clear empirically (e.g., Gazagnes et al. 2020; Izotov et al. 2021a), through radiative transfer simulations (e.g., Dijkstra et al. 2016; Kimm et al. 2019), and makes intuitive sense: $\text{Ly}\alpha$ photons can scatter and escape through somewhat higher column density gas, while LyC cannot. The $\text{Ly}\alpha$ f_{esc} for our High Escape stack is $47^{+3}_{-8}\%$ whereas for the Low Escape stack we find $9^{+2}_{-2}\%$ (Table 2). This is a strong cross-check on the robustness of our stacks – the Low Escape stack is ruled out from having a LyC $f_{\text{esc}} > 10\%$ while the High Escape stack may have an f_{esc} as high as $\approx 50\%$.

We find that the leakers have a $\text{Ly}\alpha$ EW $\approx 2\times$ higher than the non-leakers. However, note that the $61 \pm 3 \text{ \AA}$ EW in the Low Escape stack is also substantial and demonstrates that $\text{Ly}\alpha$ EW by itself is an impure predictor of f_{esc} . This is discussed further in §7.3.

5.6 Escape: Optically thin gas traced by Mg II

The Mg II doublet has a similar ionization potential to that of H⁰ (15 eV), resonantly scatters like $\text{Ly}\alpha$, and will be within the grasp of *JWST* at $z > 6$ when $\text{Ly}\alpha$ is damped by the neutral IGM (e.g., Henry et al. 2018; Feltre et al. 2018; Chisholm et al. 2020). Our stacks show that the Mg II doublet can be used as an indirect tracer of HI column density (fourth row, Figure 4; Figure 5). The Low Escape stack shows redshifted ($+130 \pm 10 \text{ km s}^{-1}$) Mg II emission while in the High Escape stack Mg II emission arises much closer to the line-centre ($+30 \pm 10 \text{ km s}^{-1}$). Further, the line ratio of the Mg II doublet ($R_{\text{MgII}2796/2803}$) is in agreement with recent results from Chisholm et al. (2020) who argued the column density of neutral Hydrogen is proportional to $R_{\text{MgII}2796/2803}$ in the optically thin regime. Indeed, in the Low Escape stack $R_{\text{MgII}2796/2803} \approx 1$ whereas in the High Escape stack the redder line in the doublet is undetected, implying a higher line ratio.

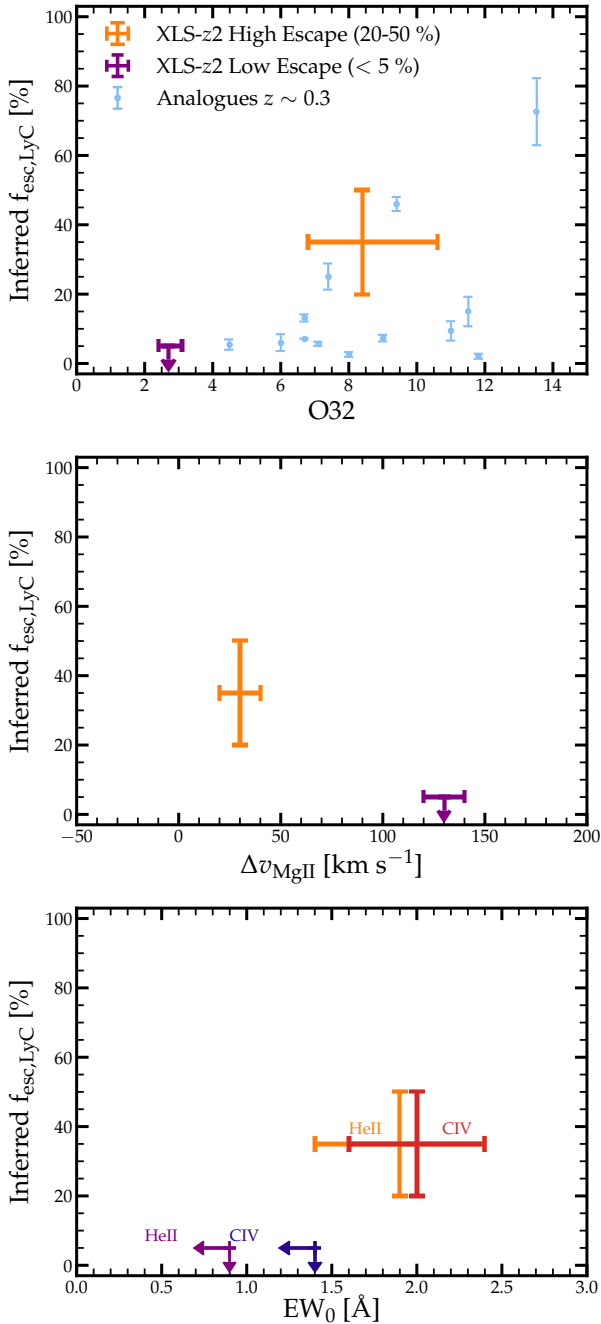


Figure 5. Spectroscopic tracers of LyC f_{esc} identified in this work that will be easily accessible with *JWST* – the [OIII]/[OII] ratio (top), the MgII velocity offset (middle), and the rest-frame EWs of high ionization lines (HeII, CIV; bottom). The High Escape stack is represented in shades of orange, while the Low Escape stack is shown in shades of purple. We depict the full conservative range (LyC $f_{\text{esc}} \approx 20 - 50\%$) for the High Escape stack (see Table 3). For comparison, individual [OIII]/[OII] measurements for the $z \approx 0.3$ Izotov et al. (2021a) Green Peas are shown in the top panel – note that most of the GPs were selected for follow-up because they have high [OIII]/[OII]. MgII offsets and UV emission line EWs are not yet available for these sources.

5.7 Escape: Low covering fraction in leakers revealed by CII absorption

The covering fraction of neutral gas is a measure of how riddled with ionized channels (“holes”) the ISM is. Covering fractions, as inferred from ISM absorption lines (both metal lines as well as Hydrogen lines), are expected to trace LyC f_{esc} , with a higher covering fraction corresponding to lower f_{esc} (e.g., Reddy et al. 2016; Gazagnes et al. 2018, 2020; Mauerhofer et al. 2021). Our sensitivity for detecting HI absorption lines blue-wards of Ly α is low. In stacks of LAEs the strongest low-ionisation interstellar absorption lines are typically SiII and CII (Trainor et al. 2015). We clearly detect CII absorption in the Low Escape stack (with an EW = -1.6 ± 0.2 Å), and no such absorption feature in the High Escape stack (with a 2σ limiting EW > -0.6 Å; Figure 4). No significant SiII absorption is detected in any of the stacks (2σ limiting EWs > -0.8 Å and > -0.6 Å for the High and Low escape stack, respectively). The difference between SiII and CII is likely of instrumental origin as our sensitivity is a factor ≈ 1.4 better around CII than around SiII. The differences between the CII absorption strengths in the stacks is another line of evidence that a porous ISM conducive to high LyC f_{esc} occurs in the High Escape stack, whereas the Low Escape sources do not have such pathways.

6 RESULTS: THE ESCAPE FRACTION OF THE HIGH ESCAPE STACK

The High Escape stack was constructed purely based on Ly α profiles to have LyC $f_{\text{esc}} > 20\%$, and contains $50 \pm 10\%$ (binomial error from sample size) of the sample studied in this work (Table 1). Through multiple spectroscopic indicators (§5) we have verified this stack is indeed probing high f_{esc} . We now estimate what the f_{esc} of this sample is likely to be.

6.1 Constraints from the Ly α escape fraction

A strict upper bound on the LyC f_{esc} is due to the Ly α $f_{\text{esc}} = 47^{+3}_{-8}\%$, the 95th percentile of which is $\approx 55\%$. Both empirical (e.g., Gazagnes et al. 2020; Izotov et al. 2021a) and theoretical (e.g., Dijkstra et al. 2016; Kimm et al. 2019, 2021) work show that the Ly α $f_{\text{esc}} \geq \text{LyC } f_{\text{esc}}$. Ly α and LyC likely emanate from the same production sites powered by young stars, and the resonant scattering of Ly α gives it an added advantage when it comes to escaping the ISM. We deem this broad range (20 – 55%) our “conservative” estimate since it encompasses the entire realm of possibility for our stack.

We make a finer estimate of the LyC f_{esc} by observing that in the Izotov et al. (2021a) Green Pea compilation, the higher the LyC f_{esc} , the closer it is to the Ly α f_{esc} . This trend is supported by the Kimm et al. (2019) simulations in which turbulent clouds with LyC $f_{\text{esc}} > 20\%$ have $f_{\text{esc, LyC}}/f_{\text{esc, Ly}\alpha} \approx 1$. Indeed, for the seven Izotov et al. (2021a) GPs that satisfy our High Escape selection criteria (Eq. 3) we calculate a bootstrapped ratio of $f_{\text{esc, LyC}}/f_{\text{esc, Ly}\alpha} = 0.82^{+0.16}_{-0.15}$. This ratio produces an LyC f_{esc} of $38^{+9}_{-8}\%$ for the High Escape stack.

The Ly α f_{esc} we use for this estimate is calculated via the same assumptions as the Izotov et al. (2021a) compilation (e.g., the intrinsic Ly α /H α ratio is matched). Further, the spatial scale probed by the *HST*/COS apertures in the Green Pea studies ($\approx 1.3''$ radius, 7 – 10 kpc at $z \approx 0.3$) is comparable to our $1''$ slits at $z \approx 2$. This ensures consistent Ly α f_{esc} comparison, given the spatially extended nature of Ly α emission (e.g., Hayes et al. 2013; Wisotzki

et al. 2016). We also clarify that this argument does not imply that high Ly α f_{esc} selects for high LyC f_{esc} – the point is that at high LyC f_{esc} , $f_{\text{esc,LyC}}/f_{\text{esc,Ly}\alpha} \approx 1$ which is supported by these $f_{\text{esc}} > 20\%$ systems being in “density bounded nebulae” that are transparent to LyC along all lines of sight (e.g., Ramambason et al. 2020), thus diminishing the resonance advantage of Ly α over LyC.

6.2 Constraints from the Ly α red peak and HI covering fraction

The HI covering fraction (f_{cov}) – the fraction of high column density ($N(\text{HI}) > 10^{16} \text{cm}^{-2}$) channels – has been used as a successful predictor of the LyC escape fraction (e.g., Reddy et al. 2016, 2021; Chisholm et al. 2018) as follows:

$$f_{\text{esc}} = (1 - f_{\text{cov}}) \times 10^{-0.4A(\lambda=912\text{\AA})}. \quad (6)$$

In our case the attenuation is negligible, so we set $A(\lambda = 912\text{\AA}) = 0$. To estimate f_{cov} we exploit the 3σ correlation with the Ly α red peak velocity ($V_{\text{red}} - V_{\text{trough}}$) reported in Gazagnes et al. (2020). Note that the red peak velocity is measured with respect to the Ly α “trough”, i.e., the minima between the red and blue peak in typical double-peaked profiles. The Gazagnes et al. (2020) sample, mostly drawn from the Izotov et al. (2021a) compilation, has very similar Ly α resolution to the sample studied here, so differential effects are limited. The significant, albeit noisy, relationship (S. Gazagnes, private comm.) is as follows:

$$f_{\text{cov}} = (0.29 \pm 0.10) \times (V_{\text{red}} - V_{\text{trough}}) / (100 \text{ km s}^{-1}) + 0.14 \pm 0.22. \quad (7)$$

We cannot apply this metric directly to the stack since there is no clear trough in the profile – instead, we apply it object by object to each individual source and compute the median f_{cov} . In the three cases where there is no trough in the profile we either set aside the source (XLS-24) or assume $V_{\text{red}} - V_{\text{trough}} = 0$ (XLS-20, XLS-28). The adopted values for all galaxies are shown along with their profiles in Appendix A. The median $V_{\text{red}} - V_{\text{trough}}$ for our sample is $147_{-28}^{+28} \text{ km s}^{-1}$ which translates to $1 - f_{\text{cov}} = 43_{-26}^{+26}\%$.

We have verified that for the seven GPs that satisfy the High Escape criteria computing $1 - f_{\text{cov}}$ in this manner results in a number slightly higher than their mean LyC f_{esc} (48% vs 35%) – this is due to significant dust attenuation in these sources, i.e., $A(\lambda = 912\text{\AA})$ is not zero. It is important to note that Eqn. 6 assumes an “ionization bounded nebula” – i.e., the ionization front is surrounded by an impermeable layer of high column density gas ($N_{\text{HI}} \gg 10^{18} \text{cm}^{-2}$) that is perforated by a smattering of low column density channels whose proportion is $\approx 1 - f_{\text{cov}}$. However, as we discuss in the following section, $f_{\text{esc}} > 20\%$ leakers likely deviate from this physical picture.

6.3 The difference between Lyman edge f_{esc} (850-912 Å) and total f_{esc} (0-912 Å)

The optical line ratios and covering fractions of prolific LyC leakers ($f_{\text{esc}} > 20\%$) imply they are best described as “density bounded nebulae” (Ramambason et al. 2020). That is, the ionization front is surrounded by low column density gas ($10^{16} - 10^{18} \text{cm}^{-2}$) punctuated by entirely transparent ($< 10^{16} \text{cm}^{-2}$) channels (see Fig. 16 of Gazagnes et al. 2020 for an excellent schematic). Modifying Eqn. 6 for this situation and assuming no dust attenuation we have:

$$f_{\text{esc,LyC}} = \underbrace{(1 - f_{\text{cov}}) \times 1}_{< 10^{16} \text{ cm}^{-2}} + \underbrace{f_{\text{cov}} \times f_{\text{cov,esc}}}_{10^{16} - 10^{18} \text{ cm}^{-2}}. \quad (8)$$

This equation expresses the view that there is a fraction ($1 - f_{\text{cov}}$) of entirely transparent channels with $f_{\text{esc,LyC}} = 100\%$ through which the ionizing continuum emerges as is. However, there is also a fraction of channels (f_{cov}) that is not entirely transparent ($10^{16} - 10^{18} \text{cm}^{-2}$) but is permeable to ionizing photons which have an effective escape fraction of $f_{\text{cov,esc}}$. It is in the context of $f_{\text{cov,esc}}$ that the $< 850\text{\AA}$ photons powering our High Escape stack become important.

All the LyC f_{esc} measurements we have discussed in this paper, devised our selections around, and used to empirically estimate the LyC f_{esc} in the previous sections were made at the Lyman edge ($\approx 850 - 912\text{\AA}$). However, photons below the Lyman edge ($< 850\text{\AA}$) are produced in copious amounts in the High Escape sources, as testified by the presence of strong optical line EWs (e.g., rest-frame $[\text{OIII}]_{4960,5008} + \text{H}\beta \approx 1100 \text{\AA}$), as well as $\text{He II } \lambda 1640$ and $\text{C IV } \lambda 1548, \lambda 1550$ emission. The $< 850\text{\AA}$ photons have much lower photoionization cross-sections compared to those at $> 850\text{\AA}$. Thus, there may be significant differences between the total escape fraction measured across the entire ionizing continuum (“total f_{esc} ”, $0 - 912\text{\AA}$) compared to the escape fraction measured only at the Lyman edge (“edge f_{esc} ”, $850 - 912\text{\AA}$) (e.g., Gnedin et al. 2008; Inoue 2010; Haardt & Madau 2012; McCandliss & O’Meara 2017; Kimm et al. 2019; Berg et al. 2019). Since $< 850\text{\AA}$ photons are an ubiquitous feature of LyC f_{esc} , occurring in our median stack, literature LyC f_{esc} estimates and the empirical scaling relations we used in this section may be systematically underestimating the total LyC f_{esc} . And it is the total f_{esc} that ultimately matters for reionization calculations.

For the High Escape stack, with an $f_{\text{cov}} \approx 60\%$ (§6.2), our estimates from the previous sections are roughly underestimated by $\gtrsim 10\%$ for covering column densities of $N(\text{HI}) < 10^{18} \text{cm}^{-2}$ expected in the density-bound scenario, i.e., a total $f_{\text{esc}} \gtrsim 50\%$ (Figure B.1). Independently, the Gnedin et al. (2008) hydrodynamical simulations provide an explicit scaling of $f_{\text{esc}}(0-912\text{\AA}) \approx 1.25 f_{\text{esc}}(912\text{\AA})$, which also results in an $f_{\text{esc}}(0-912\text{\AA}) \approx 50\%$ for our stack.

From the arguments in this section it might seem our Low Escape stack (edge LyC $f_{\text{esc}} < 5\%$, Ly α $f_{\text{esc}} < 10\%$) must also have a higher total f_{esc} . However, it displays significant CII absorption implying high column densities (i.e., it is likely ionization bounded as further suggested by its lower O32 ratio). The difference between edge and total f_{esc} applies only to the $f_{\text{cov}} \times f_{\text{cov,esc}}$ term in Eq. 8 when the covering gas is also transparent ($10^{16} - 10^{18} \text{cm}^{-2}$). Further, the Low Escape stack lacks the ionizing sources producing $< 850\text{\AA}$ photons (e.g., no He II and C IV emission). Due to the correlated nature of low column densities, low dust, and ionizing stellar populations, the difference between edge and total f_{esc} must be thought of as a “high edge f_{esc} implies higher total f_{esc} ” effect. We also note that a contribution from free-bound emission of H which peaks shortward of the LyC limit may mean that reported edge escape fractions are conversely somewhat overestimated (see Inoue 2010). Here we only seek to argue that some difference likely exists between the edge and total f_{esc} , and have provided an approximate estimate – more sophisticated modeling that accounts for e.g., realistic ionization and density structure is warranted.

Table 3. Summary of f_{esc} constraints for the High Escape stack from a variety of arguments. Assuming our sample is representative, half the $> 0.2L^*$ LAEs at $z \approx 2$ have this median f_{esc} .

Conservative range by selection and $f_{\text{esc,LyC}} < f_{\text{esc,Ly}\alpha}$ (§6.1)	20 – 55%
Empirical $f_{\text{esc,LyC}}/f_{\text{esc,Ly}\alpha}$ ratio for $f_{\text{esc,LyC}} > 20\%$ (§6.1)	$38 \pm 9\%$
$\text{Ly}\alpha$ red peak and covering fraction correlation (§6.2)	$43 \pm 26\%$
Accounting for difference between edge and total f_{esc} (§6.3)	$\approx 50\%$

6.4 Consistency with existing LBG and LAE escape fraction constraints

A back-of-the-envelope consistency check for our estimated LyC f_{esc} comes from recent stacked f_{esc} measurements of $M_{\text{UV}} \lesssim -19$ LBGs at $z \approx 2.5 - 4$ that all find an average $f_{\text{esc}} \approx 5 - 10\%$ (Marchi et al. 2017; Steidel et al. 2018; Pahl et al. 2021). At these redshifts and for comparable M_{UV} the fraction of $L > 0.2L^*$ LAEs (i.e., our survey faint limit) in LBG samples is $\approx 30\%$ (e.g., Santos et al. 2021). Importantly, the entire $p(M_{\text{UV}}|L_{\text{Ly}\alpha})$ distribution for $L > 0.2L^*$ LAEs is contained at $M_{\text{UV}} < -19$ as seen via the XLS-z2 sample (Matthee et al. 2021). If half of these LAEs (i.e., 15% of LBGs) have an average $f_{\text{esc}} \approx 40\%$ at the Lyman edge, and all other galaxies have $f_{\text{esc}} \approx 0\%$ then the stacked f_{esc} for an $M_{\text{UV}} \lesssim -19$ LBG sample should be $\approx 5 - 10\%$, in excellent agreement with literature estimates. Another cross check comes from the fraction of individually detected leakers in the LBG samples – for the Keck Lyman Continuum Survey (KLCS) this fraction is $\approx 10\%$ (Pahl et al. 2021), which is consistent with the $\approx 15\%$ ($< 15\%$ with IGM damping) implied by our results. For a more sophisticated exploration of how our LAE constraints translate to the overall LBG population, we refer readers to §5 of our companion paper (Matthee & Naidu et al. 2021).

As for LyC studies of LAEs, Oesch et al. (2021) and Bian & Fan (2020) stacked direct LyC imaging at $z \approx 3$ from the Hubble Deep UV Survey (HDUV, Oesch et al. 2018) with samples dominated by $M_{\text{UV}} \lesssim -18$ LAEs from the MUSE-Wide (Urrutia et al. 2019) and MUSE-HUDF (Bacon et al. 2017) surveys. These authors report 2σ upper limits of $\lesssim 20\%$ on the $\approx 900\text{\AA}$ f_{esc} (see also Japelj et al. 2017 who report consistent estimates using a smaller sample of MUSE LAEs with shallower imaging). On the other hand, the LAE subsample of KLCS ($M_{\text{UV}} < -19$) has reported $f_{\text{esc}} \approx 20\%$, albeit with considerable IGM transmission uncertainties due to their sample size of 26 (Pahl et al. 2021). As we argue that only half the LAEs are in the leaking-phase, the imaging constraints are marginally inconsistent and the spectroscopic constraints in excellent agreement with our results that expect these studies to find $f_{\text{esc}} \approx 20\%$ (half the LAEs have edge f_{esc} of $\approx 40\%$).

7 DISCUSSION

7.1 Implications for constraining LyC f_{esc} with JWST: can strong lines do it all?

A prime directive of LyC studies at $z < 4$ is to identify indirect estimators of LyC that are easily accessible during the EoR. The pressing question is, which spectroscopic features must be targeted in future observations at the highest redshifts? Our High and Low Escape stacks show promising and significant median differences in lines like MgII and CII expected to be tightly linked to the HI column density (e.g., Gazagnes et al. 2018, 2020; Mauerhofer et al. 2021; Henry et al. 2018; Chisholm et al. 2020). This bodes well for programs pursuing these faint features with JWST.

Furthermore, highly ionizing stellar populations (seen via HeII, CIV and extreme optical line EWs), a dust-free, high-ionization state ISM (seen via H α /H β , [OIII]/[OII]) occur, on average, *simultaneously* in the High Escape stack. The LAEs with a low inferred f_{esc} on the other hand are on average dusty, have a less ionised ISM and weaker ionizing populations. Therefore, the correlated nature of these conditions may mean that selecting for any one (or any combination) of these properties dramatically increases the chances of selecting for a low HI column density as well. The possible underlying physics driving the correlated conditions is that highly ionizing stellar populations in super star clusters may be carving porous channels in the HI as well as destroying dust while producing a high ionization state ISM.

At first glance, this may imply that a handful of relatively easily observed strong emission lines may be used to implicitly chart f_{esc} without the need for detecting faint, explicitly HI-linked features such as MgII or [SII] which will likely be measured only for a small fraction of galaxies at $z > 6$. However, there are two important subtleties to this picture.

The first subtlety is that our stacking analysis gives us the *average* picture of leakers and non-leakers. Across individual galaxies there is substantial scatter in any given property among our identified correlated conditions (e.g., high ionization state ISM). For example, the top panel in Fig. 5 suggests substantial scatter between f_{esc} and [OIII]/[OII] in low-redshift analogues (discussed further in §7.2). Some individual LAEs that are part of the Low Escape stack are known to show nebular HeII and CIV emission (e.g. XLS-22; see Amorín et al. 2017). Therefore, our stacks should ideally be compared not to any individual galaxies, but to well-defined stacks of galaxies to constrain the *average* f_{esc} , which is ultimately the key quantity relevant to reionization.

The second subtlety is that our parent sample consists of LAEs with strong Ly α emission. The escape of Ly α emission is likely dependent on the viewing direction (e.g. Behrens et al. 2019; Smith et al. 2019, 2021). It is plausible that a Ly α -selected sample picks out only galaxies viewed at favorable angles, which might minimize the scatter between f_{esc} and galaxy properties reported in previous studies (e.g., Fletcher et al. 2019; Nakajima et al. 2020; Tang et al. 2021). Alternatively, it is possible that the Ly α pre-selection selects for “hidden” parameters that otherwise add scatter to such correlations as well, e.g., the presence of outflows or the relatively low mass of LAEs (e.g. Matthee et al. 2021). Thus, the findings of this work apply only to LAEs, and not to the overall galaxy population.

However, the fraction of UV-selected galaxies that are LAEs increases strongly with redshift (e.g. Stark et al. 2010; Kusakabe et al. 2020). At redshifts $z \sim 6$, the LAE fraction of bright $M_{\text{UV}} \gtrsim -19$ galaxies is about 40%, while it is about 10% at $z \approx 3$ (see Ouchi et al. 2020 for a review). Thus, our findings about LAEs at $z \approx 2$ might apply to a significant fraction of the galaxy population at higher redshifts. Naively extrapolating our results, at $z \approx 8$ when the LAE fraction among $M_{\text{UV}} \lesssim -18$ galaxies may approach $\approx 100\%$, we would expect half the galaxies to be dust-free leakers with average LyC $f_{\text{esc}} \approx 50\%$ and [OIII]/[OII] ≈ 8.5 , while the other half would have $f_{\text{esc}} < 5\%$, [OIII]/[OII] ≈ 3 as well as high $E(B - V)$ evident from Balmer lines. We refer to our companion paper (Matthee & Naidu et al. 2021) for an analysis how the population averaged f_{esc} of UV-selected galaxies may evolve with redshift based on what we know about the evolution of Ly α emission from galaxies over $z \approx 2 - 6$.

7.2 A case for optimism about $[O\text{III}]/[O\text{II}]$ as a LyC f_{esc} predictor at high-redshift

The $[O\text{III}]/[O\text{II}]$ line-ratio has been considered a promising indicator of LyC leakage as it might trace density-bounded nebulae (e.g., Jaskot & Oey 2013; Nakajima & Ouchi 2014) and has been extensively studied due to the relative brightness of both emission-lines. However, tests of this indicator have produced mixed results (e.g., Naidu et al. 2018; Chisholm et al. 2018; Jaskot et al. 2019; Bassett et al. 2019; Nakajima et al. 2020). On the other hand, we identify a stark contrast in $[O\text{III}]/[O\text{II}]$ across our stacks of LAEs (§5).

We consider three effects that may explain the difference between our results and previous work. First, the LAE selection may help reduce the scatter arising from viewing angle effects (e.g. akin to those expected for LyC escape, Gnedin et al. 2008; Paardekooper et al. 2015; Cen & Kimm 2015) by honing in on galaxies at similar, favorable viewing angles to begin with. The LAE selection also selects galaxies with relatively low masses, compact sizes, high specific star formation rate, and elevated star-formation surface density - conditions that may correlate with f_{esc} , and thereby further reduce scatter (e.g. Heckman et al. 2011; Marchi et al. 2018; Cen 2020; Naidu et al. 2020; Matthee et al. 2021). Second, the absence of a strong correlation between f_{esc} and $[O\text{III}]/[O\text{II}]$ in high-redshift analogues at $z \approx 0.3$ that are all LAEs (e.g., Izotov et al. 2021a) may be due to physical sources of scatter that are absent at higher-redshift. These could, for example, be diverse star formation histories on longer timescales that drive differences in chemical abundances in the ionising stellar populations. Third, the absence of strong differences in $[O\text{III}]/[O\text{II}]$ between LAEs classed as LyC leakers or non-leakers using direct imaging experiments (e.g., Fletcher et al. 2019) may be explained by stochasticity in the IGM transmission (e.g. Steidel et al. 2018). Differences in properties such as $[O\text{III}]/[O\text{II}]$ are obscured if average IGM transmission values are applied to compute f_{esc} for individual sources – such samples are then effectively split by IGM transmission and not by whether sources are genuine leakers or non-leakers (e.g., Bassett et al. 2021).

Our Ly α line-profile based strategy likely minimizes viewing angle effects, bypasses IGM transmission stochasticity, and thus helps clearly identify the physical conditions in galaxies associated with LyC escape at high-redshift. The increased prevalence of LAEs with increasing redshift, and the clear variations in $[O\text{III}]/[O\text{II}]$ among LAEs with high and low f_{esc} are likely cause for optimism for $[O\text{III}]/[O\text{II}]$ as a stand-alone indicator of the average LyC f_{esc} for galaxies at the highest redshifts.

7.3 The interplay between Ly α EW and LyC f_{esc} : high f_{esc} does not imply low EWs

It may seem intuitive that high LyC f_{esc} sources must have weak emission lines since large fractions of ionizing photons are lost to the IGM without exciting emission in the ISM. Thus, a potential concern underlying this work is that the Ly α line luminosity may decrease with increasing f_{esc} , and the most prolific LyC leakers are missed in our Ly α -selected sample. On the other hand, it is expected (e.g., Dijkstra et al. 2016) as well as observed (e.g., Izotov et al. 2020) that the Ly α escape fraction (and thus the emerging Ly α luminosity) is correlated with the LyC escape fraction as both are sensitive to the HI column density.

The Ly α EW that emerges from a galaxy is plausibly proportional to the intrinsic Ly α EW associated with a stellar population and the Ly α escape fraction. As the Ly α and LyC escape fractions

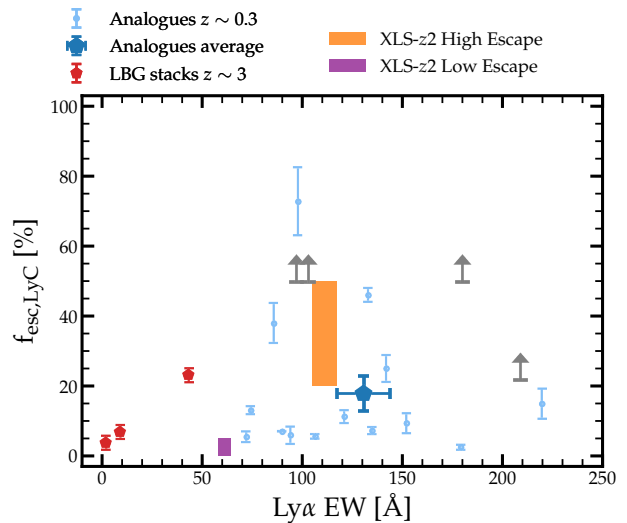


Figure 6. Compilation of observed LyC f_{esc} and observed rest-frame Ly α EWs from stacks of Lyman-break galaxies at $z \sim 3$ (Steidel et al. 2018; Pahl et al. 2021), low-redshift Green Pea galaxies that are analogues to high-redshift galaxies (Izotov et al. 2016b,a, 2018a,b) and a handful of individual high-redshift leakers (GS30668, Ion2, Sunburst Arc, see §3). The f_{esc} values in high-redshift sources are displayed as lower limits due to their uncertain IGM correction. The orange and purple shaded regions show the Ly α EWs and full conservative range of the estimated escape fractions of the High (20 – 50%) and Low Escape (< 5%) XLS-z2 stacks.

are correlated (e.g. Izotov et al. 2021a; Kimm et al. 2021), there is a regime of small LyC f_{esc} where variations in Ly α EWs correlate with $f_{\text{esc, LyC}}$ producing a linear relation (e.g. Steidel et al. 2018). It is expected that the correlation between Ly α EW and $f_{\text{esc, LyC}}$ breaks or flattens eventually (e.g. Nakajima & Ouchi 2014), as very high escape fractions impact the Ly α source term too much. The question is where this break happens, which is complicated as galaxies show varying intrinsic Ly α EWs (i.e. due to differences in stellar ages and metallicities).

We investigate these effects in Fig. 6, where we compiled measured Ly α EWs and LyC f_{esc} , and also illustrate the conservative range of f_{esc} (Table 3) for the High and Low Escape LAEs. The LyC leaker GPs at $z \approx 0.3$ are all accompanied by high observed Ly α EWs $> 70 \text{ \AA}$ (e.g. Izotov et al. 2016b,a, 2018a,b), without the Ly α EW being a criterion in their sample selection. For the leaking GPs, the average LyC f_{esc} is $\approx 20\%$ and the average Ly α EW $\approx 130 \text{ \AA}$. This suggests that these GPs are experiencing particularly young bursts (Chisholm et al. 2019) leading to high intrinsic EWs. None of the confirmed leakers with $f_{\text{esc}} > 10\%$ have a Ly α EW that is below 20-25 \AA (i.e. the typical selection thresholds for LAE surveys). On the other hand, there are several galaxies with a Ly α EW $> 100 \text{ \AA}$, but a moderate $< 10\%$ escape fraction.

There are two key takeaways from this compilation. The first is that the conditions that produce high f_{esc} (e.g., the presence of young, extremely ionizing stellar populations) often also produce very high intrinsic EWs such that even the weakened EWs due to the $(1-f_{\text{esc}})$ in the source term are high (e.g., $\approx 110 \text{ \AA}$ for Ly α in our High Escape stack compared to $\approx 60 \text{ \AA}$ for the Low Escape stack). The second takeaway is that there is considerable scatter in the relation between Ly α EW and f_{esc} , both in individual sources and in our two High and Low Escape stacks, which both show relatively high Ly α EW. High LyC leakage is found in galaxies with

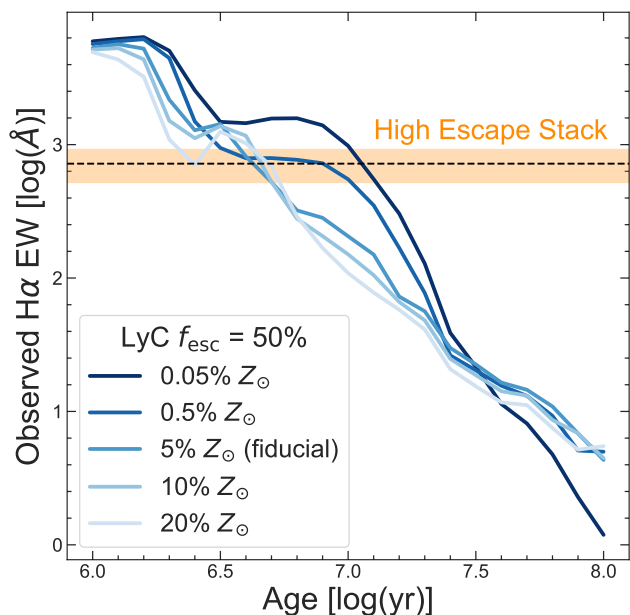


Figure 7. Comparison of observed $H\alpha$ EWs with predictions from BPASS burst SEDs as a function of age and metallicity. The EW from the burst SEDs are adjusted for an $f_{\text{esc}} \approx 50\%$ that we estimated for the High Escape stack (§6). We see that for stellar metallicities consistent with the High Escape stack ($\approx 5\%Z_{\odot}$) only $\approx 2 - 10$ Myr bursts match the observed $H\alpha$ EW.

high emerging $\text{Ly}\alpha$ EWs, suggesting that $\text{Ly}\alpha$ EW may serve as a complete pre-selector of LyC leaking galaxies. However, $\text{Ly}\alpha$ EW alone will also select a high number of false-positives.

7.4 The coincidence of high f_{esc} with high ξ_{ion} and timing the LyC escape phase to $\approx 2 - 10$ Myrs

A main concern of f_{esc} simulations (e.g., Ma et al. 2015) is that short-lived massive stars with highly ionizing spectra are also the stars that need to explode and clear the ISM. The paucity of these massive stars once the ISM is cleared may lead to poor ionizing output. That is, high f_{esc} periods and high ξ_{ion} periods may be out of phase. Our results show that galaxies with high LyC f_{esc} are also the ones with hard ionizing spectra and elevated ξ_{ion} .

What could cause this? Hydrodynamical simulations have emphasized the importance of bursty feedback from young, massive stars in driving LyC f_{esc} (e.g., Rosdahl et al. 2018; Kimm et al. 2019; Ma et al. 2020) where the LyC f_{esc} is expected to be highly stochastic, varying rapidly on ≈ 10 Myr timescales (e.g., Trebitsch et al. 2017; Barrow et al. 2020). We can test this by estimating the burstiness of the recent star formation history in the stacks using EWs of recombination lines like $H\alpha$ that are, to first order, sensitive to the relative number of very hot stars and therefore to the age of stellar populations. These EWs have the added advantage of only mild dependencies on the initial mass function, metallicity and fine-grained properties like binarity and rotation velocity (e.g. Leitherer et al. 1999; Gräferer & Vink 2015).

Following Jaskot & Oey (2013), we estimate the age of the star-bursts in the High and Low Escape stacks based on $H\alpha$ EWs from BPASS (Stanway & Eldridge 2018) and Starburst99 models (Leitherer et al. 1999). We assume a stellar metallicity $Z = 5\%Z_{\odot}$ motivated by the inferred gas-phase metallicity (see also Matthee et al. 2021). The High Escape stack has an $H\alpha$ EW of $\approx 1400 \text{ \AA}$

(corrected for $1/(1-f_{\text{esc}})$)⁶, which requires a very young age of $2 - 10$ Myr for a single burst and $\lesssim 10$ Myr for continuous star formation (see top panel of Figure 7). The $H\alpha$ EW of the Low Escape stack is compatible with a much larger age spread: ≈ 10 Myr for a single burst, but < 200 Myr for continuous star formation. Confirming the emerging picture from simulations, a key distinguishing feature of High Escape galaxies is that they have undergone a very recent ($\lesssim 10$ Myr) burst.

A bursty SFH does not necessarily yield coherence in the phases of high ionising photon production *and* escape. Feedback first needs to clear the birth clouds before LyC f_{esc} can occur. The effects of binary star evolution have been proposed as a remedy to this issue, since they yield significant LyC production even after the most massive stars have exploded (e.g., Ma et al. 2016; Rosdahl et al. 2018; Doughty & Finlator 2021). The EWs of nebular He II and C IV emission can help test this scenario since they are sensitive to hotter stars than H I -ionising stars, and may probe Myr timescales (e.g., Göteborg et al. 2019; Stanway et al. 2020; Senchyna et al. 2021). Knowledge of the origin of these strong nebular lines could in the future further help timing the LyC leaking phases. In addition, more sensitive spectroscopy that can measure P Cygni stellar wind features from e.g. NV and OIV could be useful in constraining the ages of the most massive stars (e.g. Izotov et al. 2018b; Chisholm et al. 2019).

7.5 A unified scheme for LyC Escape and extrapolating $z \approx 2$ results to $z > 6$

In Figure 8 we present a simple unified picture of LyC f_{esc} across all star-forming galaxies by synthesizing our findings, the relation between LAEs and the general galaxy population, and results from recent hydrodynamical simulations (e.g., Trebitsch et al. 2017; Rosdahl et al. 2018; Kimm et al. 2019; Ma et al. 2020; Barrow et al. 2020; Kimm et al. 2021). Our evolutionary sequence for LyC f_{esc} follows in the footsteps of Tenorio-Tagle et al. (1999); Mas-Hesse et al. (2003); Mao et al. (2007) who presented such sequences for the emergence of $\text{Ly}\alpha$ from star-forming galaxies.

We distinguish galaxies as being in one of four phases. In Phase I, super star cluster like objects form in vigorous starbursts. It takes $\approx 2 - 3$ Myrs for the massive stars in them to destroy their birth clouds and clear channels through the ISM via feedback (e.g., winds, supernovae). Phase I might explain the persisting mystery as to why f_{esc} constraints (more precisely, N(HI) constraints) from long Gamma Ray Bursts (GRBs; e.g., Vielfaure et al. 2020) across a wide range of redshifts find low average f_{esc} (e.g., 0.5%, Tanvir et al. 2019), at odds with LBG stacks (e.g. Pahl et al. 2021). A possible explanation is that the short-lived (< 5 Myr) progenitors of long GRBs ($> 40 M_{\odot}$ stars, e.g., Levan et al. 2016) preferentially explode while the birth clouds and ISM are yet to be cleared.

In Phase II, which describes the phase of the galaxies in our High Escape stack, the birth clouds are plausibly disrupted and channels in the ISM have been carved for LyC f_{esc} (§7.4). Binary products, in addition to young stars that continue forming within the ionized shells cleared by feedback, radiate photons into the IGM with a very high ionising photon production efficiency. In Phase III, corresponding to our Low Escape stack, the ISM is more opaque to $\text{Ly}\alpha$ and LyC as feedback weakens since the most massive stars have already exploded – relatively young populations that can

⁶ In the lower limiting case $f_{\text{esc}}=20\%$, the intrinsic $H\alpha$ EW of the High Escape stack is $\approx 900 \text{ \AA}$ which implies ages $\lesssim 7 - 30$ Myr.

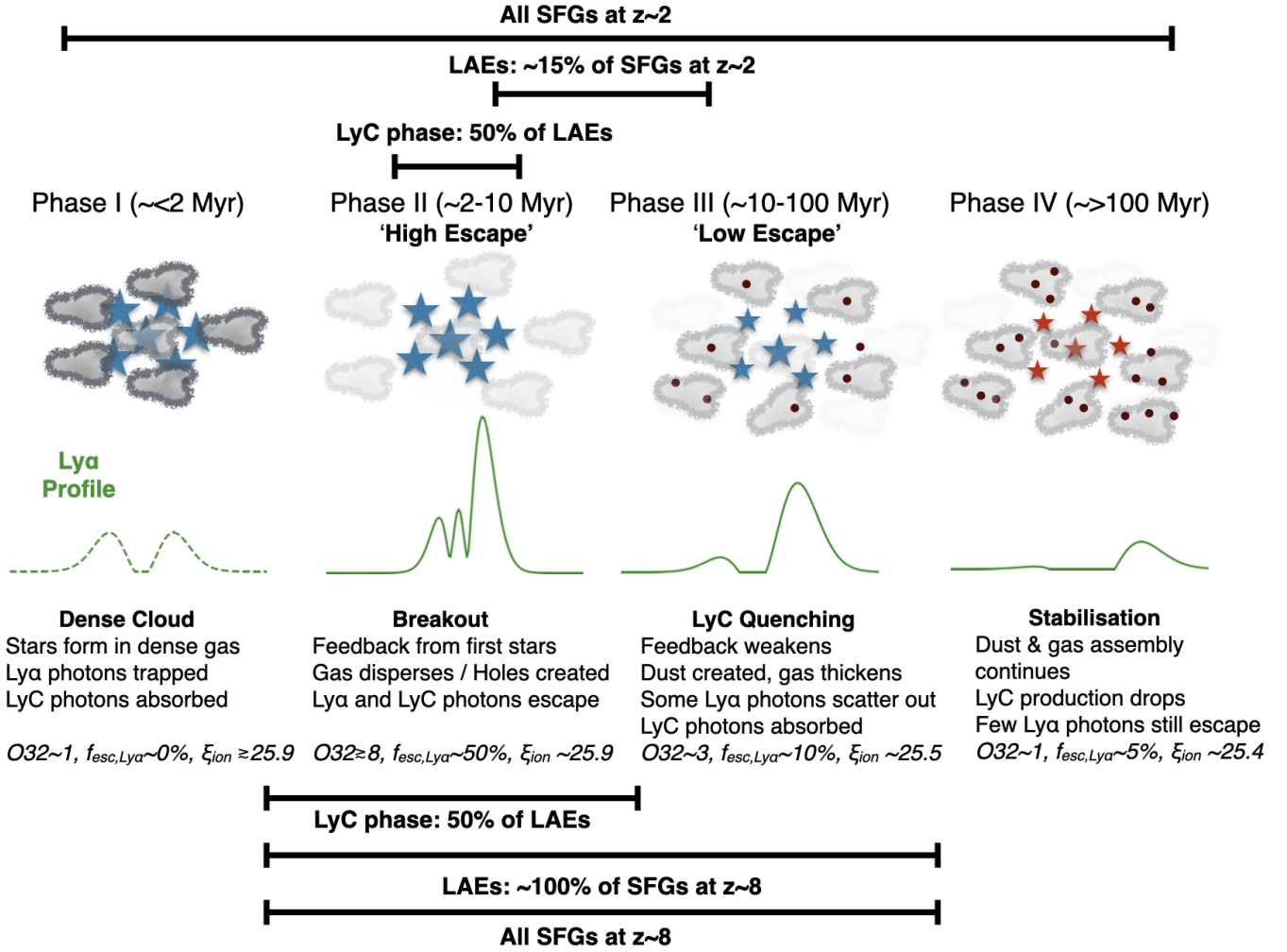


Figure 8. Schematic of the LyC duty cycle. Young stellar populations are depicted as blue stars (sizes scaled by stellar mass), old ones in red, HI is shown as gray clouds (colors scaled with density), and dust is shown as dark brown points. We divide the duty cycle into four phases and show the expected emergent Ly α profile for each phase in green. The proportion of galaxies observed and expected in each phase is indicated at the top and bottom of the plot for $z \approx 2$ and $z \approx 8$ respectively. We note that the fraction of galaxies observed to be in a specific phase is, in addition to the relevant timescales, also likely modulated by the covering fraction of favourable sight-lines between the clusters and the observer. In Phase I, massive stars are born embedded in dense birth clouds – despite their hard ionizing spectra there is little LyC f_{esc} . Phase II, corresponding to the LAEs observed in the High Escape stack, is when the dense birth clouds have been destroyed by feedback, and when high LyC f_{esc} occurs through a transparent ISM – the duration is likely short, because the most ionizing stars are short-lived. In Phase III, corresponding to our Low Escape stack, young stars are still present but the most massive stars have already exploded as core collapse supernovae – the emergent ionizing spectrum is not as hard, and dust/HI in the ISM begin to clog pathways to f_{esc} once again. The majority of star-forming galaxies at $z \approx 2$ are in Phase IV (non-LAE LBGs), and are characterized by older stellar populations and a dusty, high column HI ISM. At any given time, $< 10\%$ of the star-forming galaxy (SFG) population at $z \approx 2$ (half of the LAEs) is in the LyC leaking phase, but this fraction is expected to rise to $\approx 40 - 50\%$ during the EoR as the LAE fraction among the total SFG population rises.

produce Ly α are nonetheless still present. Phase IV describes the ‘steady-state’ LBGs in which the ISM is opaque to dust and HI and the ionising photon production efficiency is about ≈ 3 times lower than during Phase II (e.g. Bouwens et al. 2016 and §5).

Remarkably, we found that half the LAEs are in Phase II despite its short characteristic timescale (< 10 Myrs) compared to Phase III (10-100 Myrs). This implies that the likelihood of observing a galaxy to be in a specific phase is not solely determined by the duration of these phases. There might be two important physical effects at play. First, the fraction of favorable viewing angles such that a Phase II galaxy is observed as a Ly α emitter is likely higher compared to a Phase III galaxy. This may be the case when the large scale ISM around young Phase II clusters has a larger

fraction of low column density and dust-poor sight-lines compared to Phase III bursts (as supported by §5). Second, the duty cycle of Phase II might be rapid, with consecutive bursts occurring in quick succession. Ma et al. (2020) detail such a scenario: an accelerating supernova superbubble sweeps up material in its wake, and consecutive generations of young stars form *inside* the cleared out bubble – a kpc-scale bubble is expected to take $\approx 20 - 40$ Myrs to expand during which it would support Phase II conditions (El-Badry et al. 2019).

At $z \approx 2$, the majority of LBGs are not detected as LAEs (e.g., Cassata et al. 2015; Kusakabe et al. 2018) and Phase IV is therefore the most common. Galaxies in any phase can go back to being in Phase I and II when they undergo starbursts. However, the more

massive a galaxy is, the more unlikely it is that young starbursts can dominate significant fraction of the light. This could be either because they are out-shined by older star-forming regions, or because the fraction of favourable sight-lines through the galaxy decreases with increasing mass. This may be reflected by observations that find that the Ly α escape fraction generally decreases with increasing mass for galaxies selected irrespective of their Ly α strength (e.g. Matthee et al. 2016; Oyarzún et al. 2017). Our line-profile statistics (§3.3) suggest that Phase II is concentrated in a minority (< 10%, i.e., half the LAEs) of the overall galaxy population ($\geq 0.5L^*$ LBGs) at $z \approx 2$.

This framework helps explain the rarity of LyC leakers at lower redshifts and their probable increasing incidence at higher redshifts (e.g. Faucher-Giguère 2020) in terms of the growing LAE fraction (specifically Phase II fraction) among LBGs. At higher redshifts, the LAE population forms an increasing fraction of the LBG population (e.g. Stark et al. 2010), and therefore a higher fraction of the total galaxy population occupies Phases II-III sketched in Fig. 8. There are already strong hints that Phase II conditions (e.g., high [OIII]/[OII], extreme [OIII] EWs) grow increasingly common towards the EoR in lockstep with the rising LAE fraction (e.g., Labbé et al. 2013; De Barros et al. 2019; Endsley et al. 2021). At $z \approx 2$ when the LAE fraction among $M_{UV} < -18$ LBGs is ≈ 0.1 , the average LyC f_{esc} is ≈ 0.05 , whereas at $z \approx 8$ when the LAE fraction may be ≈ 1 , we expect an average f_{esc} of 0.25 (half the LAEs have $f_{esc} \approx 50\%$, the other half have $f_{esc} \approx 0$, non-LAEs have $f_{esc} \approx 0$). Indeed, the Ly α escape fraction measured in LAEs at $z \approx 2$ is comparable to the LBG population-averaged Ly α escape fraction at $z > 6$ (Hayes et al. 2011; Sobral et al. 2017a; Matthee et al. 2021). This implies that – if the Ly α to LyC connection is not evolving – the average LyC escape fraction of LAEs at $z \approx 2$ is comparable to the average LyC escape fraction of the star-forming galaxy population in the Epoch of Reionisation.

It is therefore plausible that we can extrapolate our f_{esc} results on LAEs at $z \approx 2$ to LAEs at $z > 3$ as LAEs show redshift-invariance of various properties relevant to f_{esc} – sizes, Σ_{SFR} , line profiles, β_{UV} slopes, and luminosity functions (e.g., Malhotra et al. 2012; Paulino-Afonso et al. 2018; Herenz et al. 2019; Santos et al. 2020; Hayes et al. 2021), but direct tests – such as the evolution of the distribution of Ly α line-profiles with redshift – would be able to verify this. In a companion paper (Matthee & Naidu et al. 2021), we quantify the implications of this framework by showing the ionizing emissivity from bright LAEs is sufficient to explain the cosmic ionizing background from $z \approx 2 - 8$.

7.6 Caveats & Limitations

Here we discuss caveats and limitations around our results and ways to address them.

While theoretically well-motivated, and validated by multiple independent spectroscopic indicators (§5), our Ly α profile-based LyC selection criteria were designed based on a small sample of ≈ 25 sources that have both high-resolution Ly α profiles as well as direct LyC f_{esc} measurements. These criteria must be further validated with larger samples – e.g., there are now ≈ 20 LyC leaker candidates at $z \approx 2-4$ awaiting high-resolution Ly α measurements (e.g., Bian et al. 2017; Steidel et al. 2018; Fletcher et al. 2019).

A $\approx 4\times$ larger sample would help confirm our results and reduce the error on the fraction of LyC leaking LAEs by half (currently we report $50 \pm 10\%$). However, obtaining high-resolution spectra spanning the entire rest-frame UV to optical wavelength range that we have analyzed here is challenging. Very few datasets

currently exist at *any* redshift with such coverage. We hope the validation of the Ly α -based approach in this study spurs greater investments in large surveys designed to measure the bare minimum high-resolution Ly α coupled with a precise systemic redshift for galaxies drawn representatively from Ly α LFs (see Matthee & Naidu et al. 2021 for a Ly α -LF based framework for the emissivity).

The high ionization lines (CIV $\lambda 1548, \lambda 1550$, HeII $\lambda 1640$) detected only in the $f_{esc} > 20\%$ stack may prove very informative – they show extremely ionizing (> 54.4 eV) photons are produced during periods of elevated LyC f_{esc} . However, latest stellar population models are unable to match the observed EWs of these lines (bottom panel of Figure 7), and so quantitative details relying on these models such as the exact time when HeII $\lambda 1640$ production peaks after a burst are uncertain. We now have yet another motivating reason – understanding LyC f_{esc} – to unravel the origins of nebular HeII (e.g., Stanway et al. 2020; Senchyna et al. 2021; Simmonds et al. 2021; Olivier et al. 2021).

Finally we comment on the generalizability of our results to lower and higher redshifts. To first order, the framework presented in Figure 8 applies to any redshift – what changes is the fraction of galaxies that are in each phase. However, it must also be acknowledged that despite all their similarities, $z \approx 2$ LAEs may have different star-formation histories, stellar abundances, and interstellar media compared to $z \approx 0$ LAEs or $z \approx 6$ LAEs. In our framework these differences would manifest in the details and duration of each phase. For instance, Phase II (the LyC phase), may be even more leaky and extended at $z \approx 6$ given possibly lower metallicities and thus harder ionizing spectra (bottom panel of Fig. 7). To clarify this issue we need a systematic study of the detailed ISM and stellar populations of LAEs across redshift in the style of Izotov et al. (2021b) who focused on compact star-forming galaxies.

8 SUMMARY & OUTLOOK

We seek to isolate the physical conditions for LyC f_{esc} by comparing samples of LyC leakers (inferred $f_{esc} > 20\%$, High Escape) against a control sample of non-leakers (inferred $f_{esc} < 5\%$, Low Escape). Such a controlled study has been difficult to perform at high- z due to sightline effects and at low- z due to complex selection functions. Here we circumvent these hurdles by using resolved Ly α profiles from the luminosity-limited XLS- $z2$ survey to select leakers and non-leakers. Our empirically motivated selection criteria using the Ly α peak separation (v_{sep}) and central fraction (f_{cen}) are based on literature sources with f_{esc} measurements at $z \approx 0-4$, and have solid theoretical grounding in decades of radiative transfer simulations [§3, Figs. 1, 2, 3, Table 1]. By contrasting stacked spectra of the High Escape and Low Escape samples we find the following [Figure 4, Table 2]:

- The robustness of our stacks – that they do separate leakers ($f_{esc} > 20\%$) from non-leakers ($f_{esc} < 5\%$) – is confirmed by half a dozen independent spectroscopic indicators sensitive to HI and dust, the two chief regulators of f_{esc} . In the High Escape stack MgII is observed close to the systemic velocity, the resonant CIV is in emission, the Ly α f_{esc} which is \geq LyC f_{esc} is $\approx 50\%$, CII absorption that is a hallmark of dense HI columns is undetected, and the $H\alpha/H\beta \approx 2.8$ reveals a dust-free ISM. On the other hand, the low escape stack shows redshifted MgII ($+130$ km s $^{-1}$), no CIV emission, $f_{esc, LyC} \leq f_{esc, Ly\alpha} \approx 10\%$, strong CII absorption, and $H\alpha/H\beta \approx 4$ implying $E(B - V) \approx 0.3$. [§5.3-§5.7, Figure 4, Table 2]

- The leakers show strong nebular He II and C IV emission in the *median* stack, signaling the ubiquity of hard ionizing spectra along with a $\log(\xi_{\text{ion}}/\text{Hz erg}^{-1}) \approx 25.7 - 25.9$ (for $f_{\text{esc}} = 20 - 50\%$). These high-ionization features and extreme EWs (e.g., [O III]+H β rest-frame EW $\approx 1100\text{\AA}$) can be produced only by young (< 10 Myr), low metallicity ($< 10\%Z_{\odot}$) stellar populations in theoretical burst SEDs. Low Escape sources have similar M_{UV} and a high $\log(\xi_{\text{ion}}/\text{Hz erg}^{-1}) \approx 25.6$ but lack the extreme EWs and He II (> 54.4 eV). That is, the star-formation in leakers and non-leakers is similar on timescales of ≈ 100 Myrs but not on ≈ 10 Myrs. [§5.1, Figure 4, Table 2]

- The massive star-formation in the High Escape sources is occurring in an extreme ionization state ISM ([O III]/[O II] ≈ 8.5 , $\log(U) \approx -2.3$), comparable to local super star cluster complexes. Non-leakers have a less ionized ISM with [O III]/[O II] ≈ 3 . [§5.4, Figure 4, Table 2]

- The LyC f_{esc} at $850 - 912\text{\AA}$ (“Lyman edge f_{esc} ”) of the High Escape stack is $20 - 55\%$ – the lower bound is by the Ly α profile-based selection and the upper bound is by requiring $f_{\text{esc,Ly}\alpha} \geq f_{\text{esc,LyC}}$. We make a finer estimate of the edge LyC f_{esc} ($\approx 40\%$) by exploiting empirical correlations with the Ly α f_{esc} and the Ly α red-peak velocity. Since the $< 850\text{\AA}$ photons that are ubiquitous among the leakers escape easily compared to edge photons, we estimate the total f_{esc} ($0 - 912\text{\AA}$) that matters for reionization calculations to be $\approx 50\%$. [§6.3, Table 3, Figure B.1]

- With *JWST*, the LyC f_{esc} for $z > 6$ galaxies may be constrained with a handful of strong emission lines. The defining characteristics of leakers – low column densities, hard ionizing spectra, a dust-free, high-ionization state ISM – occur *simultaneously* in the $f_{\text{esc}} > 20\%$ stack of LAEs. That is, these properties are highly correlated, and selecting for one of them increases the chances of selecting the others on *average* – significant scatter across individual galaxies still exists. So even though [O III]/[O II] and Balmer decrements are not explicitly sensitive to HI, they may be sufficient to implicitly estimate the average f_{esc} . This result is derived for LAEs, but is applicable to the EoR since the majority of $z > 6$ galaxies are expected to be LAEs. [§7.1, Figure 5]

- Observed emission lines need not be weak when LyC f_{esc} is high. Based on our stacks as well as a literature compilation of leakers we argue high f_{esc} occurs during a period of prolific ionizing photon production and so the intrinsic emission line EWs are so high that the observed EWs (e.g., $\approx 110\text{\AA}$ for Ly α) are still $\approx 2\times$ higher than non-leakers. [§7.3, Figure 6]

- We chart the highly non-linear relationship between observed Ly α EW and LyC f_{esc} . The Ly α EW serves as a complete but highly impure selector of high f_{esc} galaxies. For instance, our $f_{\text{esc}} < 5\%$ stack has a $\approx 60\text{\AA}$ EW, which according to the linear Ly α EW - LyC f_{esc} relation in Steidel et al. (2018); Pahl et al. (2021) implies a LyC $f_{\text{esc}} \approx 30\%$ that is strongly ruled out by the indicators discussed above (e.g., $f_{\text{esc,Ly}\alpha} \approx 10\% \geq f_{\text{esc,LyC}}$). [§7.3, Figure 6]

- We synthesize our findings in the following physical picture that confirms several aspects of recent hydrodynamical simulations. LyC leakers are galaxies that have undergone recent (< 10 Myr) episodes of vigorous star-formation. The super star clusters born out of these episodes have produced spatially concentrated feedback. This feedback has carved channels through the ISM, thus clearing paths for LyC. Crucially, for reionization, even after the ISM is

cleared a reservoir of highly ionizing sources is still available to stream photons into the IGM. The galaxies with properties that favour a high escape of ionizing photons are also the galaxies that emit copious amounts of those photons at the right time – production and escape occur in sync. In sharp contrast, non-leakers (despite being strong Ly α emitters in our sample) have a relatively dusty, opaque ISM that has not been cleared out by feedback, most likely linked to their dearth of the youngest, most massive stars. [§7.4 - 7.5, Figures 7, 8]

An important contribution of this work is the statistics of LyC f_{esc} among LAEs. Half the LAEs have $f_{\text{esc}} \approx 50\%$, the other half have $f_{\text{esc}} < 5\%$, and non-LAE LBGs have $f_{\text{esc}} \approx 0\%$ (LyC $f_{\text{esc}} \leq \text{Ly}\alpha$ $f_{\text{esc}} \approx 0$). Since fundamental LAE properties are redshift-invariant, we can, with some confidence, extrapolate the constraints derived here to LAEs at higher redshifts. While comprising a minuscule fraction of the overall galaxy population at $z \approx 2$, the LAE fraction strongly evolves such that almost every $L_{\text{UV}} > 0.1L^*$ galaxy at $z \approx 8$ is perhaps an LAE. This work motivates and forms the basis of a Ly α -based formalism for the cosmic ionizing emissivity that uses Ly α luminosity functions instead of UV luminosity functions. The L_{UV} that varies on ≈ 100 Myr timescales and is insensitive to the HI column densities is replaced with $L_{\text{Ly}\alpha}$ that is intimately tied to the bursty, stochastic LyC f_{esc} that fluctuates on Myr timescales. Developing this Ly α -anchored formalism for reionization is the focus of our companion paper.

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DATA AVAILABILITY

The VLT/X-SHOOTER data underlying this article were accessed from the ESO archive. The raw ESO data can be accessed through <http://archive.eso.org/cms.html>. The *HST*/COS spectra were accessed through the Lyman- α Spectral Database accessible through <http://lasd.lyman-alpha.com/>. The derived data generated in this research will be shared on reasonable request to the corresponding authors.

REFERENCES

- Amorín R., et al., 2017, *Nature Astronomy*, **1**, 0052
 Astropy Collaboration et al., 2013, *A&A*, **558**, A33
 Bacon R., et al., 2017, *A&A*, **608**, A1
 Barrow K. S. S., Robertson B. E., Ellis R. S., Nakajima K., Saxena A., Stark D. P., Tang M., 2020, *ApJ*, **902**, L39
 Bassett R., et al., 2019, *MNRAS*, **483**, 5223
 Bassett R., Ryan-Weber E. V., Cooke J., Meštrić U., Kakiichi K., Prichard L., Rafelski M., 2021, *MNRAS*, **502**, 108
 Becker G. D., Bolton J. S., 2013, *MNRAS*, **436**, 1023
 Behrens C., Dijkstra M., Niemeyer J. C., 2014, *A&A*, **563**, A77
 Behrens C., Pallottini A., Ferrara A., Gallerani S., Vallini L., 2019, *MNRAS*, **486**, 2197
 Berg D. A., Erb D. K., Auger M. W., Pettini M., Brammer G. B., 2018, *ApJ*, **859**, 164
 Berg D. A., Chisholm J., Erb D. K., Pogge R., Henry A., Olivier G. M., 2019, *ApJ*, **878**, L3
 Bian F., Fan X., 2020, *MNRAS*, **493**, L65
 Bian F., Fan X., McGreer I., Cai Z., Jiang L., 2017, *ApJ*, **837**, L12
 Bian F., Kewley L. J., Dopita M. A., 2018, *ApJ*, **859**, 175
 Bouwens R. J., Smit R., Labbé I., Franx M., Caruana J., Oesch P., Stefanon M., Rasappu N., 2016, *ApJ*, **831**, 176
 Bouwens R. J., et al., 2021, arXiv e-prints, p. [arXiv:2102.07775](https://arxiv.org/abs/2102.07775)
 Calhau J., et al., 2020, *MNRAS*, **493**, 3341
 Cardelli J. A., Clayton G. C., Mathis J. S., 1989, *ApJ*, **345**, 245
 Cassata P., et al., 2015, *AAP*, **573**, A24
 Cen R., 2020, *ApJ*, **889**, L22
 Cen R., Kimm T., 2015, *ApJ*, **801**, L25
 Chevallard J., et al., 2018, *MNRAS*, **479**, 3264
 Chisholm J., et al., 2018, *A&A*, **616**, A30
 Chisholm J., Rigby J. R., Bayliss M., Berg D. A., Dahle H., Gladders M., Sharon K., 2019, *ApJ*, **882**, 182
 Chisholm J., Prochaska J. X., Schaerer D., Gazagnes S., Henry A., 2020, *MNRAS*, **498**, 2554
 Davis D., et al., 2021, arXiv e-prints, p. [arXiv:2107.11319](https://arxiv.org/abs/2107.11319)
 De Barros S., Oesch P. A., Labbé I., Stefanon M., González V., Smit R., Bouwens R. J., Illingworth G. D., 2019, *MNRAS*, **489**, 2355
 Dijkstra M., Gronke M., Venkatesan A., 2016, *ApJ*, **828**, 71
 Dopita M. A., et al., 2006, *ApJ*, **647**, 244
 Doughty C., Finlator K., 2021, *MNRAS*, **505**, 2207
 Draine B. T., 2011, Physics of the Interstellar and Intergalactic Medium
 Duncan K., Conselice C. J., 2015, *MNRAS*, **451**, 2030
 El-Badry K., Ostriker E. C., Kim C.-G., Quataert E., Weisz D. R., 2019, *MNRAS*, **490**, 1961
 Endsley R., Stark D. P., Chevallard J., Charlot S., 2021, *MNRAS*, **500**, 5229
 Fan X., et al., 2006, *AJ*, **132**, 117
 Faucher-Giguère C.-A., 2018, *MNRAS*, **473**, 3717
 Faucher-Giguère C.-A., 2020, *MNRAS*, **493**, 1614
 Feltre A., Charlot S., Gutkin J., 2016, *MNRAS*, **456**, 3354
 Feltre A., et al., 2018, *A&A*, **617**, A62
 Finkelstein S. L., et al., 2019, *ApJ*, **879**, 36
 Fletcher T. J., Tang M., Robertson B. E., Nakajima K., Ellis R. S., Stark D. P., Inoue A., 2019, *ApJ*, **878**, 87
 Gawiser E., et al., 2007, *ApJ*, **671**, 278
 Gazagnes S., Chisholm J., Schaerer D., Verhamme A., Rigby J. R., Bayliss M., 2018, *A&A*, **616**, A29
 Gazagnes S., Chisholm J., Schaerer D., Verhamme A., Izotov Y., 2020, *A&A*, **639**, A85
 Gnedin N. Y., Kravtsov A. V., Chen H.-W., 2008, *ApJ*, **672**, 765
 Götzberg Y., de Mink S. E., Groh J. H., Leitherer C., Norman C., 2019, *A&A*, **629**, A134
 Gräfener G., Vink J. S., 2015, *AAP*, **578**, L2
 Gronke M., 2017, *A&A*, **608**, A139
 Gronke M., Dijkstra M., Trenti M., Wyithe S., 2015a, *MNRAS*, **449**, 1284
 Gronke M., Bull P., Dijkstra M., 2015b, *ApJ*, **812**, 123
 Gronke M., Dijkstra M., McCourt M., Oh S. P., 2016, *ApJ*, **833**, L26
 Gronwall C., et al., 2007, *ApJ*, **667**, 79
 Guseva N. G., et al., 2020, *MNRAS*, **497**, 4293
 Haardt F., Madau P., 2012, *ApJ*, **746**, 125
 Hansen M., Oh S. P., 2006, *MNRAS*, **367**, 979
 Harikane Y., et al., 2018, *ApJ*, **859**, 84
 Hashimoto T., et al., 2015, *ApJ*, **812**, 157
 Hashimoto T., et al., 2017, *A&A*, **608**, A10
 Hayes M., 2015, *Publ. Astron. Soc. Australia*, **32**, e027
 Hayes M., et al., 2010, *Nature*, **464**, 562
 Hayes M., Schaerer D., Östlin G., Mas-Hesse J. M., Atek H., Kunth D., 2011, *ApJ*, **730**, 8
 Hayes M., et al., 2013, *ApJ*, **765**, L27
 Hayes M. J., Runnholm A., Gronke M., Scarlata C., 2021, *ApJ*, **908**, 36
 Heckman T. M., et al., 2011, *ApJ*, **730**, 5
 Henry A., Berg D. A., Scarlata C., Verhamme A., Erb D., 2018, *ApJ*, **855**, 96
 Herenz E. C., et al., 2019, *A&A*, **621**, A107
 Hunter J. D., 2007, *Computing In Science & Engineering*, **9**, 90
 Hutter A., Dayal P., Legrand L., Gottlöber S., Yepes G., 2021, *MNRAS*, **506**, 215
 Indebetouw R., et al., 2009, *ApJ*, **694**, 84
 Inoue A. K., 2010, *MNRAS*, **401**, 1325
 Inoue A. K., Hirashita H., Kamaya H., 2001, *ApJ*, **555**, 613
 Inoue A. K., Shimizu I., Iwata I., Tanaka M., 2014, *MNRAS*, **442**, 1805
 Israel F. P., Kennicutt R. C., 1980, *Astrophys. Lett.*, **21**, 1
 Izotov Y. I., Schaerer D., Thuan T. X., Worseck G., Guseva N. G., Orlitová I., Verhamme A., 2016a, *MNRAS*, **461**, 3683
 Izotov Y. I., Orlitová I., Schaerer D., Thuan T. X., Verhamme A., Guseva N. G., Worseck G., 2016b, *Nature*, **529**, 178
 Izotov Y. I., Schaerer D., Worseck G., Guseva N. G., Thuan T. X., Verhamme A., Orlitová I., Fricke K. J., 2018a, *MNRAS*, **474**, 4514
 Izotov Y. I., Worseck G., Schaerer D., Guseva N. G., Thuan T. X., Fricke K. J., Verhamme A., Orlitová I., 2018b, *MNRAS*, **478**, 4851
 Izotov Y. I., Schaerer D., Worseck G., Verhamme A., Guseva N. G., Thuan T. X., Orlitová I., Fricke K. J., 2020, *MNRAS*, **491**, 468
 Izotov Y. I., Worseck G., Schaerer D., Guseva N. G., Chisholm J., Thuan T. X., Fricke K. J., Verhamme A., 2021a, *MNRAS*, **503**, 1734
 Izotov Y. I., Guseva N. G., Fricke K. J., Henkel C., Schaerer D., Thuan T. X., 2021b, *A&A*, **646**, A138
 Japelj J., et al., 2017, *MNRAS*, **468**, 389
 Jaskot A. E., Oey M. S., 2013, *ApJ*, **766**, 91

⁷ <http://lasd.lyman-alpha.com>

- Jaskot A. E., Dowd T., Oey M. S., Scarlata C., McKinney J., 2019, *ApJ*, **885**, 96
- Ji Z., et al., 2020, *ApJ*, **888**, 109
- Jones L. H., Barger A. J., Cowie L. L., Oesch P., Hu E. M., Songaila A., Naidu R. P., 2018, *ApJ*, **862**, 142
- Juneau S., et al., 2014, *ApJ*, **788**, 88
- Kakiichi K., Gronke M., 2021, *ApJ*, **908**, 30
- Kauffmann G., et al., 2003, *MNRAS*, **341**, 54
- Kewley L. J., Nicholls D. C., Sutherland R. S., 2019, *ARA&A*, **57**, 511
- Kimm T., Blaizot J., Garel T., Michel-Dansac L., Katz H., Rosdahl J., Verhamme A., Haehnelt M., 2019, *MNRAS*, **486**, 2215
- Kimm T., Bieri R., Geen S., Rosdahl J., Blaizot J., Michel-Dansac L., Garel T., 2021, arXiv e-prints, p. [arXiv:2110.02975](https://arxiv.org/abs/2110.02975)
- Kluyver T., et al., 2016, in Loizides F., Schmidt B., eds, Positioning and Power in Academic Publishing: Players, Agents and Agendas. pp 87 – 90
- Kulas K. R., Shapley A. E., Kollmeier J. A., Zheng Z., Steidel C. C., Hainline K. N., 2012, *ApJ*, **745**, 33
- Kulkarni G., Worseck G., Hennawi J. F., 2019, *MNRAS*, p. 1429
- Kusakabe H., et al., 2018, *PASJ*, **70**, 4
- Kusakabe H., et al., 2020, *A&A*, **638**, A12
- Labbé I., et al., 2013, *ApJ*, **777**, L19
- Labbe I., et al., 2021, UNCOVER: Ultra-deep NIRCam and NIRSpect Observations Before the Epoch of Reionization, JWST Proposal. Cycle 1
- Laursen P., Sommer-Larsen J., Razoumov A. O., 2011, *ApJ*, **728**, 52
- Leitherer C., et al., 1999, *ApJS*, **123**, 3
- Leitherer C., Byler N., Lee J. C., Levesque E. M., 2018, *ApJ*, **865**, 55
- Levan A., Crowther P., de Grijs R., Langer N., Xu D., Yoon S.-C., 2016, *Space Sci. Rev.*, **202**, 33
- Levesque E. M., Richardson M. L. A., 2014, *ApJ*, **780**, 100
- Loeb A., Furlanetto S. R., 2013, The First Galaxies in the Universe
- Lusso E., Worseck G., Hennawi J. F., Prochaska J. X., Vignali C., Stern J., O’Meara J. M., 2015, *MNRAS*, **449**, 4204
- Ma X., Kasen D., Hopkins P. F., Faucher-Giguère C.-A., Quataert E., Kereš D., Murray N., 2015, *MNRAS*, **453**, 960
- Ma X., Hopkins P. F., Kasen D., Quataert E., Faucher-Giguère C.-A., Kereš D., Murray N., Strom A., 2016, *MNRAS*, **459**, 3614
- Ma X., Quataert E., Wetzel A., Hopkins P. F., Faucher-Giguère C.-A., Kereš D., 2020, *MNRAS*, **498**, 2001
- Madau P., Haardt F., Rees M. J., 1999, *ApJ*, **514**, 648
- Maiolino R., Mannucci F., 2019, *A&ARv*, **27**, 3
- Malhotra S., Rhoads J. E., Finkelstein S. L., Hathi N., Nilsson K., McLinden E., Pirzkal N., 2012, *ApJ*, **750**, L36
- Mao J., Lapi A., Granato G. L., de Zotti G., Danese L., 2007, *ApJ*, **667**, 655
- Marchi F., et al., 2017, *A&A*, **601**, A73
- Marchi F., et al., 2018, *A&A*, **614**, A11
- Marques-Chaves R., Schaerer D., Alvarez-Marquez J., Colina L., Dessauges-Zavadsky M., Perez-Fouron I., Saldana-Lopez A., Verhamme A., 2021, arXiv e-prints, p. [arXiv:2107.12313](https://arxiv.org/abs/2107.12313)
- Mas-Hesse J. M., Kunth D., Tenorio-Tagle G., Leitherer C., Terlevich R. J., Terlevich E., 2003, *ApJ*, **598**, 858
- Mason C. A., Treu T., Dijkstra M., Mesinger A., Trenti M., Pentericci L., de Barros S., Vanzella E., 2018, *ApJ*, **856**, 2
- Mason C. A., et al., 2019, *MNRAS*, **485**, 3947
- Matsuoka Y., et al., 2018, *ApJ*, **869**, 150
- Matthee J., Sobral D., Oteo I., Best P., Smail I., Röttgering H., Paulino-Afonso A., 2016, *MNRAS*, **458**, 449
- Matthee J., Sobral D., Best P., Khostovan A. A., Oteo I., Bouwens R., Röttgering H., 2017, *MNRAS*, **465**, 3637
- Matthee J., et al., 2021, *MNRAS*,
- Mauerhofer V., Verhamme A., Blaizot J., Garel T., Kimm T., Michel-Dansac L., Rosdahl J., 2021, *A&A*, **646**, A80
- McCandliss S. R., O’Meara J. M., 2017, *ApJ*, **845**, 111
- Meštrić U., et al., 2020, *MNRAS*, **494**, 4986
- Micheva G., Christian Herenz E., Roth M. M., Östlin G., Girichidis P., 2019, *A&A*, **623**, A145
- Naidu R. P., et al., 2017, *ApJ*, **847**, 12
- Naidu R. P., Forrest B., Oesch P. A., Tran K.-V. H., Holden B. P., 2018, *MNRAS*, **478**, 791
- Naidu R. P., Tacchella S., Mason C. A., Bose S., Oesch P. A., Conroy C., 2020, *ApJ*, **892**, 109
- Nakajima K., Ouchi M., 2014, *MNRAS*, **442**, 900
- Nakajima K., Ellis R. S., Robertson B. E., Tang M., Stark D. P., 2020, *ApJ*, **889**, 161
- Nanayakkara T., et al., 2019, *A&A*, **624**, A89
- Neufeld D. A., 1990, *ApJ*, **350**, 216
- Oesch P. A., et al., 2010, *ApJ*, **709**, L21
- Oesch P. A., et al., 2018, *ApJS*, **237**, 12
- Oesch P. A., Naidu R. P., Leja J., 2021, in prep.
- Oke J. B., Gunn J. E., 1983, *ApJ*, **266**, 713
- Oliphant T. E., 2015, Guide to NumPy. Continuum Press
- Olivier G. M., Berg D. A., Chisholm J., Erb D. K., Pogge R. W., Skillman E. D., 2021, arXiv e-prints, p. [arXiv:2109.06725](https://arxiv.org/abs/2109.06725)
- Orlitová I., Verhamme A., Henry A., Scarlata C., Jaskot A., Oey M. S., Schaerer D., 2018, *A&A*, **616**, A60
- Östlin G., et al., 2021, *ApJ*, **912**, 155
- Ouchi M., et al., 2008, *ApJS*, **176**, 301
- Ouchi M., Ono Y., Shibuya T., 2020, *ARA&A*, **58**, 617
- Oyarzún G. A., Blanc G. A., González V., Mateo M., Bailey John I. I., 2017, *ApJ*, **843**, 133
- Paardekooper J.-P., Khochfar S., Dalla Vecchia C., 2015, *MNRAS*, **451**, 2544
- Pahl A. J., Shapley A., Steidel C. C., Chen Y., Reddy N. A., 2021, arXiv e-prints, p. [arXiv:2104.02081](https://arxiv.org/abs/2104.02081)
- Paulino-Afonso A., et al., 2018, *MNRAS*, **476**, 5479
- Pentericci L., et al., 2014, *ApJ*, **793**, 113
- Pérez F., Granger B. E., 2007, *Computing in Science and Engineering*, **9**, 21
- Pérez-Montero E., Amorín R., Sánchez Almeida J., Vílchez J. M., García-Benito R., Kehrig C., 2021, *MNRAS*, **504**, 1237
- Planck Collaboration et al., 2018, arXiv e-prints, p. [arXiv:1807.06209](https://arxiv.org/abs/1807.06209)
- Plat A., Charlot S., Bruzual G., Feltre A., Vidal-García A., Morisset C., Chevillard J., Todt H., 2019, *MNRAS*, **490**, 978
- Prichard L. J., et al., 2021, arXiv e-prints, p. [arXiv:2110.06945](https://arxiv.org/abs/2110.06945)
- Rafelski M., et al., 2015, *AJ*, **150**, 31
- Ramabason L., Schaerer D., Stasińska G., Izotov Y. I., Guseva N. G., Vílchez J. M., Amorín R., Morisset C., 2020, *A&A*, **644**, A21
- Reddy N. A., Steidel C. C., Pettini M., Bogosavljević M., Shapley A. E., 2016, *ApJ*, **828**, 108
- Reddy N. A., et al., 2020, *ApJ*, **902**, 123
- Reddy N. A., et al., 2021, arXiv e-prints, p. [arXiv:2108.05363](https://arxiv.org/abs/2108.05363)
- Reines A. E., Johnson K. E., Goss W. M., 2008, *AJ*, **135**, 2222
- Rivera-Thorsen T. E., et al., 2017, *A&A*, **608**, L4
- Rivera-Thorsen T. E., et al., 2019, *Science*, **366**, 738
- Robertson B. E., et al., 2013, *ApJ*, **768**, 71
- Robertson B. E., Ellis R. S., Furlanetto S. R., Dunlop J. S., 2015, *ApJ*, **802**, L19
- Rosdahl J., et al., 2018, *MNRAS*, **479**, 994
- Runnholm A., Gronke M., Hayes M., 2021, *PASP*, **133**, 034507
- Sanders R. L., et al., 2015, *ApJ*, **799**, 138
- Santos S., et al., 2020, *MNRAS*, **493**, 141
- Santos S., et al., 2021, *MNRAS*,
- Saxena A., et al., 2020, *A&A*, **636**, A47
- Saxena A., et al., 2021, arXiv e-prints, p. [arXiv:2109.03662](https://arxiv.org/abs/2109.03662)
- Senchyna P., Stark D. P., Charlot S., Chevillard J., Bruzual G., Vidal-García A., 2021, *MNRAS*, **503**, 6112
- Sharma M., Theuns T., Frenk C., Bower R., Crain R., Schaller M., Schaye J., 2016, *MNRAS*, **458**, L94
- Shen X., Hopkins P. F., Faucher-Giguère C.-A., Alexander D. M., Richards G. T., Ross N. P., Hickox R. C., 2020, *MNRAS*, **495**, 3252
- Shibuya T., Ouchi M., Harikane Y., Nakajima K., 2019, *ApJ*, **871**, 164
- Shirazi M., Brinchmann J., 2012, *MNRAS*, **421**, 1043
- Shivaei I., et al., 2018, *ApJ*, **855**, 42
- Simmonds C., Schaerer D., Verhamme A., 2021, arXiv e-prints, p. [arXiv:2108.12438](https://arxiv.org/abs/2108.12438)

- Smith A., Ma X., Bromm V., Finkelstein S. L., Hopkins P. F., Faucher-Giguère C.-A., Kereš D., 2019, *MNRAS*, **484**, 39
- Smith B. M., et al., 2020, *ApJ*, **897**, 41
- Smith A., Kannan R., Garaldi E., Vogelsberger M., Pakmor R., Springel V., Hernquist L., 2021, arXiv e-prints, p. arXiv:2110.02966
- Sobral D., Matthee J., 2019, *A&A*, **623**, A157
- Sobral D., et al., 2017a, *MNRAS*, **466**, 1242
- Sobral D., et al., 2017b, *MNRAS*, **466**, 1242
- Sobral D., Santos S., Matthee J., Paulino-Afonso A., Ribeiro B., Calhau J., Khostovan A. A., 2018, *MNRAS*, **476**, 4725
- Song M., et al., 2014, *ApJ*, **791**, 3
- Stanway E. R., Eldridge J. J., 2018, *MNRAS*, **479**, 75
- Stanway E. R., Chrimes A. A., Eldridge J. J., Stevance H. F., 2020, *MNRAS*, **495**, 4605
- Stark D. P., Ellis R. S., Chiu K., Ouchi M., Bunker A., 2010, *MNRAS*, **408**, 1628
- Stark D. P., Ellis R. S., Ouchi M., 2011, *ApJ*, **728**, L2
- Steidel C. C., Bogosavljević M., Shapley A. E., Reddy N. A., Rudie G. C., Pettini M., Trainor R. F., Strom A. L., 2018, *ApJ*, **869**, 123
- Strom A. L., Steidel C. C., Rudie G. C., Trainor R. F., Pettini M., Reddy N. A., 2017, *ApJ*, **836**, 164
- Strom A. L., Steidel C. C., Rudie G. C., Trainor R. F., Pettini M., 2018, *ApJ*, **868**, 117
- Tacchella S., Forbes J. C., Caplar N., 2020, *MNRAS*, **497**, 698
- Tang M., Stark D. P., Chevallard J., Charlot S., Endsley R., Congiu E., 2021, *MNRAS*, **503**, 4105
- Tanvir N. R., et al., 2019, *MNRAS*, **483**, 5380
- Taylor M. B., 2005, in Shopbell P., Britton M., Ebert R., eds, *Astronomical Society of the Pacific Conference Series Vol. 347, Astronomical Data Analysis Software and Systems XIV*. p. 29
- Tenorio-Tagle G., Silich S. A., Kunth D., Terlevich E., Terlevich R., 1999, *MNRAS*, **309**, 332
- Topping M. W., Shapley A. E., Reddy N. A., Sanders R. L., Coil A. L., Kriek M., Mobasher B., Siana B., 2020, *MNRAS*, **499**, 1652
- Trainor R. F., Steidel C. C., Strom A. L., Rudie G. C., 2015, *ApJ*, **809**, 89
- Trainor R. F., Strom A. L., Steidel C. C., Rudie G. C., 2016, *ApJ*, **832**, 171
- Trebitsch M., Blaizot J., Rosdahl J., Devriendt J., Slyz A., 2017, *MNRAS*, **470**, 224
- Urrutia T., et al., 2019, *A&A*, **624**, A141
- Vanzella E., et al., 2015, *A&A*, **576**, A116
- Vanzella E., et al., 2016, *ApJ*, **825**, 41
- Vanzella E., et al., 2018, *MNRAS*, **476**, L15
- Vanzella E., et al., 2019, arXiv e-prints, p. arXiv:1904.07941
- Vanzella E., et al., 2020, *MNRAS*, **491**, 1093
- Vanzella E., et al., 2021, arXiv e-prints, p. arXiv:2106.10280
- Verhamme A., Schaerer D., Maselli A., 2006, *A&A*, **460**, 397
- Verhamme A., Orlitová I., Schaerer D., Hayes M., 2015, *A&A*, **578**, A7
- Verhamme A., Orlitová I., Schaerer D., Izotov Y., Worseck G., Thuan T. X., Guseva N., 2017, *A&A*, **597**, A13
- Vernet J., et al., 2011, *A&A*, **536**, A105
- Vielhaure J. B., et al., 2020, *A&A*, **641**, A30
- Virtanen P., et al., 2020, *Nature Methods*, **17**, 261
- Wang B., Heckman T. M., Leitherer C., Alexandroff R., Borthakur S., Overzier R. A., 2019, *ApJ*, **885**, 57
- Wang B., et al., 2021, *ApJ*, **916**, 3
- Wise J. H., Cen R., 2009, *ApJ*, **693**, 984
- Wise J. H., Demchenko V. G., Halicek M. T., Norman M. L., Turk M. J., Abel T., Smith B. D., 2014, *MNRAS*, **442**, 2560
- Wisotzki L., et al., 2016, *AAP*, **587**, A98
- da Cunha E., Charlot S., Elbaz D., 2008, *MNRAS*, **388**, 1595

APPENDIX A: $Ly\alpha$ PROFILES OF INDIVIDUAL GALAXIES

Figure A.1 shows the individual $Ly\alpha$ profiles of the XLS-z2 LAEs classified in the High Escape subset, while Figures A.2 and A.3

show the profiles of the LAEs in the Intermediate and Low Escape subsets, respectively. In each panel we list the $Ly\alpha$ escape fraction of the LAE, the fraction of their $Ly\alpha$ emission that escapes within $\pm 100 \text{ km s}^{-1}$ of the systemic redshift (f_{cen}), the peak separation (when applicable) and the velocity difference between the peak of the red line and the nearest minimum blueward of it (i.e. the valley; $v_{\text{red-valley}}$). For XLS-20 we do not list $v_{\text{red-valley}}$ because its $Ly\alpha$ line does not show a distinct asymmetric red peak. For the LAEs in the High Escape subset, we also list the reason why they have been classed in that subset.

We note that in some cases multiple velocity components are detected in the rest-frame optical spectra, such as a broad component (e.g. XLS-18, XLS-24) or a second narrow component (e.g. XLS-12, XLS-16, but also XLS-25 and XLS-35 where they are blended). In these cases, as described in Matthee et al. (2021), the systemic redshift is placed at the component that is spatially closest associated with the $Ly\alpha$ emission. XLS-33 shows triple-peaked $Ly\alpha$ emission, but this is likely due to an absorbing system at $\approx -400 \text{ km s}^{-1}$ (see also XLS-18 for another such example), instead of a peak at the systemic velocity.

APPENDIX B: COMPARISON BETWEEN EDGE (850 – 912Å) AND TOTAL (0 – 912Å) f_{esc}

Here we demonstrate the difference between the edge f_{esc} and total f_{esc} with SEDs matched to the High Escape stack’s highly ionizing nature and with LyC transmission curves for 0 – 912Å. The LyC transmission curves from McCandliss & O’Meara (2017) based on theoretical photoionization cross-sections are a function of three parameters: the column density (N_{HI}), the neutral Hydrogen fraction (X_{HI}), and neutral Helium fraction (X_{HeI}). In the bottom panels we see that even for column densities of $\approx 10^{18} \text{ cm}^{-2}$ where the edge f_{esc} is ≈ 0 , the 0-912Å f_{esc} can be $\approx 20\%$. We also note that free-bound emission of H which peaks shortward of the LyC limit may also affect the determination of the LyC escape fractions, such that reported values may be currently overestimated since they do not account for this (e.g., Inoue 2010). Refined estimates for the edge-to-total correction will require future studies.

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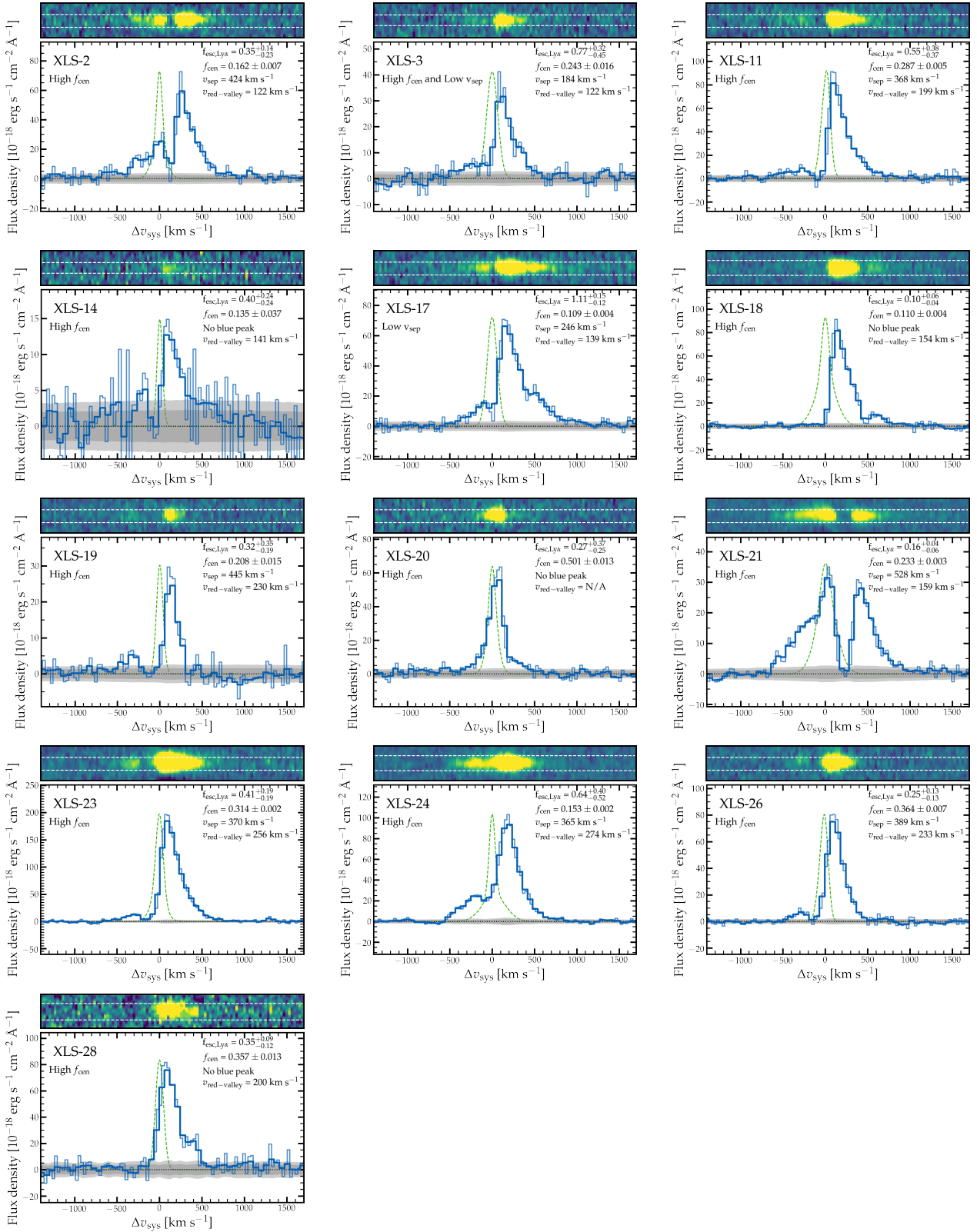


Figure A.1. Individual Lyman- α line-profiles of the LAEs classified in the High Escape subset. The velocity axis is centered on the systemic redshift. The thin and thick blue line shows the Ly α profiles with native and factor two binning, respectively. The green dashed line shows the line-profile of the rest-frame optical lines. The upper inset panels show the two-dimensional Ly α profiles, where the dashed white lines highlight the FWHM of the extraction window.

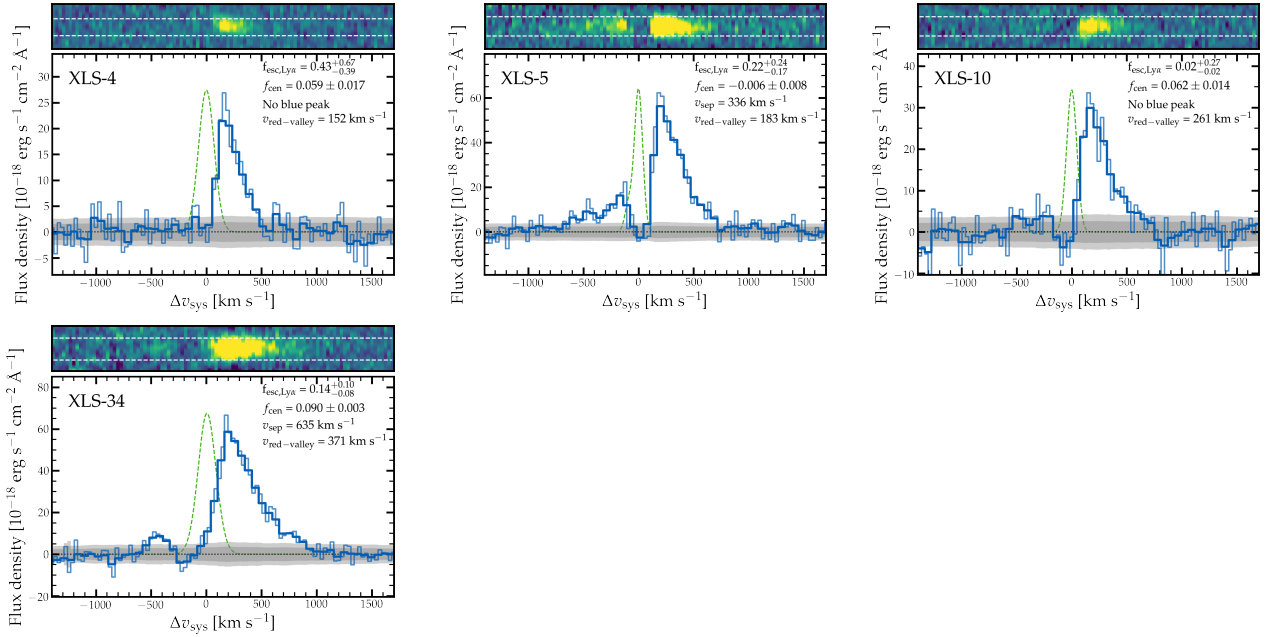


Figure A.2. As Fig. A.1, but now showing individual Lyman- α line-profiles of the LAEs classified in the Intermediate Escape subset.

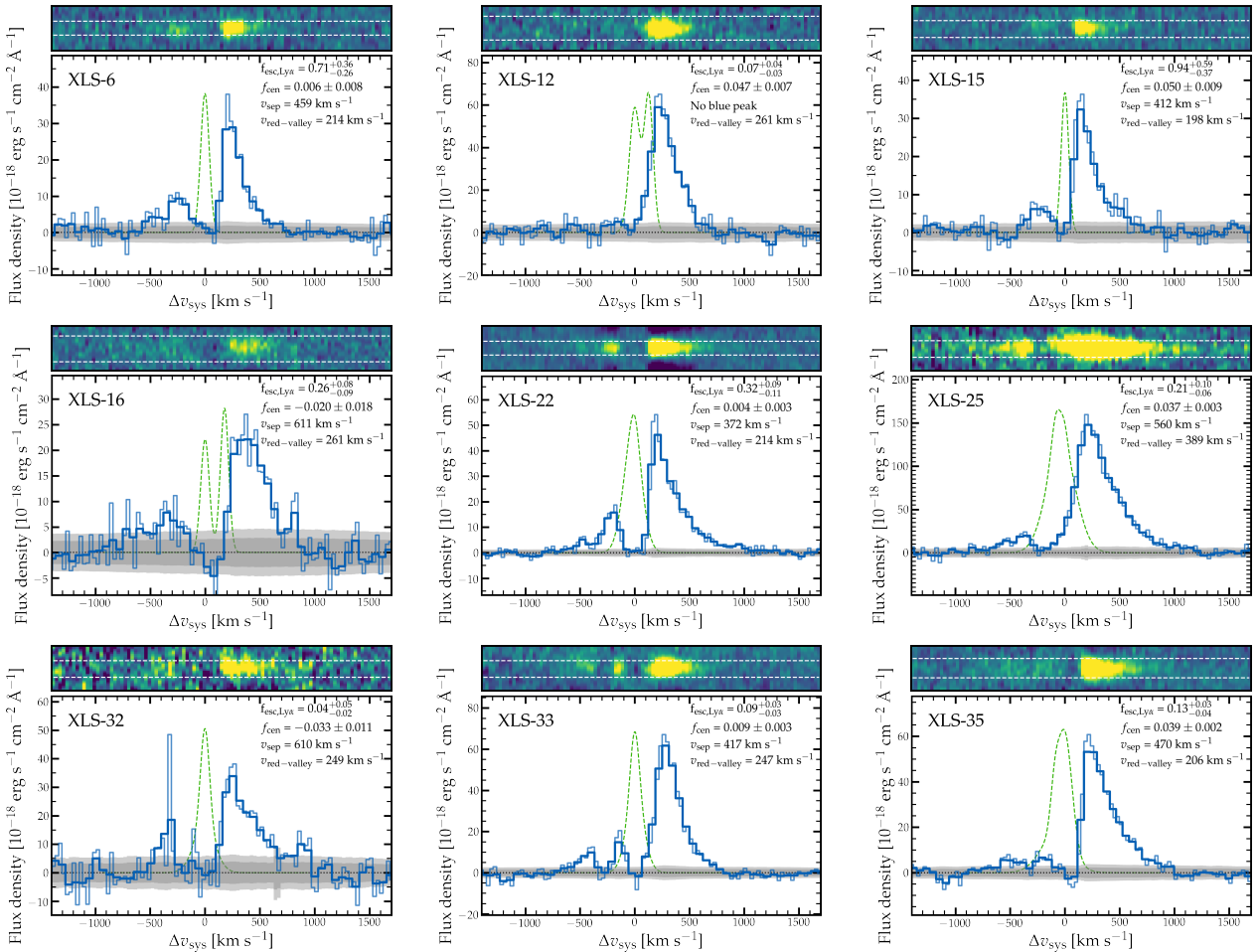


Figure A.3. As Fig. A.1, but now showing individual Lyman- α line-profiles of the LAEs classified in the Low Escape subset.

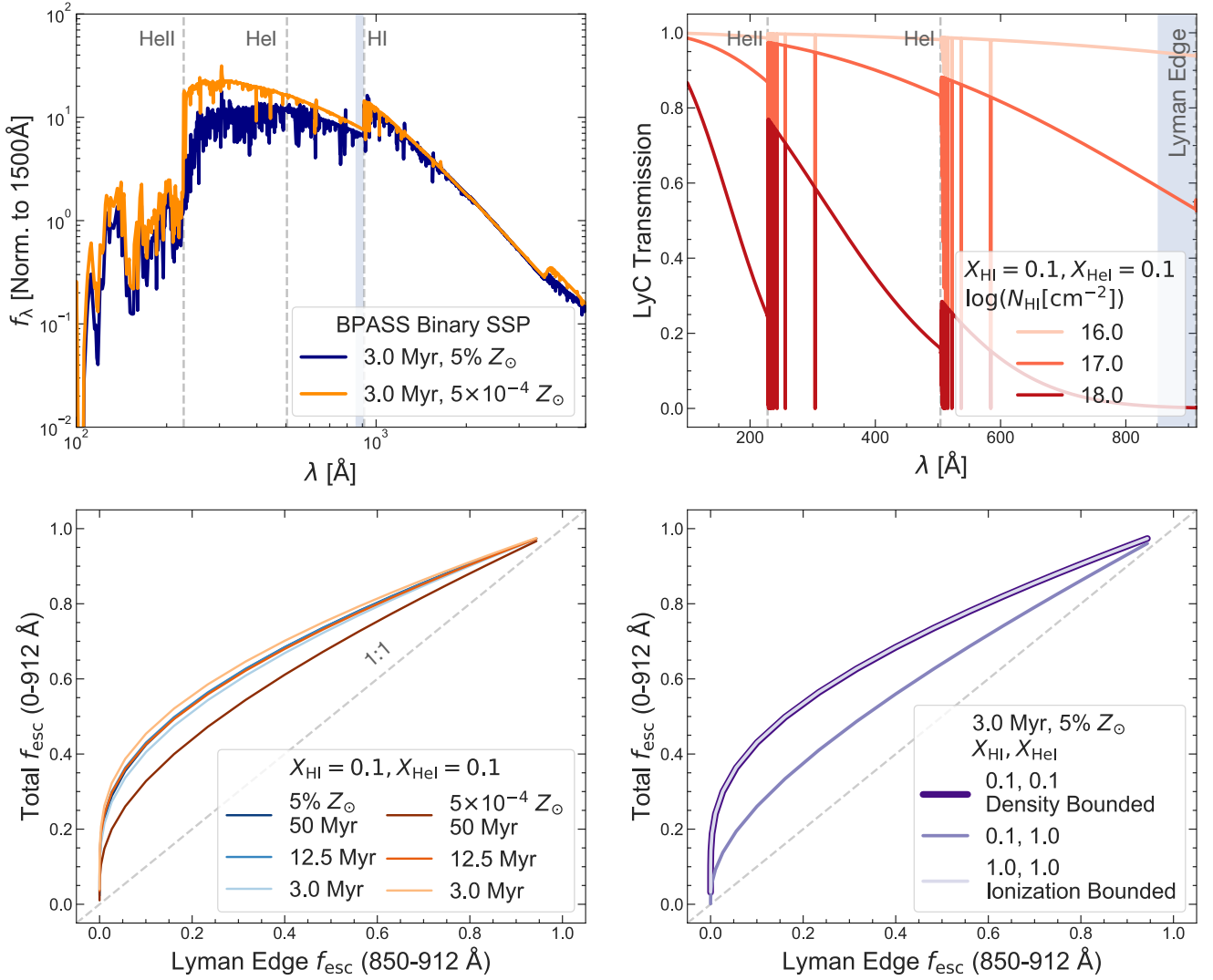


Figure B.1. The difference between Lyman edge f_{esc} (850 – 912 Å) and total f_{esc} (0 – 912 Å). **Top left:** BPASS SEDs selected to illustrate the hard ionizing nature of the High Escape stack. **Top right:** LyC transmission curves from [McCandliss & O’Meara \(2017\)](#) for $\log(N_{\text{HI}})$ and neutral fractions relevant to the semi-permeable portions of density bounded nebulae (see §6.3). **Bottom left:** The LyC f_{esc} computed over the entire ionizing spectrum compared to the f_{esc} measured at the Lyman edge as a function of SED age and metallicity. These curves are a result of convolving the SEDs with LyC transmission curves and comparing against the intrinsic SED. The total f_{esc} lies significantly above the 1 : 1 line (dashed gray). Remarkably, even for meagre edge f_{esc} ($< 5\%$), significant total f_{esc} (20 – 40%) is possible. Varying metallicity and age has little effect on the edge to total f_{esc} conversion. **Bottom right:** Same as bottom-left panel, but exploring the effect of neutral fractions. Somewhat unintuitively, what matters to these curves is not the absolute Hydrogen and Helium neutral fractions, but the fractions *relative* to each other (e.g., the ionization bounded and density bounded cases are indistinguishable).

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