

Lights in a sea of darkness: constraining the nature and properties of dark matter using the stellar kinematics in the centres of ultra-faint dwarf galaxies Zoutendijk, S.L.

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Aims. The lowest-mass galaxies, ultra-faint dwarf galaxies, promise unparalleled constraints on how feedback regulates galaxy formation, and on the small-scale matter power spectrum. Their inner dark-matter densities can also be used to constrain dark-matter models and to determine the most promising targets for potential signals from dark-matter annihilation or decay. However, these goals are limited by the current large uncertainties on the properties of the dark-matter haloes that these galaxies inhabit. In this paper, we present 201 new stellar line-of-sight velocities from the MUSE-Faint survey for the faint and ultra-faint dwarf galaxies Antlia B, Leo T, Hydra II, and Grus 1. Combining these with literature data, we obtain the tightest constraints to date on their dark-matter halo masses and inner dark-matter densities.

Methods. We use the Jeans equations implemented in CJAM to model the density profiles and constrain the presence of dark-matter cores and solitons (a prediction of fuzzy dark-matter models). Further modelling is done with GravSphere to test the influence of the choice of modelling tool. We calculate masses, concentrations, and circular velocities from the profiles, include results for Eridanus 2 from our previous work, and compare these properties to theoretical scaling relations, deriving constraints on tidal stripping in the process.

Results. We find that dark-matter cores as large as those of more massive dwarf galaxies are ruled out for our galaxies (core radius $r_{\rm c}$ < 66–95 pc at the 68% confidence level). We constrain the soliton radii to $r_{\rm sol}$ < 13–112 pc (68% confidence level). We find that the galaxies are consistent with not having been significantly tidally stripped within their half-light radii. The virial masses and concentrations are sensitive to the choice of dynamical modelling tool: GravSphere produces results consistent with $M_{200} \sim 10^9 M_{\odot}$, as expected from models in which ultra-faint dwarf galaxies are re-ionization fossils, while CJAM prefers haloes that are less massive.

S. L. Zoutendijk, M. P. Júlio, J. Brinchmann, J. I. Read, D. Vaz, L. A. Boogaard, N. F. Bouché, D. Krajnović, K. Kuijken, J. Schaye, & M. Steinmetz (2021b). "The MUSE-Faint survey: III. No large dark-matter cores and no significant tidal stripping in ultra-faint dwarf galaxies". arXiv: 2112.09374 [astro-ph.GA], submitted to *Astron. Astrophys*.

The smallest galaxies promise unparalleled constraints on cosmological models, on the nature of dark matter, and on how feedback processes regulate galaxy formation (e.g. Agertz et al., 2020; Battaglia et al., 2013; Bullock & Boylan-Kolchin, 2017; Simon, 2019). They have become a particular focus due to several tensions at the scale of dwarf galaxies between observations and the prevailing ACDM cosmological model (Bullock & Boylan-Kolchin, 2017). Two well-known issues are the core–cusp problem and the missing satellites problem. In the first, dark matter–only simulations predicted steep central density profiles for galaxies of any mass, while observations of several classical dwarf galaxies have shown evidence of constant-density cores (Flores & Primack, 1994; Moore, 1994). The second problem entails that there are far fewer observed satellite galaxies of the Milky Way than that there are subhaloes in dark matter–only simulations (Klypin et al., 1999b; Moore et al., 1999). Both problems could be addressed without abandoning ACDM by accounting for baryonic physics.

Modern hydrodynamical simulations (e.g. Brooks & Zolotov, 2014; Di Cintio et al., 2014b; Governato et al., 2010; Mashchenko et al., 2008; Oñorbe et al., 2015; Read et al., 2016; Teyssier et al., 2013) are able to reproduce cores in dwarf galaxies of mass $M_{200} \sim 10^{10} M_{\odot}$ through repeated cycles of supernova feedback, a dynamical mechanism that has become known as darkmatter heating (e.g. Navarro et al., 1996a; Pontzen & Governato, 2012, 2014; Read & Gilmore, 2005). This process requires sufficient star formation to take place over an extended period such that dwarf galaxies with only old stars are expected to have smaller, denser, dark-matter cores, or no cores at all (e.g. Bermejo-Climent et al., 2018; Brook & Di Cintio, 2015; Read et al., 2016). Indeed, there seems to be mounting observational evidence for this scenario (e.g. Bouché et al., 2022; Read et al., 2019; Sharma et al., 2022).

It remains unclear, however, whether the very smallest and faintest galaxies – ultra-faint dwarf (UFD) galaxies ($M_V > -7.7$; Simon, 2019) – have undergone sufficient star formation to excite dark-matter cusp–core transformations. Models agree that such transformations are likely to be incomplete, yielding in some cases a lowering of the inner density from a pristine dark-matter cusp, but unlikely to form a large, low-density core as found in higher-mass dwarf galaxies (e.g. Read et al., 2019). The issue is made more complex, however, by a competing dynamical mechanism for core formation, dynamical friction (e.g. El-Zant et al., 2001; Nipoti & Binney, 2015), that can act to lower the inner dark-matter density of UFDs, even when they have experienced little star formation (Orkney et al., 2021).

The missing satellites problem can also be solved by baryonic effects, as

it depends on which dark matter halos become luminous due to star formation. The latest abundance-matching models suggest that the most massive subhaloes are occupied by the Milky Way's classical dwarf galaxies. These models favour pre-infall masses for UFDs of $\leq 10^9 M_{\odot}$ (DES Collaboration, 2020; Jethwa et al., 2018; Kim et al., 2018; Read & Erkal, 2019), consistent with the latest high-resolution numerical models (e.g. Agertz et al., 2020; Applebaum et al., 2021; Munshi et al., 2017). However, direct dynamical estimates of UFD pre-infall masses, while consistent with the abundancematching methods and numerical models, are inconclusive due to their order-of-magnitude uncertainties (e.g. Errani et al., 2018; Forbes et al., 2018; Read & Erkal, 2019).

The above solutions to the cusp-core and missing satellite problems yield two key predictions that remain untested: (i) UFDs should have cuspier inner dark-matter density profiles than nearby dwarf irregular galaxies that experience significantly more star formation; and (ii) UFDs should inhabit dark-matter haloes of mass $M_{200} \sim 10^9 M_{\odot}$ or lower. To test these predictions, we require accurate constraints on the dark-matter density profiles of UFDs. Such profiles, when measured close enough to the centre, will directly address the first prediction, while integration of the profile to larger radii will yield the halo masses of UFDs.

With MUSE-Faint (Zoutendijk et al., 2020; Chapter 2 of this thesis; hereafter Paper I), a survey of UFDs with MUSE (Bacon et al., 2010), we are observing the spectroscopically unexplored centres of faint and ultra-faint satellites of the Milky Way. Previously, we have derived constraints on the dark-matter density profile of Eridanus 2 (Eri 2) and on the properties of self-interacting and fuzzy dark matter (Zoutendijk et al., 2021a; Chapter 3 of this thesis; hereafter Paper II). While we could not resolve a core, we found that a core in Eri 2 must be smaller than $\approx 100 \text{ pc}$ (95% confidence level), which is smaller than the cores found in larger dwarf galaxies. To start addressing the above predictions on UFD core size and mass more rigorously, in this paper we expand our analysis to the four additional dwarf galaxies with completed MUSE-Faint observations; in decreasing order of luminosity: Antlia B (Ant B), Leo T, Hydra II (Hya II), and Grus 1 (Gru 1). We use different density profile models to test whether UFDs have cores and how large these cores can be, and to calculate halo properties. We focus on testing the predicted UFD properties in the ACDM paradigm and will therefore model each galaxy individually, without assuming a particular core formation mechanism. We defer a joint analysis of the density profiles, in which we will constrain the nature and properties of dark matter through the core formation prescribed by the dark-matter physics of each model, to a follow-up paper.

By expanding the number of dark-matter profiles from MUSE-Faint galaxies from one to five, we are able to compare the properties of a small population of galaxies with scaling relations and other expectations. First, we introduce our observations and data reduction process (Sect. 4.2) and our methods (Sect. 4.3). We then constrain the density profiles of the new galaxies using three different profile models (core, cusp, and soliton), derive constraints on halo properties, and compare the evidence for the different models (Sects. 4.4.1-4.4.3). Additionally, we test whether the four new galaxies, supplemented with Eri 2, could have undergone tidal stripping of dark matter, and examine how their galaxy and halo properties compare to mass-concentration relations and stellar-to-halo mass ratios determined from simulations and observations of more massive galaxies (Sects. 4.4.4 and 4.4.5). We end with a discussion of our results (Sect. 4.5) and a summary of our conclusions (Sect. 4.6). In Appendix 4.A we test the robustness of our results by repeating our analyses with a different dynamical modelling tool, and we provide figures of the constraints on the profile model parameters, including the core size, in Appendix 4.B.

In keeping with the previous papers in this series, we adopt the *Planck* 2015 cosmological parameters (Planck Collaboration, 2016). For convenience, we consistently show results for the different profile models with the same colour in every figure.

4.2 Observations and data reduction

We describe here the galaxies in our sample (Sect. 4.2.1) and our observations and general process of data reduction (Sect. 4.2.2), followed by details about the individual galaxies (Sects. 4.2.3–4.2.6).

4.2.1 Sample

Ant B is part of the nearby NGC 3109 association and was discovered by Sand et al. (2015) using Blanco/DECam imaging. These data indicate a distance of 1.29 ± 0.10 Mpc, an absolute V-band magnitude of -9.7 ± 0.6 mag, a half-light radius of 0.72 ± 0.7 arcmin (273 ± 29 pc), and the presence of two stellar populations: one with an age >10 Gyr and metallicity [Fe/H] ≈ -2 , the other $\approx 200-400$ Myr old and with [Fe/H] ≈ -1 . No H α was detected with SOAR/Goodman spectroscopy, which is consistent with the lack of a population <100 Myr old (Sand et al., 2015). Radio spectroscopy with GBT/VEGAS revealed (2.8 ± 0.2)×10⁵ M_{\odot} of H I with a line-of-sight velocity of ≈ 375 km s⁻¹. Hargis et al. (2020) followed up with *HST*/ACS photometry, revising the distance to 1.35 ± 0.06 Mpc. They also constrained the starformation history of Ant B using this higher-resolution photometry, which shows that Ant B started forming stars \approx 13 Gyr ago and had its last episode of star formation \approx 2–3 Gyr ago.

The earliest-discovered galaxy in our sample, Leo T, was found by Irwin et al. (2007) in SDSS DR5 images. Follow-up with INT/WFC revealed two stellar populations, one <1 Gyr old, the other 6–8 Gyr old with $[Fe/H] \approx -1.6$. The galaxy was found to have a total absolute magnitude of -7.1 mag and a half-light radius of 1.4 arcmin (170 \pm 15 pc; Simon & Geha, 2007). An H I component of $\approx 2 \times 10^5 M_{\odot}$ was found in HIPASS with a line-of-sight velocity of 35 km s⁻¹ (Irwin et al., 2007), at a distance of 417^{+20}_{-19} kpc (Irwin et al., 2007; Simon & Geha, 2007). Simon & Geha (2007) observed Leo T with Keck/DEIMOS and determined the stars to have a mean line-of-sight velocity of 38.1 ± 2.0 km s⁻¹ with a dispersion of 7.5 km s⁻¹. Their spectroscopy indicates a much lower metallicity. $[Fe/H] = -2.29 \pm 0.10$, than the photometry. Using GMRT and WSRT, Ryan-Weber et al. (2008) find that the H I gas consists of two components with different temperatures, $\approx 500 \text{ K}$ and ≈ 6000 K, where the cold component is more centrally concentrated, as is the younger stellar population. This is confirmed by Adams & Oosterloo (2018) with deeper WSRT data, resulting in an increased H I mass of $4.1 \pm 0.4 \times 10^5 M_{\odot}$, of which $\approx 10\%$ is a cold neutral medium with a velocity dispersion of 2.5 ± 0.1 km s⁻¹, while the remaining part is a warm neutral medium with a velocity dispersion of 7.1 ± 0.4 km s⁻¹. Further photometric studies with LBT/LBC (de Jong et al., 2008) and HST/WFPC2 (Weisz et al., 2012) and re-analyses of photometric (Clementini et al., 2012) and spectroscopic (Kirby et al., 2013, 2008) data confirm the existence of two stellar populations and report metallicities ranging from $[Fe/H] = -2.02 \pm 0.05$ to \approx -1.5. The LBT/LBC data of de Jong et al. (2008) indicates an absolute magnitude of -8.0 mag and a half-light radius of $0.99 \pm 0.06 \operatorname{arcmin} (120 \pm 7 \text{ pc})$, while Muñoz et al. (2018) find -7.60 ± 0.14 mag and 1.27 ± 0.13 arcmin $(154 \pm 16 \text{ pc})$ from new Magellan/Megacam imaging.

Hya II was discovered by Martin et al. (2015) in the Survey of the MAgellanic Stellar History (SMASH; Nidever et al., 2017), consisting of Blanco/DECam imaging. From these data Martin et al. estimate that Hya II is 13 Gyr old, has a metallicity of [Fe/H] = -2.2, has an absolute *V*-band magnitude of -4.8 ± 0.3 mag, has a half-light radius of $1.7^{+0.3}_{-0.2}$ arcmin (68 ± 11 pc), and is located at a distance of 134 ± 10 kpc. Kirby et al. (2015) have obtained Keck/DEIMOS spectroscopy and determined a metallicity of $[Fe/H] = -2.02 \pm 0.08$. The intrinsic velocity dispersion could not be resolved. Vivas et al. (2016) find a distance of 151 ± 8 kpc, based on time series observations of an RR Lyrae star. Muñoz et al. (2018) re-analyse the data of Martin et al. (2015) and find an absolute *V*-band magnitude of -4.60 ± 0.37 mag and a half-light radius of 1.65 ± 0.39 arcmin (64.3 ± 15.2 pc). An analysis of photometry from *HST* by Sacchi et al.

(2021) indicates that Hya II reached half of its cumulative star formation 13.21 ± 0.32 Gyr ago.

Koposov et al. (2015) discovered Gru 1 in public DES data, with an absolute V-band magnitude of -3.4 ± 0.3 mag and a half-light radius of $1.77^{+0.85}_{-0.39}$ arcmin ($62^{+29.8}_{-13.6}$ pc), at a distance of 120 kpc. No H I was detected in its direction (Westmeier et al., 2015). Though the sky position of Gru 1 was not part of the DES Y1A1 catalogue analysed by the DES Collaboration (2015a) simultaneously to and independent of the study of Koposov et al. (2015), its presence was confirmed using data of the DES Y2 catalogue (DES Collaboration, 2015b). Walker et al. (2016) studied Gru 1 with Magellan/M2FS spectroscopy and find a mean line-of-sight velocity of $-140.5^{+2.4}_{-1.6}$ km s⁻¹, but could not resolve the dispersion. In the same study, the metallicity was determined to be $[Fe/H] = -1.42^{+0.55}_{-0.42}$. Muñoz et al. (2018) re-analysed archival DES data and find an absolute V-band magnitude of -3.47 ± 0.59 mag and a half-light radius of 1.50 ± 0.68 arcmin $(52.4 \pm 23.8 \text{ pc})$. Jerjen et al. (2018) find a much more metal-poor result, $[Fe/H] = -2.5 \pm 0.3$, using Gemini/GMOS-S photometry, and find a distance of 115 ± 6 kpc. Ji et al. (2019), on the other hand, find a metallicity of [Fe/H] \approx -2.5 for two stars with high-resolution Magellan/MIKE spectroscopy, and suggest the difference with the result of Walker et al. (2016) is due to the presence of low-signal-to-noise spectra in the original spectroscopic sample. With SOAR/Goodman and Blanco/DECam, the DES Collaboration (2019) find two RLLs in Gru 1, which lead to a distance measurement of 127 ± 6 kpc. Reanalysing DES data, Moskowitz & Walker (2020) find a significantly larger half-light radius of $2.84^{+0.35}_{-0.28}$ arcmin. The DES Collaboration (2021a) performed a deeper photometric study with Magellan/Megacam and find Gru 1 consists of a single stellar population at a distance of 125^{+6}_{-12} kpc, with an age of $13.26^{+0.18}_{-0.25}$ Gyr, a metallicity of [Fe/H] $\approx -1.88^{+0.09}_{-0.03}$, an absolute V-band magnitude of -4.1 ± 0.3 mag, and a half-light radius of $4.16^{+0.54}_{-0.84}$ arcmin $(151^{+21}_{-31} \text{ pc})$.

For consistency, when available and reasonably up-to-date, we adopted the same positions and distances as in the homogeneous study by Muñoz et al. (2018) and the same photometric and structural parameters as they derive. Though Sérsic (1963, 1968) profiles provide the best fits, exponential profiles are consistent and have fewer parameters; therefore we adopt the latter. Ant B, not being a satellite of the Milky Way, was not included in the study of Muñoz et al. (2018). We therefore use the distance of Hargis et al. (2020) and the position, absolute magnitude, and structural parameters of Sand et al. (2015). For Hya II, we found that the distance assumed by Muñoz et al. (2018) leads to isochrones that do not fit the horizontal branch. The other distance determination, from Vivas et al. (2016), did fit.

References		1, 2	3, 4, 5	3, 6	7	
$m_V - M_V$	(mag)	25.65			20.48	
0' <i>A</i> M	$(magarcsec^{-2})$		25.42	26.14		
M_V	(mag)	-9.7	-7.60	$-4.86^{(a)}$	-4.1	
$R_{1/2}$	(arcmin)	0.72	1.27	1.65	4.16	
ω		0.30	0.24	0.25	0.44	
θ	(deg)	+4.0	-104	+13	+153	
D	(kpc)	1.35×10^{3}	417.0	151	125	
Dec.	(deg)	-25.9900	+17.0482	-31.9860	-50.168	
RA	(deg)	147.2337	143.7292	185.4251	344.166	
		Ant B	Leo T	Hya II	Gru 1	

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NOTES: RA: central right ascension; Dec.: central declination; D: heliocentric distance; θ : position angle; ε : ellipticity; $R_{1/2}$: angular half-light radius; M_V : absolute V-band magnitude; $\mu_{V,0}$: central V-band surface brightness; $m_V - M_V$: V-band distance modulus. ^(a) Adjusted for the difference in adopted distance.

REFERENCES: (1) Sand et al. (2015); (2) Hargis et al. (2020); (3) Muñoz et al. (2018); (4) Irwin et al. (2007); (5) Simon & Geha (2007); (6) Vivas et al. (2016); (7) DES Collaboration (2021a). Though we retain the angular structural parameters and surface brightness from Muñoz et al. (2018), we adjust their absolute magnitude in accordance with the change in distance. Lastly, a recent, deeper study of Gru 1 (DES Collaboration, 2021a) revealed a substantially larger half-light radius and brighter magnitude, therefore we adopt the parameters found in this study. We display the list of adopted parameters in Table 4.1.

4.2.2 Overview of observations and data reduction

In addition to 21.5 h of data in five fields towards Eri 2, reduced and presented in Paper I and Paper II, in this paper we used 4.5 h on Ant B (one field), 4 h on Leo T (one field), 14.75 h on Hya II (four fields), and 4 h on Gru 1 (one field) from the MUSE-Faint survey. These data were taken between February 2018 and February 2020 during MUSE Collaboration guaranteed-time observing runs. The natural seeing varied between 0.6 and 1.2 arcsec, with median values between 0.7 and 0.9 arcsec for each dwarf galaxy. The adaptive-optics system indicated corrected median seeings between 0.5 and 0.6 arcsec. After the data reduction we measured full widths at half-maximum of 0.55, 0.61, 0.40, and 0.67 arcsec for Ant B, Leo T, Hya II, and Gru 1, respectively, at 7000, by fitting a Moffat function to the point spread functions of the brightest stars.

We used the same data reduction procedure as for Eri 2 in Paper I and Paper II, which we summarize here for convenience. We used the standard procedure for MUSE data reduction using the MUSE Data Reduction Software (DRS; version 2.6; Weilbacher et al., 2020), supplemented with a bad-pixel table from Bacon et al. (2017) and an auto-calibration step, when possible. The field of Ant B was too crowded, therefore the auto-calibration was skipped for this target. Contrary to the reduction for Eri 2, it was not necessary to build a source mask from a source catalogue during the autocalibration of Leo T, Hya II, and Gru 1. Instead we relied on the automatic masking based on pixel brightness. These same three galaxies were reduced with an updated overscan setting that became the default in DRS version 2.8 (Weilbacher et al., 2020) after this was found to improve the reduction quality of the MUSE Extremely Deep Field (MXDF; Bacon et al. in prep.). For Leo T a satellite trail had to be masked as well. The data cubes reduced with the DRS were post-processed with the Zurich Atmosphere Purge (ZAP; version 2.0; Soto et al., 2016) to remove residual sky signatures. Compositecolour images of the post-processed cubes created with fits2comp¹ using the method of Lupton et al. (2004), using SDSS filters g, r, and i for blue, green, and red, respectively, are shown in Fig. 4.1. Spectral extraction was

^{1.} https://github.com/slzoutendijk/fits2comp



FIGURE 4.1: Composite-colour images of the targeted galaxies based on data from the MUSE-Faint survey. The SDSS filters g, r, and i were used to create the blue, green, and red channels, respectively, of the images. Stars identified in this paper as members of these galaxies that are located within the bounds of these MUSE-Faint images are indicated with yellow circles. The angular and physical scales of the images are indicated at their lower left corners. The directions north and east are indicated in the lower right corners of the images.

performed with PampelMuse (version 1.orc2; Kamann et al., 2013) using source catalogues produced from public *Hubble Space Telescope* (*HST*) data (see Sects. 4.2.3–4.2.6). In the case of Hya II, the source catalogue included a number of spurious detections around a bright star; these we removed manually from the catalogue. The extracted spectra were then fit with spexxy (version 2.5; Husser, 2012) in combination with the PHOENIX synthetic stellar spectral library, resulting in line-of-sight velocities.

We used publicly available HST photometry in the F606W and F814W bands, which we analysed with SExtractor (Bertin & Arnouts, 1996) to construct colour-magnitude diagrams for each dwarf galaxy. We compared the HST photometry to PARSEC (Bressan et al., 2012; Chen et al., 2015, 2014; Marigo et al., 2017; Pastorelli et al., 2019, 2020; Tang et al., 2014) isochrones, assuming a Kroupa IMF (Kroupa, 2001, 2002; Kroupa et al., 2013) corrected for unresolved binaries. We converted the isochrones from Vega to AB magnitudes using the solar magnitudes of Willmer (2018) and applied Galactic dust extinction (Schlegel et al., 1998; Schlafly & Finkbeiner, 2011 recalibration). We used metallicity, age, and distance measurements from the literature as starting points to select one or more isochrones. As the goal here was to determine source membership and not a detailed starformation history, we did not fine tune the isochrone parameters but accepted a combination that gave a good match by eye to the colour-magnitude diagram. To determine which stars are photometrically consistent with membership, we adopted an uncertainty of 0.1 mag on the colour values of the isochrone. This is to compensate for the coarse isochrone parameter selection, the discontinuous nature of the isochrone samples, the possibility of variations in stellar parameters (e.g. metallicity dispersion), and any error in the theoretical isochrones. We combined this uncertainty with the stellar measurement uncertainties on both colours, and rejected stars offset more than two combined standard deviations from the isochrone. From the fitted isochrone and the accompanying PARSEC simple stellar population simulation, we calculated a stellar mass-to-light ratio for each dwarf galaxy by adding stellar remnant masses to the active stellar masses using the recipes from Renzini & Ciotti (1993).

We queried the astrometry and kinematics of sources in *Gaia* Early Data Release 3 (EDR3; Gaia Collaboration, 2016, 2021; Lindegren et al., 2021) within a radius from the centre of each dwarf galaxy sufficiently large to encapsulate the sky coverage of both the MUSE and the *HST* observations. We considered a given parallax measurement reliable if it is positive and if the renormalized unit-weight error (RUWE) is less than 1.4 (Lindegren, 2018). If a source had a reliable parallax measurement that was inconsistent with zero at a level of at least 2σ , we rejected the source. When available, we used *Gaia* line-of-sight velocity measurements carried

4 No large cores & no significant stripping

over from Data Release 2; however, no sources with *Gaia* line-of-sight velocities made it into the final source selections.

Not all spectra extracted with PampelMuse have a converged spexxy fit, which naturally limits the number of sources we can include in our sample. Below a signal-to-noise ratio (S/N) of 5, spexxy may incorrectly estimate uncertainties (Kamann et al., 2018), which would influence the intrinsic velocity dispersion estimate. However, the faintness of these galaxies makes it challenging to assemble a large enough sample of sources to trace the density profile. We have therefore relaxed the S/N criterion to 3 in the three faintest galaxies Leo T, Hya II, and Gru 1. To safeguard ourselves from introducing a bias into the kinematics in this way, we have confirmed that the bulk intrinsic velocity and bulk intrinsic velocity dispersion are consistent at both S/N criteria.

When available, we added line-of-sight velocity measurements from the literature to our sample. These generally come from high-resolution spectroscopic measurements, which typically have smaller velocity uncertainties, but the lower spatial resolution of these instruments introduces a lack of measurements in the dense centres of faint dwarf galaxies; a lack we can address with the higher spatial resolution and smaller field of view of MUSE.

We matched the celestial positions of entries in the *HST* F814W, *Gaia* EDR3, and any high-resolution spectroscopy catalogues using TOPCAT (Taylor, 2005). We remind the reader that the spexxy velocities are already linked to the *HST* positions through the use of the *HST* catalogue in the extraction of spectra with PampelMuse. We calibrated the positions of *HST* and high-resolution spectroscopy entries to *Gaia* EDR3 using the sources in common. We then built a unified catalogue of positions and velocities: We used the *Gaia* EDR3 position if available for a source, otherwise we take the average of any other (*Gaia*-calibrated) positions available. We combined velocity measurements by taking the average weighted by the inverse variance and propagated the measurement uncertainties accordingly. To filter out galaxies, we reject sources for which SExtractor determined CLASS_STAR < 0.8 in both the F606W and the F814W *HST* data. The remaining sources we considered stars. We removed foreground stars using our parallax criterion and applied the isochrone criterion.

Finally, we used the following procedure to identify kinematic outliers: We modelled the distribution underlying the velocity measurements v_i and their uncertainties ε_i as a normal distribution of member stars, with mean μ and intrinsic dispersion σ , and a uniform distribution of contaminants within the velocity range considered taking up a fraction η of the sample. The likelihood that the measurements are generated by this model with a particular combination of parameters is

TABLE 4.2: Derived properties of the stellar populations and the kinematic samples.

-	$\log_{10}(M_*/M_{\odot})$	$N_{ m mem}^{ m MUSE}$	$N_{ m mem}^{ m tot}$	μ	$\sigma_{ m int}$
				$({\rm km}{\rm s}^{-1})$	$({\rm km}{\rm s}^{-1})$
Ant B	5.88	127	127	375.5 ± 1.5	$8.0^{+1.6}_{-1.4}$
Leo T	5.16	55	75	39.5 ± 2.1	$7.6^{+2.3}_{-1.7}$
Нуа 11	4.30	15	28	$299.5_{-4.7}^{+4.5}$	$12.0^{+5.0}_{-3.5}$
Gru 1	2.80	4	14	$-139.2^{+6.1}_{-5.2}$	$10.4^{+9.3}_{-5.1}$

NOTES: M_* : stellar mass; $N_{\text{mem}}^{\text{MUSE}}$: number of member stars in the sample with a MUSE-Faint velocity measurement; $N_{\text{mem}}^{\text{tot}}$: total number of member stars in the sample; μ : mean velocity; σ_{int} : intrinsic velocity dispersion.

$$\mathcal{L}(\mu,\sigma,\eta|v_i,\varepsilon_i) = \prod_i \left(\frac{1-\eta}{\sqrt{2\pi(\sigma^2+\varepsilon_i^2)}}\exp\left(-\frac{(v_i-\mu)^2}{2(\sigma^2+\varepsilon_i^2)}\right) + \frac{\eta}{\max(v_i)-\min(v_i)}\right), \quad (4.1)$$

We used emcee (Foreman-Mackey et al., 2013) to find the posterior distributions of μ , σ , and η . We assumed uniform priors of $\min(v_i)$ to $\max(v_i)$ for μ , 0 to 50 km s⁻¹ for σ , and 0 to 1 for η . For the median values $\hat{\mu}$ and $\hat{\sigma}$ of the posteriors of μ and σ , respectively, we calculated the membership likelihood of each star:

$$\mathcal{L}_{\text{mem}}(v_i, \varepsilon_i | \hat{\mu}, \hat{\sigma}) = \frac{1}{\sqrt{2\pi(\hat{\sigma}^2 + \varepsilon_i^2)}} \exp\left(-\frac{(v_i - \hat{\mu})^2}{2(\hat{\sigma}^2 + \varepsilon_i^2)}\right).$$
(4.2)

When ordered according to decreasing membership likelihood, we found that the membership likelihoods gradually decrease down to a certain point after which the membership likelihoods of remaining stars rapidly decrease. This break was usually located at a likelihood value between the equivalent of a 2σ and a 5σ outlier of a normal distribution with standard deviation σ . These breaks in the membership likelihood distributions seemed an appropriate choice to divide the stars into members and non-members. We also compared the membership likelihoods against the expected values for normally distributed measurements, using a quantile– quantile plot, to ensure that the proposed selection of members and non-members would not overly curtail the distribution. After finalizing the selection, we removed the non-members. The kinematic selection procedure was repeated on the remaining stars until we found no more non-members. Finally, we set $\eta = 0$ and ran emcee once again. We compared the resulting intrinsic distribution to the one reported in the literature, if available (see Sects. 4.2.3–4.2.6).

In the following sections we discuss the sample selection procedure for each galaxy. We provide a summary of the derived sample and stellar properties in Table 4.2.

4.2.3 Antlia B

Júlio et al. (in prep.) describe the sample of selected member stars in Ant B. For the sake of completeness, we summarize the procedure here. An extraction catalogue was created by running SExtractor on publicly available HST/ACS photometry². Using this catalogue, 141 spectra with a S/N of >5 were extracted from the MUSE-Faint data and 131 of these were successfully fitted. A visual inspection of the *HST* photometry and the extracted spectra revealed no galaxies. The extracted stars had a very clean velocity distribution, with four clear outliers more than twice the standard deviation away from the mean. This lead to a sample of 127 stars. The Ant B colourmagnitude diagram shows a very clear separation between photometrically consistent and inconsistent stars; we could verify by eye that no photometric outliers were present in this sample.

Out to a radius of 5 arcmin from the centre of Ant B, we found 305 *Gaia* EDR3 sources. Seven sources had a DR2 line-of-sight velocity, of which six also had a good RUWE. These six were however all foreground stars, leaving our sample at 127 sources.

Though a kinematic cut was already made, we applied our kinematic outlier procedure to test for remaining contaminants. We did not find any additional outliers. We also inspected the CLASS_STAR values returned by SExtractor as an extra precaution, but found no additional galaxies in the sample. The intrinsic mean line-of-sight velocity of the final sample is $375.5 \pm 1.5 \text{ km s}^{-1}$, with an intrinsic dispersion of $8.0^{+1.6}_{-1.4} \text{ km s}^{-1}$.

Ant B reached half its present cumulative star formation ≈ 6 Gyr ago (Hargis et al., 2020). For the purpose of obtaining stellar mass-to-light ratios, we fitted a PARSEC isochrone with distance D = 1.35 Mpc, age t = 6.0 Gyr, and metallicity [M/H] = -2.0. This isochrone led to a stellar mass-to-light ratio of 1.19. Adopting an absolute magnitude $M_V = -9.7$ mag, the resulting stellar mass is $M_* = 10^{5.88} M_{\odot} = 7.59 \times 10^5 M_{\odot}$.

4.2.4 Leo T

The selection of member stars in Leo T is described in more detail by Vaz

^{2.} Hubble Space Telescope Proposal 14078, principal investigator Jonathan Hargis.

et al. (in prep.), but we summarize it here for completeness. With spexxy we were able to fit 130 out of the 252 extracted spectra with a line-of-sight velocity. For Leo T a S/N criterion of >3 was used, which yielded 56 sources. Three emission-line stars were found, the spectra of which spexxy was not able to fit due to the absence of a suitable template in PHOENIX; for these three stars a velocity was determined using ULySS (Koleva et al., 2009) with the MIUSCAT library (Ricciardelli et al., 2012; Vazdekis et al., 2012). Iso-chrones of various ages, reflecting the extended star-formation history of Leo T (Weisz et al., 2012), were fitted to the colour-magitude diagram of public³ *HST*/ACS data, adopting a distance D = 417 kpc and a metallicity [M/H] = -1.6. One of the 59 sources was inconsistent with the isochrones and was removed. The 19 member stars of Simon & Geha (2007) were added to the MUSE-Faint sample. Two stars were in common between Simon & Geha (2007) and the MUSE-Faint observations. No kinematic outliers were found in this sample of 75 stars by Vaz et al. (in prep.).

For consistency with the analysis used on other sources in this paper, we additionally queried *Gaia* EDR3 and found 110 sources, of which three had a DR2 velocity measurement, two of which with a good RUWE. These, however, were foreground sources according to their parallax measurements. Our other selection criteria did not reveal additional interlopers. We therefore arrived at the same sample of 75 stars as Vaz et al. (in prep.). Of these stars, 55 have a velocity measurement from MUSE-Faint. We measured an intrinsic mean line-of-sight velocity of $39.5 \pm 2.1 \text{ km s}^{-1}$ and an intrinsic line-of-sight velocity dispersion of $7.6^{+2.3}_{-1.7} \text{ km s}^{-1}$. The inferred kinematics in the final sample did not significantly differ when we tested with a S/N criterion of >5, but this would have resulted in 14 fewer stars; therefore we found the lower S/N cut to be justified.

Considering half of the stellar mass of Leo T was assembled 7.6 Gyr ago (Weisz et al., 2012), we use this age and [M/H] = -1.7 to derive a stellar mass-to-light ratio of 1.57. This resulted in a stellar mass of $M_* = 10^{5.16} M_{\odot} = 1.44 \times 10^5 M_{\odot}$, somewhat larger than the $1.05^{+0.27}_{-0.23} \times 10^5 M_{\odot}$ found by Weisz et al. (2012).

4.2.5 Hydra II

We used publicly available HST/ACS photometry⁴ to construct a colourmagnitude diagram for Hya II. We compared the HST photometry to PAR-SEC isochrones. We assumed an age of t = 13.2 Gyr based on the star-

^{3.} *Hubble Space Telescope* Proposals 12914, pincipal investigator Tuan Do, and 14224, principal investigator Carme Gallart.

^{4.} Hubble Space Telescope Proposal 14734, principal investigator Nitya Kallivayalil.

formation history. We tried metallicities of [M/H] = -2.2 and -2.0 at both distance measurements, and found the combination of metallicity [M/H] = -2.2 and distance D = 151 kpc fits the horizontal branch the best. From the fitted isochrone, we obtained a stellar mass-to-light ratio of 2.70. Combined with the luminosity, we calculated a stellar mass of $M_* = 10^{4.30} M_{\odot} = 2.00 \times 10^4 M_{\odot}$.

Out of 132 extracted spectra, spexxy was able to converge to a spectral fit for 80 sources. Of the extracted spectra, 79 had a S/N of at least 3, and 48 of these also had a converged spexxy fit.

Through the Keck/DEIMOS spectroscopy of Kirby et al. (2015), we have access to an additional 31 measurements of line-of-sight velocities in the direction of Hya II. Of these sources, 13 are considered members by Kirby et al. (2015). We included all 31 measurements in our preliminary sample to have a unified selection procedure.

We queried the astrometry and kinematics of sources in *Gaia* EDR3 within 5 arcmin from the centre of Hya II. Six of the 1076 sources in the queried catalogue had DR2 line-of-sight velocities, of which five had a RUWE of less than 1.4. We added these five measurements to our preliminary selection.

Out of 84 velocity measurements, we built a catalogue of 81 unique sources with a (combined) velocity measurement. Nine sources were not sufficiently star-like according to SExtractor, the remaining 72 sources we considered stars. We removed foreground stars using our parallax criterion and found 59 possibly distant stars. Of these stars, 46 were consistent with the isochrone criterion.

After removing kinematic outliers, we obtained a final selection of 28 stars with a mean line-of-sight velocity of $299.5^{+4.5}_{-4.7}$ km s⁻¹ and an intrinsic dispersion of $12.0^{+5.0}_{-3.5}$ km s⁻¹. Out of this sample, 15 stars have a velocity measurement from MUSE-Faint. We confirmed that a S/N criterion of >5 yielded consistent kinematics. The dispersion is over two standard deviations higher than the Kirby et al. (2015) 95% upper limit of 4.5 km s⁻¹, but we find no further kinematic outliers, and the posterior distribution is well-shaped. There is no obvious cause of this discrepancy, though Kirby et al. (2015) note that their upper limit is sensitive to the in- or exclusion of two less likely member stars.

4.2.6 Grus 1

Using publicly available *HST*/ACS photometry⁵ of Gru 1, we constructed a colour–magnitude diagram. Guided by the literature reviewed in

^{5.} Hubble Space Telescope Proposal 14734, principal investigator Nitya Kallivayalil.

Sect. 4.2.1, we found a good match by eye using PARSEC isochrones with age t = 13.5 Gyr, metallicity [M/H] = -1.9, and distance D = 120 kpc. The adopted parameters correspond to a stellar mass-to-light ratio of 1.72. This resulted in a stellar mass of $M_* = 10^{3.80} M_{\odot} = 6.31 \times 10^3 M_{\odot}$.

We extracted 309 spectra, of which we successfully fitted 194 with spexxy. Only 11 extracted sources had a S/N of at least 5, and only seven of these had a velocity fit. When we relaxed the S/N criterion to >3, we had 28 extracted spectra, with 18 velocities. Given the low number of sources even before considering membership, we chose to use a S/N cut of >3. We repeated the selection with a cut of >5 as well and found no significant difference in the inferred bulk dynamics.

We supplemented our sample with that of Walker et al. (2016), which consists of 133 sources in the direction of Gru 1, though only seven are considered members. We limited the Walker et al. (2016) sample to 64 sources with a velocity error $\leq 20 \text{ km s}^{-1}$ to avoid poor-quality velocity measurements. For the sake of a uniform selection procedure, we did not adopt the membership probabilities determined by Walker et al. (2016), but performed our own membership analysis. We further added the two velocity measurements of Ji et al. (2019), whose sources are also included in the Walker et al. (2016) sample.

We queried *Gaia* EDR3 in a radius of 20 arcmin around the position of Gru 1 and found 1733 sources. There were 15 sources with a DR2 velocity measurement, of which 13 had a good RUWE. These 13 sources were added to our sample, though we remind the reader that for none of our galaxies did a source with a *Gaia* velocity end up in our final selection of member stars.

Our preliminary sample consisted of 97 velocity measurements of 95 sources. Consecutively applying membership criteria, we found 86 sources were stars, of which 58 were not nearby, of which 54 matched to the PARSEC isochrone.

This sample was still heavily contaminated with kinematic outliers. We applied our iterative kinematic member selection and arrived at a final sample of 14 members. There are four stars in this sample with a velocity measurement from MUSE-Faint. This sample includes the seven members of Walker et al. (2016), but also three stars that Walker et al. (2016) did not consider members. We find this sample has a mean line-of-sight velocity of $-139.2_{-5.2}^{+6.1}$ km s⁻¹ and a velocity dispersion of $10.4_{-5.1}^{+9.3}$ km s⁻¹. The velocity dispersion is marginally resolved and is about one standard deviation away from the median of the unresolved posterior of Walker et al. (2016). The dispersion measurement supports the classification of Gru 1 as a galaxy.

4.3 Methods

In Paper II we used two dynamical modelling tools, CJAM (Watkins et al., 2013) and pyGravSphere (Genina et al., 2020; Read & Steger, 2017) in combination with hkbin⁶ (Paper II), which is an alternative velocity binning algorithm based on that of pyGravSphere, in our analysis of the dark-matter profiles. We found consistent results between the two tools for our galaxy Eri 2. In this paper, we use CJAM together with the updated GravSphere⁷ (Collins et al., 2021; Genina et al., 2020; Read & Steger, 2017; Read et al., 2018), which we describe in Sects. 4.3.1 and 4.3.2, respectively. When the two tools are in agreement, we show the results from one of the tools in the main body of this paper and the results from the other in Appendix 4.A, whereas in the case of disagreement, we present the results of both in the main body of the paper, without declaring a preference. We choose CJAM as our fiducial tool in case of agreement, because its simpler implementation of a fully cored profile allows us to address our hypothesis about the cuspiness of UFDs, while we have too few measurements to constrain the more complex implementation of cores in GravSphere, which allows partial core formation.

4.3.1 CJAM

In our CJAM analysis we used three density profile models from Paper II. The diversity of profile shapes between the three models makes them wellsuited to explore the properties of individual galaxies. This choice of models has the additional advantages of enabling the joint analysis of darkmatter properties using multiple galaxies in future work, and of already having been implemented. We will be brief in the description of these profiles and refer the reader to Paper II for details on the associated darkmatter physics.

Firstly, we use the cuspy Navarro–Frenk–White (NFW; Navarro et al., 1996b) profile, determined by a characteristic density ρ_0 and a scale radius r_s :

$$\rho_{\rm cusp}(r;\rho_0,r_{\rm s}) = \frac{\rho_0}{(r/r_{\rm s})(1+r/r_{\rm s})^2} \tag{4.3}$$

This profile is divergent ($\rho_{cusp} \propto r^{-1}$) at small radii r and transitions to a steeper slope ($\rho_{cusp} \propto r^{-3}$) at radii larger than r_s . The NFW profile is found in simulations of cold dark matter without baryonic interactions, but is

^{6.} https://github.com/slzoutendijk/hkbin

^{7.} https://github.com/justinread/gravsphere

also expected for UFDs due to their scarcity of baryons (Oñorbe et al., 2015; Peñarrubia et al., 2012; Wheeler et al., 2019).

An alternative to cuspy profiles are cored profiles. Here we use the profile of Lin & Loeb (2016):

$$\rho_{\rm core}(r;\rho_0,r_{\rm s},r_{\rm c}) = \frac{\rho_0}{r_{\rm c}/r_{\rm s} + (r/r_{\rm s})(1+r/r_{\rm s})^2}.$$
(4.4)

This model introduces a core radius r_c ; at radii much smaller than this scale, the profile becomes flat ($\rho_{core} \propto r^0$). At larger radii the profile behaves like the NFW profile, and if $r_c = 0$ the two are identical at every radius. Though this profile is designed to describe self-interacting dark matter, it is flexible enough to fit to other core-producing mechanisms, such as baryonic feedback (Brooks & Zolotov, 2014; Di Cintio et al., 2014b).

As our final model, we have a profile that is steeper than the NFW profile at intermediate radii. This profile, derived for fuzzy dark matter, is parametrized by Marsh & Pop (2015) as

$$\rho_{\rm sol}(r;\rho_{\rm sol,0},r_{\rm sol},\rho_{\rm cusp,0},r_{\rm s}) = \begin{cases} \frac{\rho_{\rm sol,0}}{(1+(r/r_{\rm sol})^2)^8}, & (r < r_{\rm t}), \\ \frac{\rho_{\rm cusp,0}}{(r/r_{\rm s})(1+r/r_{\rm s})^2}, & (r \ge r_{\rm t}). \end{cases}$$
(4.5)

This is identical to the NFW profile at radii larger than the transition radius r_t , but then steeply rises (up to $\rho_{sol} \propto r^{-16}$) until becoming flat at the centre. The inner part deviating from the NFW profile is known as the soliton.

Though a full explanation of our CJAM modelling and the implementation of our density profiles is given in Paper II, we recapitulate here. Given a density profile, characterized by parameters θ and modelled with a multi-Gaussian expansion (MGE; Emsellem et al., 1994), CJAM calculates expected line-of-sight velocity dispersion $\sigma_i(\theta)$ at the projected radius of each tracer i (i.e. each star). It is then up to the user to implement a strategy to find the best model and the uncertainties thereon. We make use of Equations (7), (9), (11), and (15) provided by Graham & Driver (2005) and the absolute solar magnitude $M_{V,\Omega}$ = 4.81 of Willmer (2018) to transform the adopted magnitudes and central surface brightness parameters in Table 4.1 to the surface brightness at the half-light radius that is required by CJAM. We construct an axisymmetric luminosity profile with the adopted position angles and ellipticities, and the assumption that the system is seen edge-on. To avoid the model from becoming computationally too expensive, we assume an isotropic velocity distribution and a spherical dark-matter halo. We shall see later that GravSphere, which does not assume isotropy, indicates that anisotropy has no significant influence on our results.

The likelihood that a model with profile parameters θ and systemic lineof-sight velocity v_0 describes the observed velocities v_i and their measurement uncertainties ε_i , is

$$\mathcal{L}(\theta, v_0 | v_i, \varepsilon_i) = \prod_i \frac{1}{\sqrt{2\pi \left(\sigma_i^2(\theta) + \varepsilon_i^2\right)}} \exp\left(-\frac{(v_i - v_0)^2}{2(\sigma_i^2(\theta) + \varepsilon_i^2)}\right).$$
(4.6)

The model is varied by sampling different model parameters θ and v_0 . Using MultiNest (Feroz & Hobson, 2008; Feroz et al., 2009, 2019) through the pyMultiNest (Buchner et al., 2014) interface, the parameters are constrained. MultiNest calculates the Bayesian evidence for each model, with which the models can be compared.

We found that a parametrization of the cored profile in the densities $\rho_1 = \rho(50 \text{ pc})$, $\rho_2 = \rho(100 \text{ pc})$, and $\rho_3 = \rho(150 \text{ pc})$ gives the best constraints on the posterior distribution. These three radii were chosen because the greatest density of tracers is found within this radial range. As the cuspy profile is a special case of the cored profile with $r_c = 0$, for this model we parametrize only with ρ_2 and ρ_3 . The soliton profile we parametrize with the value $\rho_{\text{cusp},100} = \rho_{\text{cusp}}(100 \text{ pc})$ of the outer (cuspy) density profile at 100 pc, the logarithmic slope $\alpha_{\text{cusp},100} \coloneqq (d \ln \rho_{\text{cusp}}/d \ln r)(100 \text{ pc})$ of the outer density profile at 100 pc, the ratio $r_{\text{sol}}/r_{\text{s}}$ between soliton and scale radius, and the ratio $\varepsilon = \rho_{\text{sol}}(r_t)/\rho_{\text{sol},0}$ between the density at the transition radius and at the centre.

We used the same priors as in Paper II, indicated in Table 4.3. Additionally, as in Paper II⁸, the following conditions were imposed to ensure physically plausible profiles with a well-fit MGE: $r_c \le r_s$ and 1.5 pc $\le r_s \le$ 50 kpc.

4.3.2 GravSphere

In our GravSphere (Collins et al., 2021; Genina et al., 2020; Read & Steger, 2017; Read et al., 2018) analysis we use two profile models. The first is a cuspy model using the same NFW profile as CJAM. However, GravSphere parametrizes this profile with the virial mass M_{200} and concentration c_{200} . These are related to the conventional ρ_0 and r_s through

$$\rho_0 = \frac{200\rho_{\rm crit}c_{200}^3}{3\left(\ln(1+c_{200}) - c_{200}/(1+c_{200})\right)},\tag{4.7}$$

$$r_{\rm s} = r_{200}/c_{200},\tag{4.8}$$

^{8.} Paper II describes these conditions incorrectly. The conditions given in that paper should read identical to those given here.

TABLE 4.3: Priors on parameters explored with MultiNest.

Prior	Min.	Max.	Profiles
$\log_{10}(\rho_1/M_{\odot}{\rm kpc}^{-3})^{(a)}$	6	12	core
$\log_{10}(\rho_2/M_{\odot} \mathrm{kpc^{-3}})^{(a)}$	6	12	cusp, core
$\log_{10}(\rho_3/M_{\odot}{\rm kpc^{-3}})^{(a)}$	6	12	cusp, core
$\log_{10}(\rho_{\rm cusp,100}/M_{\odot}{\rm kpc^{-3}})$	6	10	sol.
$\alpha_{\rm cusp,100}$	-3	-1	sol.
$\log_{10}(r_{\rm sol}/r_{\rm s})$	-3	0	sol.
$\log_{10} \varepsilon$	-5	log ₁₀ 1/2	sol.
$v_0/{\rm km}{\rm s}^{-1}$ (Ant B)	365	385	cusp, core, sol.
$v_0 / \text{km s}^{-1}$ (Leo T)	25	45	cusp, core, sol.
$v_0 / \text{km s}^{-1}$ (Hya II)	280	330	cusp, core, sol.
$v_0/{\rm kms^{-1}}({\rm Gru1})$	-165	-115	cusp, core, sol.

NOTES: All priors are uniform between the indicated minima and maxima and apply to the indicated profiles: core, cusp, or soliton. ρ_1 , ρ_2 , ρ_3 : dark-matter density at 50, 100, and 150 pc from the centre, respectively; $\rho_{\text{cusp},100}$: density of the large-scale, cusp-like component of the soliton profile, measured at 100 pc; $\alpha_{\text{cusp},100}$: power-law slope of the large-scale, cusp-like component of the soliton profile, measured at 100 pc; $r_{\text{sol}}/r_{\text{s}}$: ratio of the soliton radius to the scale radius of the large-scale, cusp-like component of the soliton profile; ε : fraction of the dark-matter density at the soliton profile's transition radius versus the central density; v_0 : systemic velocity. ^(a) Within the indicated priors, $\rho_i \ge \rho_{i+1}$.

where

$$r_{200} = \left(\frac{3M_{200}}{800\pi\rho_{\rm crit}}\right)^{1/3} \tag{4.9}$$

and $\rho_{\rm crit}$ is the critical density of the Universe.

The second profile model we will refer to as core+tides, as it modifies the cusp model by allowing for a (partial) central core and a lowering of the density beyond a tidal radius. This is described by the coreNFwtides profile (Read et al., 2016, 2018). Within the tidal radius r_t , this profile redistributes of mass from the central cusp to larger radii, as is expected to take place during core formation due to star-formation feedback:

$$M_{\rm cNFW}(< r) = M_{\rm NFW}(< r) f^n, \qquad (4.10)$$

with

$$f^{n} = \left(\tanh(r/r_{\rm c}) \right)^{n}, \tag{4.11}$$

where r_c is the core radius and $0 \le n \le 1$ the completeness of core formation. In terms of density, this is

$$\rho_{\rm cNFW}(r) = f^n \rho_{\rm NFW}(r) + \frac{n f^{n-1} \left(1 - f^2\right)}{4\pi r^2 r_{\rm c}} M_{\rm NFW}(< r), \qquad (4.12)$$

where

$$M_{\rm NFW}(< r) = \frac{M_{200} \left(\ln(1 + r/r_{\rm s}) - (r/r_{\rm s})(1 + r/r_{\rm s})^{-1} \right)}{\ln(1 + c_{200}) - c_{200}/(1 + c_{200})}$$
(4.13)

is the NFW cumulative mass profile. Outside of r_t , the density profile is changed into a power law with negative slope $\delta \ge 3$:

$$\rho_{\rm cNFWt}(r) = \rho_{\rm cNFW}(r_{\rm t}) (r/r_{\rm t})^{-\delta}.$$
(4.14)

The complete coreNFwtides mass profile is then

$$M_{\rm cNFWt}(< r) = \begin{cases} M_{\rm cNFW}(< r), & r < r_{\rm t}, \\ M_{\rm cNFW}(< r_{\rm t}) + & \\ 4\pi\rho_{\rm cNFW}(r_{\rm t})\frac{r_{\rm t}^3}{3-\delta} ((r/r_{\rm t})^{3-\delta} - 1), & r > r_{\rm t}. \end{cases}$$
(4.15)

Because the coreNFWtides profile is parametrized with the virial parameters of its progenitor NFW profile, we will refer to these parameters as M_{200}^{prog} and c_{200}^{prog} when discussing the core+tides model, to avoid confusion with the actual M_{200} and c_{200} of the present-day profile.

Unlike for our CJAM modelling, where we have assumed an isotropic velocity distribution, our GravSphere modelling uses a Baes & Van Hese (2007) velocity anisotropy profile,

$$\beta(r) = \beta_0 + (\beta_\infty - \beta_0) \frac{1}{1 + (r_0/r)^{\eta}}.$$
(4.16)

GravSphere uses a symmetrized anisotropy,

$$\tilde{\beta} = \frac{\beta}{2-\beta},\tag{4.17}$$

and equivalently $\beta_0 \to \tilde{\beta}_0$ and $\beta_\infty \to \tilde{\beta}_\infty$, to avoid infinities. The velocity anisotropy is fully tangential for $\tilde{\beta} = -1$ and fully radial for $\tilde{\beta} = +1$, while $\tilde{\beta} = 0$ means isotropy.

GravSphere uses binning to compare the velocity moments of the profiles with the measurements. This binning is done through an algorithm called the binulator. The intrinsic velocity distribution function is modelled with a generalized Gaussian. The mean line-of-sight velocity μ_v , intrinsic line-of-sight dispersion σ_{los} , and kurtosis κ are optimized to fit the generalized Gaussian probability density function to the velocity measureTABLE 4.4: Priors on parameters explored by GravSphere with emcee.

Prior	Min.	Max.	Profiles
$\log_{10}(M_{200}/M_{\odot})$	7.5	11.5	cusp
$\log_{10}(M_{200}^{\rm prog}/M_{\odot})$	7.5	11.5	core+tides
c ₂₀₀	1.0	50.0	cusp
c_{200}^{prog}	1.0	50.0	core+tides
$\log_{10}(r_{\rm c}/{\rm kpc})$	-3	1	core+tides
n	0	1	core+tides
$\log_{10}(r_{\rm t}/{\rm kpc})$	0	$\log_{10}(20)$	core+tides
δ	3.01	5.0	core+tides
$ ilde{eta}_{0}$	-1	1	cusp, core+tides
$ ilde{eta}_{\infty}$	-1	1	cusp, core+tides
$\log_{10}(r_0/\text{kpc})$	-0.9	0	cusp, core+tides
η	1.0	3.0	cusp, core+tides
$M_*/M_{*,\mathrm{nom}}$	0.75	1.25	cusp, core+tides
$M_i/M_{i,\rm best}$	0.9	1.1	cusp, core+tides
$a_i/a_{i,\text{best}}$	0.9	1.1	cusp, core+tides

NOTES: All priors are uniform between the indicated minima and maxima and apply to the indicated profiles. M_{200} : virial mass of the cusp model; M_{200}^{prog} : virial mass of the cuspy progenitor to the core+tides model; c_{200} : concentration of the cusp model; c_{200}^{prog} : concentration of the cusp progentor to the core+tides model; r_c : core radius; n: coredness parameter; r_t : tidal radius; δ : negative logarithmic density slope beyond r_t ; $\tilde{\beta}_0$: inner symmetrized ansisotropy; $\tilde{\beta}_{\infty}$: outer symmetrized anisotropy; r_0 : anisotropy transition radius; η : anisotropy transition rapidity; $M_*/M_{*,\text{nom}}$: stellar mass, relative to the nominal stellar mass from Table 4.2; $M_i/M_{i,\text{best}}$: surface-brightness profile multi-Plummer amplitude parameters, relative to the best-fit values; $a_i/a_{i,\text{best}}$: surface brightness profile multi-Plummer scale parameters, relative to the best-fit values.

ments in each bin, taking into account the observational broadening by the measurement uncertainties. To break the degeneracy between density and velocity anisotropy, two virial shape parameters (Merrifield & Kent, 1990) are then calculated from the fourth velocity moments $\langle v_{los}^3 \rangle = \kappa \sigma_{los}^4$ by integration over the projected radius *R*:

$$v_{\rm s1} = \int_0^\infty \Sigma \langle v_{\rm los}^4 \rangle R \, \mathrm{d}R, \qquad (4.18)$$

$$v_{\rm s2} = \int_0^\infty \Sigma \langle v_{\rm los}^4 \rangle R^3 \,\mathrm{d}R,\tag{4.19}$$

where Σ is the surface brightness profile of the galaxy. The fourth velocity moment is assumed to be constant beyond the outermost bin. The uncertainty of the virial shape parameters is determined by random sampling of $\langle v_{los}^4 \rangle$ from the posterior of the generalized Gaussian fits, generating a probability density function. GravSphere will then compare the models to the data using the velocity dispersion of each bin, including the Gaussian uncertainties, and the two global virial shape parameters with their probability density functions.

Due to the small number of stars in our samples and the large measurement uncertainties on the stellar velocities, the fourth velocity moments are unconstrained. The result is that the virial shape parameters have little constraining power. We have tested GravSphere on Eri 2 both with and without using the virial shape parameters, and found no significant difference in the results. We have chosen to use the virial shape parameters for all our galaxies, per the default setting of GravSphere.

We fit the exponential surface-brightness profiles assumed for CJAM with a superposition of three Plummer (1911) spheres and adopt the same stellar mass as for CJAM. GravSphere uses emcee (Foreman-Mackey et al., 2013) to explore the parameter space made up of the dark-matter profile parameters, anisotropy parameters, and small variations around the adopted stellar mass and surface-brightness profile parameters. The piors are uniform; we show the ranges of the priors in Table 4.4. We use 250 walkers with 25000 steps and discard the first 75% of the steps as burn-in, which are the default settings of GravSphere.

4.4 RESULTS

We present our results in the following sections, broken down into the estimation of model parameters (Sect. 4.4.1), the determination of the constraints on the density profile and derived quantities (Sect. 4.4.2), the comparison of the different models (Sect. 4.4.3), a test for the effects of tidal stripping (Sect. 4.4.4), and the comparison of our results to the expected scaling relations (Sect. 4.4.5). Most of these results are determined with the fiducial CJAM analysis. To evaluate the robustness of the CJAM results, we have also analysed our galaxies with GravSphere. Where CJAM and GravSphere agree, we present only CJAM here and refer to the Grav-Sphere results in Appendix 4.A. If the two tools are not in agreement, the results of both are shown here.

4.4.1 Parameter estimation

We sampled the parameter spaces of our models with MultiNest, using the parametrizations described above. We then converted the posterior distributions to a different set of parameters, those that occur in Equations (4.3)–(4.5): ρ_0 and r_s for the cusp model, additionally r_c for the core model, and $\rho_{sol,0}$, r_{sol} , $\rho_{cusp,0}$, and r_s for the soliton model. These converted posteriors

are shown in Figs. 4.B.1–4.B.3 in Appendix 4.B, including the confidence intervals or upper and lower limits. Here we describe and compare the constraints on the parameters.

Comparing the galaxies among themselves (Figs. 4.B.1–4.B.3), we see a general trend with Ant B and Hya II usually having a larger r_s than Leo T and Gru 1, while Leo T and Hya II usually have a larger ρ_0 or $\rho_{cusp,0}$ than Ant B and Gru 1. These differences are, however, not significant due to the large uncertainties on these parameters.

When we look at the posteriors of r_c in Fig. 4.B.2, we see a clear peak. However, these distributions have tails extending to values smaller than the projected radii of the innermost tracers. As was the case with Eri 2 in Paper II, the posterior distributions on r_c therefore do not constitute a detection of a core, but should instead be regarded as upper limits. All four galaxies have a core radius $r_c < 66-95$ pc at the 68% confidence level. For Leo T, the 95% upper limit is $r_c < 200$ pc. The other three galaxies have $r_c < 295-309$ pc at the 95% confidence level.

Interpreting the posterior distributions of the soliton parameters $\rho_{sol,0}$ and $r_{\rm sol}$, shown in Fig. 4.B.3, is more complex. Ant B and Hya II show multi-modal distributions and there may be a hint of multi-modality in the other galaxies. Upon further inspection, we see that the mode with large r_{sol} and small $\rho_{sol,0}$ lies along $r_{sol} = r_s$, which is the edge of the prior, and is accompanied with a sudden drop in $\rho_{cusp.0}$. It therefore seems that this mode corresponds to a scenario where the soliton part of the profile is used to fit the change in slope at r_s , a feature of all three of our models, instead of an actual soliton. If we consider the modes with large r_{sol} spurious and concentrate on the other modes and their tails, we see again that the posterior distributions are consistent with radii smaller than the projected radii of the innermost tracers. We therefore interpret the posterior distributions of $r_{\rm sol}$ as upper limits. Due to the degeneracy between $r_{\rm sol}$ and $\rho_{\rm sol,0}$, we consider the posteriors of the latter as lower limits. The strength of the limit correlates with the strength of the multi-modality; for Leo T and Gru 1 we can constrain r_{sol} < 13–14 pc at the 68% confidence level, whereas the opposite extreme is Hya II with $r_{sol} < 112 \, \text{pc.}$ Ant B is in the middle with $r_{\rm sol}$ < 43 pc at the 68% confidence level. The 95% confidence levels are more divergent: r_{sol} < 251 pc for Leo T, <724 pc for Gru 1, <1.20 kpc for Ant B, and <1.58 kpc for Hya II. The large difference between the 68% and 95% confidence limits is a consequence of the spurious large- r_{sol} modes, which pull the 95% confidence limits to larger values of r_{sol} .

Due to the differences between the implemented models, the parameter constrains from CJAM and GravSphere are not directly comparable. However, we can point out that the core radius r_c of the GravSphere core+tides model, as discussed in Appendix 4.A and shown in Figs. 4.B.9–4.B.13, is not

constrained and includes the possibility of cores larger than 1 kpc. This lack of constraints is due to a degeneracy between the core radius r_c and the completeness of core formation, n: for partially formed cores, larger core radii are allowed than for the fully formed cores modelled with CJAM.

4.4.2 Profile recovery

We take the posterior distributions of model parameters, evaluate the density profile, and marginalize over the model parameters to calculate constraints on the density profiles of our dwarf galaxies. These profiles are displayed in Fig. 4.2. For each galaxy, we see that the different models agree within the uncertainties at the larger radii. The constraints are the tightest and best-agreeing at the radii with the largest concentration of tracers. The profiles start to diverge more as one goes to smaller radii, particularly the core model. The agreement between the cusp and soliton models is very good at all radii.

We further note that in the centres the soliton model prefers the highest density for three out of four galaxies and the core model the lowest for all galaxies. This can be understood as a consequence of the formulations of these models. At intermediate radii the soliton profile rises steeply, only to flatten out at scales around the soliton radius. For equal ρ_0 ($\rho_{cusp.0}$) and $r_{\rm s}$, this forces the density of the soliton model to be higher than that of the cusp model for radii inside the transition radius, which is reflected in the marginalized density profiles. Similarly, the core model always has a lower central density than the cusp model due to the presence of a core, or at most an equal density when $r_c = 0$, for which the two models produce identical profiles. This has as a side effect that the median density profile will be skewed away from the mode. For example, if we were to fit a core model to a finite number of measurements with non-zero uncertainties, drawn from a cuspy profile, the mode of the resulting density profile should be at $r_{\rm c} = 0$, the truth, but because of the finite information there will be an asymmetric tail towards $r_c > 0$. Therefore the median recovered r_c will always be larger than the mode or the truth, which translates into a lower central density.

By comparing the CJAM profiles with those derived using GravSphere in Appendix 4.A and shown in Fig. 4.A.1, we see that they are generally in good agreement, especially near the half-light radius due to the high concentration of tracers. We do see that the CJAM profiles are systematically steeper. This could mean the profile is sensitive to bias when extrapolated beyond the range containing tracers. The GravSphere results also indicate that the profile parameters are not correlated with the velocity anisotropy, which means that the assumed isotropy of our CJAM model should not have influenced its results.



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From the density profiles we can calculate constraints on additional quantities, such as the virial radius r_{200} , inside which the average density is 200 times the critical density of the Universe, and the associated concentration $c_{200} \coloneqq r_{200}/r_s$ and virial mass M_{200} . As the virial mass of satellite galaxies is hard to determine in simulations, we also calculate V_{max} , the maximum of the circular velocity profile. We further provide circular velocities and masses for the projected half-light radius $R_{1/2}$ and the three-dimensional half-light radius $r_{1/2} \simeq (4/3)R_{1/2}$ (Wolf et al., 2010). The mass-to-light ratios $\Upsilon(r_{200}) \coloneqq M_{200}/L_V$ and $\Upsilon(r_{1/2}) \coloneqq M(r_{1/2})/(L_V/2)$ are an indicator of how dark matter-dominated the galaxies are. Finally, the astrophysical J and D factors are measures of the potential to detect signals from dark-matter annihilation and decay, respectively, from a galaxy. These factors are integrals of the density profile (for decay) or the square of the density profile (for annihilation, a two-particle process) over the line of sight and a solid angle on the sky, and are therefore proportional to the reaction rate in a field of view. To calculate the expected signal flux from a certain source for a certain proposed kind of dark-matter particle, the source-specific astrophysical factors need to be combined with a particle-specific factor. We have determined the astrophysical factors inside the critical integration angles, which maximize the signal. The critical integration angle for decay, α_{c}^{D} , is the angle subtended by the projected half-light radius, while the critical integration angle for annihilation, α_c^J , corresponds to twice the projected half-light radius (Bonnivard et al., 2015b; Walker & Peñarrubia, 2011). Constraints on all these quantities are given per galaxy and model in Table 4.5.

The differences in constraints between different models of the same galaxy are generally small, certainly when considering the size of the uncertainties. The differences between the galaxies are larger. We note that, although Hya II is the third most luminous galaxy, its M_{200} and V_{max} are the highest. Within the half-light radius, the ordering of the masses is in line with that of the luminosities. Consequently, Hya II has high mass-to-light ratios and astrophysical *J* and *D* factors. Lastly, we note that Leo T and Hya II tend to higher concentrations than Ant B and Gru 1.

We repeated the calculation of the same quantities on the GravSphere profiles, the results of which we list in Table 4.A.1 and present in Ap-

FIGURE 4.2 (FACING PAGE): Recovered dark-matter density profiles of the four (ultra-)faint dwarf galaxies, for cusp, core, and soliton profiles, modelled with CJAM. The hatched bands indicate the 68% confidence interval on the density at each radius. The central, thicker line is the median density at each radius. The galaxy's projected half-light radii are indicated with the vertical dashed lines. The markers along the bottom of each panel indicate the projected radii of the kinematic tracers.

		Ant B			Leo T	
	cusp	core	soliton	cusp	core	soliton
$\log_{10}(V_{\rm max}/{\rm kms^{-1}})$	$1.20^{+0.21}_{-0.10}$	$1.24_{-0.13}^{+0.21}$	$1.17_{-0.08}^{+0.15}$	$1.17_{-0.11}^{+0.18}$	$1.23_{-0.14}^{+0.23}$	$1.14_{-0.10}^{+0.13}$
$\log_{10}(r_{200}/\text{kpc})$	$1.18^{+0.30}_{-0.19}$	$1.22_{-0.18}^{+0.29}$	$1.09^{+0.23}_{-0.17}$	$1.07^{+0.29}_{-0.19}$	$1.15_{-0.20}^{+0.32}$	$0.95_{-0.18}^{+0.25}$
$\log_{10}(c_{200})$	$1.39^{+0.32}_{-0.32}$	$1.46_{-0.30}^{+0.25}$	—	$1.61_{-0.32}^{+0.35}$	$1.63^{+0.24}_{-0.32}$	—
$\log_{10}(M_{200}/M_{\odot})$	$8.57^{+0.89}_{-0.58}$	$8.67^{+0.87}_{-0.55}$	$8.29_{-0.53}^{+0.71}$	$8.22^{+0.87}_{-0.56}$	$8.46^{+0.95}_{-0.59}$	$7.88^{+0.73}_{-0.54}$
$\log_{10}(Y(r_{200})/M_{\odot}L_{\odot}^{-1})$	$2.76^{+0.89}_{-0.58}$	$2.87^{+0.87}_{-0.55}$	$2.49^{+0.71}_{-0.53}$	$3.26^{+0.87}_{-0.56}$	$3.50^{+0.95}_{-0.59}$	$2.92_{-0.54}^{+0.73}$
$\log_{10}(V(R_{1/2})/\text{km s}^{-1})$	$1.10^{+0.05}_{-0.06}$	$1.09^{+0.05}_{-0.05}$	$1.10^{+0.05}_{-0.06}$	$1.07^{+0.07}_{-0.07}$	$1.06^{+0.08}_{-0.08}$	$1.05_{-0.09}^{+0.08}$
$\log_{10}(M(R_{1/2})/M_{\odot})$	$7.01_{-0.12}^{+0.10}$	$7.00_{-0.11}^{+0.10}$	$7.01_{-0.13}^{+0.11}$	$6.68^{+0.15}_{-0.14}$	$6.67^{+0.16}_{-0.17}$	$6.65_{-0.17}^{+0.16}$
$\log_{10}(Y(R_{1/2})/M_{\odot}L_{\odot}^{-1})$	$1.51_{-0.12}^{+0.10}$	$1.50_{-0.11}^{+0.10}$	$1.51_{-0.13}^{+0.11}$	$2.02^{+0.15}_{-0.14}$	$2.01^{+0.16}_{-0.17}$	$1.99_{-0.17}^{+0.16}$
$\log_{10}(V(r_{1/2})/\mathrm{kms^{-1}})$	$1.12_{-0.06}^{+0.06}$	$1.13_{-0.06}^{+0.06}$	$1.12_{-0.07}^{+0.06}$	$1.09^{+0.07}_{-0.07}$	$1.11_{-0.08}^{+0.08}$	$1.06^{+0.08}_{-0.09}$
$\log_{10}(M(r_{1/2})/M_{\odot})$	$7.19_{-0.12}^{+0.11}$	$7.21_{-0.12}^{+0.11}$	$7.18^{+0.12}_{-0.13}$	$6.87^{+0.14}_{-0.15}$	$6.89^{+0.16}_{-0.16}$	$6.81_{-0.19}^{+0.16}$
$\log_{10}(J(\alpha_c^J)/M_{\odot}^2 \text{ kpc}^{-5})$	$9.29^{+0.26}_{-0.24}$	$9.23^{+0.29}_{-0.26}$	$9.31_{-0.26}^{+0.36}$	$10.44_{-0.32}^{+0.34}$	$10.40_{-0.34}^{+0.36}$	$10.48^{+0.49}_{-0.36}$
$\log_{10}(D(\alpha_c^D)/M_{\odot} \text{ kpc}^{-2})$	$1.52_{-0.32}^{+0.49}$	$1.60_{-0.32}^{+0.49}$	$1.39_{-0.30}^{+0.39}$	$2.19^{+0.46}_{-0.31}$	$2.34_{-0.34}^{+0.52}$	$1.99_{-0.33}^{+0.38}$

TABLE 4.5: Parameters derived from the recovered dark-matter density profiles from CJAM.

pendix 4.A. We see good agreement between the two tools for quantities determined within the half-light radius, as expected from the agreement on the profiles. However, at the larger scales, we see systematic differences, for example in M_{200} . This is likely the result of the aforementioned systematic differences in the density slopes. We will discuss the implications of these differences in Sect. 4.4.5, where we compare our results against theoretical scaling relations.

4.4.3 Model comparison

Having appreciated the results of our models and their differences, we now turn to establishing which of these models is the best description of each galaxy. MultiNest provides several estimators of Bayesian evidence. As in Paper II, we use the nested sampling global log-evidence estimator. The Bayesian evidence is the posterior likelihood of observing the data given the model and its priors. Because this likelihood has been integrated over the entire parameter space, the Bayesian evidence takes into account not only how well the model fits the data for the best parameter values, but how well the model does in general. This penalizes models with larger parameter spaces and avoids over-fitting. We display the natural logarithm of the Bayesian evidence, $\ln(Z)$, in Table 4.6.

Different models for the same galaxy can be compared by computing the posterior odds ratios. We assume no prior preference for certain models and take the prior odds ratios to be 1. Therefore the posterior odds ratios are equal to the ratios of the Bayesian evidence, known as the Bayes factors.

Нуа п			Gru 1	
p core	soliton	cusp	core	soliton
$^{+0.25}_{-0.18}$ 1.49 $^{+0.29}_{-0.2}$	$1.38^{+0.24}_{-0.16}$	$0.98^{+0.29}_{-0.29}$	$1.02^{+0.30}_{-0.30}$	$0.99^{+0.24}_{-0.26}$
$^{+0.33}_{-0.24}$ 1.39 $^{+0.39}_{-0.22}$	$1.20^{+0.32}_{-0.22}$	$0.92^{+0.37}_{-0.30}$	$1.01_{-0.29}^{+0.34}$	$0.80^{+0.32}_{-0.27}$
$^{+0.31}_{-0.29}$ 1.70 $^{+0.2}_{-0.29}$	5 —	$1.41_{-0.45}^{+0.49}$	$1.32_{-0.36}^{+0.32}$	_
$^{+0.99}_{-0.73}$ 9.19 $^{+1.03}_{-0.73}$	$^{8}_{5}$ 8.62 $^{+0.96}_{-0.68}$	$7.79^{+1.11}_{-0.90}$	$8.06^{+1.03}_{-0.87}$	$7.43^{+0.96}_{-0.81}$
$^{+0.99}_{-0.73}$ 5.32 $^{+1.03}_{-0.73}$	$4.76^{+0.96}_{-0.68}$	$4.22^{+1.11}_{-0.90}$	$4.50^{+1.03}_{-0.87}$	$3.87^{+0.96}_{-0.81}$
$^{+0.12}_{-0.11}$ 1.05 $^{+0.12}_{-0.11}$	$1.11^{+0.13}_{-0.16}$	$0.83^{+0.24}_{-0.28}$	$0.75^{+0.23}_{-0.26}$	$0.85^{+0.22}_{-0.25}$
$^{+0.23}_{-0.21}$ 6.33 $^{+0.2}_{-0.2}$	$56.44^{+0.26}_{-0.32}$	$6.20^{+0.48}_{-0.55}$	$6.04^{+0.46}_{-0.52}$	$6.24_{-0.50}^{+0.43}$
$^{+0.23}_{-0.21}$ 2.76 $^{+0.2}_{-0.2}$	$52.87^{+0.26}_{-0.32}$	$2.93^{+0.48}_{-0.55}$	$2.78^{+0.46}_{-0.52}$	$2.97^{+0.43}_{-0.50}$
$^{+0.10}_{-0.10}$ 1.13 $^{+0.12}_{-0.11}$	$1.15^{+0.12}_{-0.13}$	$0.85^{+0.24}_{-0.27}$	$0.81^{+0.23}_{-0.26}$	$0.86^{+0.21}_{-0.25}$
$^{+0.21}_{-0.21}$ $6.60^{+0.2}_{-0.2}$	$6.66^{+0.24}_{-0.26}$	$6.38_{-0.55}^{+0.48}$	$6.04_{-0.52}^{+0.46}$	$6.40^{+0.41}_{-0.51}$
$^{+0.44}_{-0.42}$ 11.95 $^{+0.5}_{-0.42}$	$12.02^{+0.50}_{-0.49}$	$10.47_{-1.13}^{+0.93}$	$10.32^{+0.90}_{-1.08}$	$10.55_{-1.04}^{+0.88}$
$^{+0.53}_{-0.42}$ 3.45 $^{+0.60}_{-0.44}$	$3.17^{+0.51}_{-0.37}$	$2.82^{+0.65}_{-0.66}$	$2.97^{+0.65}_{-0.65}$	$2.65_{-0.65}^{+0.60}$
	$\begin{array}{c c} Hya II \\ p & core \\ \hline +0.25 & -0.18 & 1.49 \\ -0.25 & -0.18 & 1.49 \\ -0.25 & -0.28 \\ +0.31 & -0.24 \\ +0.31 & -0.24 \\ +0.31 & -0.24 \\ -0.29 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.73 & -0.29 \\ -0.74 & -0.29 \\ -0.21 & -0.74 \\ -0.11 & -0.10 \\ -0.11 & -0.11 \\ -0.10 & -0.11 \\ -0.10 & -0.11 \\ -0.10 & -0.11 \\ -0.11 & -0.11 \\ -0.10 & -0.11 \\ -0.10 & -0.11 \\ -0.11 & -0.11 \\ -0.11 & -0.11 \\ -0.12 & -0.21 \\ -0.21 & -0.21 \\ -$	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$\begin{array}{c c c c c c c c c c c c c c c c c c c $

NOTES: V_{max} : maximum circular velocity; r_{200} : virial radius; c_{200} : concentration parameter; M_{200} : virial mass; Y(r): mass-to-light ratio integrated within radius r; V(r): circular velocity at radius r; $R_{1/2}$: projected half-light radius; M(r): mass within radius r; $r_{1/2}$: three-dimensional half-light radius; $J(\alpha_c^J)$: astrophysical J factor within its critical angle; $D(\alpha_c^D)$: astrophysical D factor within its critical angle.

According to the scale of Jeffreys (1961, their Appendix B), an odds ratio of 10^{-2} is required to rule out a model decisively. For each galaxy, we calculate the Bayes factors relative to the model with the largest Bayesian evidence, and display the decimal logarithm of the Bayes factor, $\Delta \log_{10}(Z)$, in Table 4.6. The only model with substantial evidence against it ($\Delta \log_{10}(Z) < 10^{-0.5}$) is the core model for Leo T, though substantial evidence is still far from significant. For all other models the evidence is weak. We cannot exclude the cusp, core, or soliton model for any of our galaxies. For each galaxy individually, the soliton model is the most preferred and the core model the least. We defer a joint analysis, in which all galaxies are expected to follow the same profile model with the same dark-matter properties, to a follow-up paper.

4.4.4 Tidal stripping

With the newly presented galaxies in this paper, we have increased the number of dark-matter density profiles from the MUSE-Faint survey from one to five. Now we are going to compare the measured properties of all five galaxies against theoretical expectations. From the comparison between the CJAM and GravSphere profiles it is clear that the profiles are best determined, with the smallest uncertainties and the least bias, around the half-light radii. We therefore begin our comparison between the derived profiles and theoretical expectations with a model based on quantities measured around the half-light radius.

Fattahi et al. (2018) present a theoretical relation, based on the APOSTLE

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$ \begin{array}{cccccc} {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm sol} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm core} & {\rm soliton} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm cusp} & {\rm core} & {\rm soliton} & {\rm coliton} & {\rm col$			Ant B			Leo T			Hya II			Gru 1	
$ \begin{array}{llllllllllllllllllllllllllllllllllll$		cusp	core	soliton	cusp	core	soliton	cusp	core	soliton	cusp	core	soliton
$\Delta \log_{10}(Z) -0.01 -0.17 = 0.16 -0.53 = 0 -0.19 -0.27 = 0 -0.11 -0.16$	$\ln(Z)$	-499.39	-499.76	-499.37	-312.01	-312.86	-311.65	-118.28	-118.46	-117.84	-58.49	-58.62	-58.24
	$\Delta \log_{10}(Z)$	-0.01	-0.17	0	-0.16	-0.53	0	-0.19	-0.27	0	-0.11	-0.16	0

NOTES: $\ln(Z)$: natural logarithm of the Bayesian evidence Z; $\Delta \log_{10}(Z)$: decimal logarithm of the Bayes factor, or difference of the decimal logarithms of Bayesian evidence, relative to the best model of each galaxy.

TABLE 4.7: Supplementary parameters derived from the CJAM density profiles of Eridanus 2 presented in Paper II.

		Eri 2	
	cusp	core	soliton
$\log_{10}(V(r_{1/2})/\text{km s}^{-1})$	$1.14_{-0.06}^{+0.06}$	$1.16^{+0.06}_{-0.06}$	$1.10^{+0.07}_{-0.11}$
$\log_{10}(M(r_{1/2})/\text{km s}^{-1})$	$7.16_{-0.12}^{+0.12}$	$7.20_{-0.11}^{+0.13}$	$7.08^{+0.14}_{-0.21}$

NOTES: The cusp, core, and soliton models are identified in Paper II as cold dark matter, selfinteracting dark matter, and fuzzy dark matter, respectively. $V(r_{1/2})$: circular velocity at the threedimensional half-light radius; $M(r_{1/2})$: mass within the three-dimensional half-light radius.

zoom-in simulations of Local Group-like environments, between the stellar mass M_*^{prog} and maximum circular velocity $V_{\text{max}}^{\text{prog}}$ of a satellite galaxy's progenitor, when the stellar mass and maximum circular velocity where at their peak, before the progenitor started falling into the host galaxy. This theoretical relation is combined with a procedure to relate M_*^{prog} and $V_{\text{max}}^{\text{prog}}$ to the satellite's present-day stellar mass M_* , present-day three-dimensional half-light radius $r_{1/2}$, and present-day circular velocity $V(r_{1/2})$ at that radius, by accounting for tidal stripping. This stripping procedure is based on the assumption that the progenitors at peak stellar mass and peak maximum circular velocity have an NFW profile, therefore it only applies to the cusp models in this paper. The procedure has three theoretical ingredients: the aforementioned $M_*^{\text{prog}} - V_{\text{max}}^{\text{prog}}$ relation; the mass-concentration relation of Ludlow et al. (2016), applied to the progenitors $(M_{200}^{\text{prog}} - c_{200}^{\text{prog}})$; and the tidal tracks of Errani et al. (2015) describing the coupled evolution of M_* , $r_{1/2}$, and $V(r_{1/2})$. These tidal tracks are a function of $x := M(r_{1/2}^{\text{prog}})/M_{\text{prog}}(r_{1/2}^{\text{prog}})$, which is the fraction of present-day versus peak total mass remaining inside $r_{1/2}^{\text{prog}}$, the three-dimensional half-light radius of the progenitor. There should be one value of x for which a progenitor satisfying the $M_*^{\text{prog}} - V_{\text{max}}^{\text{prog}}$ and $M_{200}^{\text{prog}} - c_{200}^{\text{prog}}$ scaling relations, evolving along the tidal tracks, produces the observed galaxy.

Because in Paper II we did not compute quantities associated with the three-dimensional half-light radius, we provide in Table 4.7 the circular velocity at, and mass within, this radius, based on the original profiles. In the top row of Fig. 4.3 we show our galaxies in the $M_* - V(r_{1/2})$ and $M_* - V_{max}$ planes as well as the $M_*^{\text{prog}} - V_{\text{max}}^{\text{prog}}$ relation of Fattahi et al. (2018) that is repeated in all panels. If the galaxies have not experienced any tidal stripping, we expect that they lie on the indicated relation in the top right panel. If stripping did occur, they should be located to the left of the relation, having lost dark matter more heavily than stars. Meanwhile, in the top left panel, the galaxies are expected to always lie to the left of the relation, because



4.4 Results

by definition $V_{\text{max}} > V(r_{1/2})$. However, we need to take into account that V_{max} is determined at a larger radius than $r_{1/2}$ and could therefore be biased by the systematic difference in density profile slope that we noticed in our comparison between CJAM and GravSphere. Therefore, the fact that our measurements do not follow the relation in the top right panel is not solid evidence of stripping. As the stripping calculations are based on $V(r_{1/2})$, not V_{max} , this possible bias will not affect the results of these calculations.

Here we describe the determination of the progenitor properties and the amount of tidal stripping in more detail. Given a value of the stripping parameter x, the observed M_* , $V(r_{1/2})$, and $r_{1/2}$ can be converted to the progenitor's M_*^{prog} , $V_{\text{prog}}(r_{1/2}^{\text{prog}})$, and $r_{1/2}$ using the tidal tracks. This x is the sole degree of freedom in the tidal tracks, which we must constrain. Together, $V_{\text{prog}}(r_{1/2}^{\text{prog}})$ and $r_{1/2}^{\text{prog}}$ allow us to calculate $M_{\text{prog}}(r_{1/2}^{\text{prog}})$, the mass of the progenitor inside its half-light radius. We will constrain the degree of freedom by additionally requiring that the progenitor obeys the $M_*^{\text{prog}} - V_{\text{max}}^{\text{prog}}$ and $M_{200}^{\text{prog}} - c_{200}^{\text{prog}}$ scaling relations. Every choice of x then corresponds to an M_{200}^{prog} and c_{200}^{prog} , enough to fully specify the two-parameter NFW profile of the progenitor. From this density profile we can also calculate $M_{\text{prog}}(r_{1/2}^{\text{prog}})$. We can therefore constrain our one degree of freedom by demanding that the results of these two different $M_{\text{prog}}(r_{1/2}^{\text{prog}})$ calculations are identical. Thus we find x as well as M_*^{prog} , $V_{\text{prog}}(r_{1/2}^{\text{prog}})$, and $r_{1/2}^{\text{prog}}$.

For computational ease, we search for the solution of the above problem by varying M_{200}^{prog} instead of *x*. In this way, we save ourselves from inverting the M_{200}^{prog} - c_{200}^{prog} relation. We proceed as follows: Given an initial guess for the virial mass M_{200}^{prog} of the progenitor, we calculate its concentration c_{200}^{prog}

FIGURE 4.3 (FACING PAGE): Observed galaxy properties (top row), as determined with CJAM, matched with predicted progenitor properties (bottom row) according to the method of Fattahi et al. (2018). Top left: Observed circular velocities $V(r_{1/2})$ at the three-dimensional half-light radius against observed stellar masses M_* . Top right: Observed maximum circular velocities V_{\max} against observed stellar masses M_* . Bottom left: Predicted progenitor circular velocities $V_{\text{prog}}(r_{1/2}^{\text{prog}})$ at the three-dimensional half-light radius against predicted progenitor stellar masses M_*^{prog} . Bottom right: Predicted progenitor maximum circular velocities V_{\max}^{prog} against predicted progenitor stellar masses M_*^{prog} . The observed galaxies have properties measured under the assumption of three different density profile models, cusp, core, and soliton, while the progenitor properties can only be predicted for the cusp model. The progenitors are assumed to obey theoretical scaling relations, including the $M_*^{\text{prog}}-V_{\text{max}}^{\text{prog}}$ scaling relation of Fattahi et al. (2018), which is displayed in the bottom-right panel with a solid line and repeated for reference in the other panels with a dashed line. We devolve the observed galaxy properties in the *top-left* panel along theoretical tidal tracks to obtain the predicted progenitor properties in the *bottom* row. The observations in the *top-right* panel are not used in this procedure. The observed galaxies are tidally stripped of dark matter or stars if the observed circular velocity or stellar mass, respectively, indicated in the top-left panel, are smaller than those of the progenitor in the bottom-left panel.

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TABLE 4.8: Progenitor properties based on CJAM,

	Ant B	Leo T	Eri 2	Hya II	Gru 1
$\log_{10}(M_{*}^{\mathrm{prog}}/M_{\odot})$	$5.89_{-0.03}^{+0.17}$	$5.14_{-0.00}^{+0.08}$	$4.94_{-0.01}^{+0.10}$	$4.28_{-0.00}^{+0.00}$	$3.87_{-0.09}^{+0.59}$
$\log_{10}(V_{\rm max}^{\rm prog}/{\rm kms^{-1}})$	$1.45_{-0.07}^{+0.10}$	$1.40_{-0.06}^{+0.07}$	$1.39_{-0.05}^{+0.07}$	$1.35_{-0.04}^{+0.06}$	$1.34_{-0.04}^{+0.06}$
$\log_{10}(r_{1/2}^{\text{prog}}/\text{kpc})$	$-0.44_{-0.05}^{+0.06}$	$-0.68_{-0.06}^{+0.06}$	$-0.48_{-0.06}^{+0.06}$	$-0.97_{-0.08}^{+0.08}$	$-0.71_{-0.06}^{+0.08}$
$\log_{10}(V_{\rm prog}(r_{1/2}^{\rm prog})/{\rm kms^{-1}})$	$1.16\substack{+0.08\\-0.07}$	$1.07_{-0.07}^{+0.10}$	$1.13_{-0.07}^{+0.09}$	$1.08_{-0.15}^{+0.17}$	$0.99_{-0.08}^{+0.11}$
$\log_{10}(x)$	$-0.07_{-0.16}^{+0.13}$	$0.03_{-0.16}^{+0.13}$	$0.00^{+0.13}_{-0.15}$	$0.12_{-0.19}^{+0.17}$	$-0.17_{-0.50}^{+0.26}$
$\log_{10}(\mu_L)$	$-0.01_{-0.17}^{+0.03}$	$0.02_{-0.08}^{+0.00}$	$0.01_{-0.10}^{+0.01}$	$0.02\substack{+0.00\\-0.00}$	$-0.07_{-0.59}^{+0.09}$

NOTES: M_*^{prog} : progenitor stellar mass; V_{\max}^{prog} ; progenitor maximum circular velocity; $r_{1/2}^{\text{prog}}$; progenitor three-dimensional half-light radius; $V_{\text{prog}}(r_{1/2}^{\text{prog}})$; progenitor circular velocity within the progenitor three-dimensional half-light radius; $V_{\text{prog}}(r_{1/2}^{\text{prog}})$; progenitor circular velocity within the progenitor three-dimensional half-light radius; $W_{\text{prog}}(r_{1/2}^{\text{prog}})$; fraction of the total mass within the progenitor's three-dimensional half-light radius after tidal stripping; μ_L : M_*^{prog} , fraction of the stellar mass that remains after tidal stripping.

according to Ludlow et al. (2016). As we know the progenitor follows an NFW profile, we can use both of these parameters to calculate $V_{\text{max}}^{\text{prog}}$. The application of the Fattahi et al. (2018) $M_*^{\text{prog}} - V_{\text{max}}^{\text{prog}}$ scaling relation then leads to M_*^{prog} . We numerically solve the tidal track for the evolution of stellar mass to find the *x* for which the M_*^{prog} progenitor produces an M_* satellite. This *x* is then substituted into the other tidal tracks to find $r_{1/2}^{\text{prog}}$ from $r_{1/2}$ and $V_{\text{prog}}(r_{1/2}^{\text{prog}})$ from $V(r_{1/2})$. Together, $V_{\text{prog}}(r_{1/2}^{\text{prog}})$ and $r_{1/2}^{\text{prog}}$ allow us to calculate $M_{\text{prog}}(r_{1/2}^{\text{prog}})$. We calculate the same from M_{200}^{prog} and c_{200}^{prog} , which should give the same result if our guess of M_{200}^{prog} is correct. We numerically minimize the difference of the two calculations of $M_{\text{prog}}(r_{1/2}^{\text{prog}})$ by varying M_{200}^{prog} until a match is found.

We propagate the measurement uncertainties on M_* , $r_{1/2}$, and $V(r_{1/2})$ in a Monte Carlo fashion by taking random samples from their posterior distributions. To account for scatter in the scaling relations, we vary the nominal values from the several scaling relations with a log-normally distributed factor based on the scatter visible in the figures of Ludlow et al. (2016), Fattahi et al. (2018), and Errani et al. (2015). This scatter amounts to 0.1 dex on c_{200}^{prog} , 1 dex on M_*^{prog} , 0.2 dex on x, 0.05 dex on $r_{1/2}^{\text{prog}}$, and 0.05 dex on $V(r_{1/2}^{\text{prog}})$. We also vary the redshift at which we evaluate the mass-concentration relation uniformly between 0–1. The added scatter and redshift variation increase the uncertainties on our results, but we find that our conclusions would not have been different if we had opted to not propagate these theoretical uncertainties.

For all five of our galaxies we find a progenitor that solves all constraints. The progenitors' properties, as well as the stripping parameters x and $\mu_L := M_*/M_*^{\text{prog}}$ are presented in Table 4.8 and their locations in the $M_*^{\text{prog}}-V_{\text{prog}}(r_{1/2}^{\text{prog}})$ and $M_*^{\text{prog}}-V_{\text{max}}^{\text{prog}}$ planes are shown in the bottom row of Fig. 4.3. By design, we see that the maximum circular velocities of the progenitors follow the Fattahi et al. (2018) relation. The circular velocity at the three-dimensional half-light radius being naturally smaller than the maximum circular velocity, the galaxies lie a little to the left in the bottom-left panel. By eye, the locations of the progenitor galaxies in the top-left panel. This indicates that the total mass within the half-light radius and the stellar mass have not significantly changed during tidal stripping.

Indeed, from Table 4.8 we can see that all galaxies are consistent with having undergone no stripping, as they include x = 1 in their confidence intervals. However, the large uncertainties on Gru 1 still include $x = 10^{-0.67} \approx 0.2$, which means up to $\approx 80\%$ of its original mass could have been stripped. Given its present-day distance of >100 kpc from the Milky Way, such significant stripping seems surprising. However, there may have been


distance to the Milky Way ever reached. The stripping parameters x and μ_L are the fractions of total mass within the half-light radius and of the total stellar mass, respectively, remaining after tidal stripping; lower values indicate more stripping has occurred. We show results for two models of the Milky Way that differ in the halo mass. In most cases, the closest distance is not the pericentre distance but the current distance, as most of these galaxies are still in their first infall. For Hya II in both Milky Way models and for Gru 1 in the Milky Way models, the closest distance is the present-day distance, because in these models these galaxies are still on their first infall. We note that Antlia B is a satellite of NGC 3109, not of the Milky Way, and that its distance to the Milky Way is therefore not relevant for FIGURE 4.4: Stripping parameters of the galaxies, as determined with CJAM and comparison to theoretical models, versus their closest neavy Milky Way model, the closest distance is the pericentre. For Gru 1 in the light Milky Way models and for Leo T and Eri 2 in both ts stripping parameters; its display in this figure is merely illustrative.

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a previous time when these galaxies were closer to the Milky Way, at which time they could have been tidally stripped more significantly. Battaglia et al. (2022) provide pericentre distances for our four Milky Way satellites, based on *Gaia* EDR3 and two different Milky Way mass models: a light model ($M_{200} = 8.8 \times 10^{11} M_{\odot}$) and a heavy model ($M_{200} = 1.6 \times 10^{12} M_{\odot}$). We remind the reader that Ant B is not a satellite of the Milky Way, but rather of NGC 3109. In the light Milky Way model, only Hya II has reached its pericentre in the past; the other satellites are making their first infall. According to the heavy Milky Way model, both Hya II and Gru 1 have reached their pericentres in the past.

In Fig. 4.4 we display x and μ_L versus the closest distances to the Milky Way that the galaxies have ever reached, which is a past pericentre or the present-day distance in the case of first infall. Depending on the Milky Way model, Gru 1 may have made a close approach to the Milky Way, in which case significant stripping may indeed have occurred. The consistency of the more distant galaxies Leo T, Eri 2, and Hya II with no stripping indicates that our $V(r_{1/2})$ measurements match the theoretical expectations.

When we repeat the stripping procedure with the GravSphere results, as presented in Appendix 4.A, we find consistent results, listed in Table 4.A.3 and shown in Fig. 4.A.3. This confirms the robustness of our no-stripping conclusions and the $V(r_{1/2})$ measurements. However, the smaller uncertainties on the GravSphere profiles result in Gru 1 no longer being consistent with a significant amount of stripping.

4.4.5 Galaxy-halo scaling relations

We continue to test our results against theoretical expectations with a comparison of our measurements at larger radii against theoretical scaling relations. It is important to remember that these measurements at the virial radius may be biased due to the tendency of our two dynamical modelling tools to fits systematically different profile slopes. Though within the halflight radius, where we have kinematic tracers, the profiles agree within the measurement uncertainties, the difference in slope will make the profiles diverge as one goes to larger radii. Considering the virial radii r_{200} are over an order of magnitude larger than the half-light radii, the virial parameters may be significantly biased. Indeed, the lack of tracers far outside the halflight radii make the fitted profiles insensitive to deviations from the profile models, such as tidal stripping, if they occur at large radii. As we found no evidence of stripping inside the half-light radii and are incapable of detecting stripping outside, the virial parameters that we calculate would be those of our galaxies' progenitors, aside from the possible bias. We therefore do not have to concern ourselves with taking into account the effects of



FIGURE 4.5: Comparison of the galaxies' relation between virial masses M_{200} and concentrations c_{200} , as determined with CJAM (left) and GravSphere (*right*), to expectations from models. The model of Dutton & Macció (2014) is empirically fitted to simulations, while the models of Correa et al. (2015a,b,c) and Ludlow et al. (2016) are semi-analytical. The latter two models produce nearly indistinguishable results.

stripping on the scaling relations and can instead use the relations derived for isolated galaxies.

First we perform a comparison of virial masses and concentrations. In the left panel of Fig. 4.5 we display the values derived with CJAM for the four galaxies presented in this paper, supplemented with those of Eri 2 from Paper II. We compare these galaxies to a selection of mass–concentration relations. The models should be evaluated at the redshift at which the galaxies became satellites of the Milky Way. Lacking this information, we take a redshift of zero. The relation of Dutton & Macciò (2014) is fitted to simulations, though these fits are limited to $M_{200} \gtrsim 10^{10} M_{\odot}$. The application of this fitted relation to our galaxies is therefore an extrapolation. Correa et al. (2015a,b,c) and Ludlow et al. (2016) present semi-analytical models, which are physically motivated but still calibrated against simulations. Although the simulations against which the latter two models are calibrated do not reach UFD masses either, their physical backing makes the models more constrained and therefore these models should withstand extrapolation better.

The comparison in the left panel of Fig. 4.5 shows that all three models systematically underpredict the observations. The two semi-analytical models produce results very close to each other, while the model of Dutton & Macciò (2014) predicts somewhat higher concentrations that are slightly more consistent with the observations. Assuming a higher redshift will make the difference between theory and observations larger. The mismatch between the Ludlow et al. (2016) relation and the observations is on first thought remarkable because the stripping analysis indicated consistency with this relation.

We repeat the comparison with the GravSphere results presented in Appendix 4.A and show this in the right panel of Fig. 4.5. Now we do see an overall agreement between observation and theory, except for Hya II. The cusp model produces results close to the Dutton & Macciò (2014) scaling relations, while the lower concentrations of the core+tides model are closer to the predictions from the semi-analytical scaling relations.

In the left panel Fig. 4.6 we compare the stellar and virial masses from CJAM. When plotted in this way, we clearly see that the core models systematically tend to higher virial masses than the cusp models, which in turn tend to higher virial masses than the soliton models. The high virial mass of Hya II for its luminosity or stellar mass is also noticeable. We compare the measurements against a selection of stellar-to-halo mass scaling relations. These relations are determined applying a proposed scaling relation to haloes in a dark-matter simulation and comparing the observable properties of the simulated galaxies to observations. The relations of Behroozi et al. (2019) & Behroozi et al. (2013) are based on the UniverseMa-



FIGURE 4.6: Comparison of the galaxies' stellar masses M_{*} and virial masses M₂₀₀, as determined with CJAM (left) and Grav-Sphere (right), to expectations from models. The models of Behroozi et al. (2019) & Behroozi et al. (2013) are determined with UniverseMachine. The model of Garrison-Kimmel et al. (2017) has the scatter in the relation as a free parameter; we show lines corresponding to zero scatter (larger M_*) and 2.0 dex scatter (smaller M_*). We additionally show measurements for the sample of dwarf spheroidal (dSph) and dwarf irregular (dIrr) galaxies studied by Read et al. (2019)

chine models. Though these models have been calibrated to galaxies with $M_* \gtrsim 10^8 M_{\odot}$, Wang et al. (2021) find that the extrapolated stellar-to-halo mass relation of the second iteration (UniverseMachine DR1; Behroozi et al., 2019) is consistent with simulations of ultra-faint dwarf galaxies around a Milky Way-like host. Garrison-Kimmel et al. (2017) produce a model with a degeneracy between the low-mass slope of the scaling relation and the scatter in that relation, calibrated against observations of galaxies with M_* down to $\sim 10^5 M_{\odot}$. We show the two extremes, $M_* \propto M_{200}^{1.8}$ with zero scatter and $M_* \propto M_{200}^{2.6}$ with 2.0 dex scatter. The range between these extremes includes the UniverseMachine DR1 relation. The stellar-to-halo mass relation that best describes our measurements seems to be the old UniverseMachine model, even though this model is the only one not calibrated against observations or simulations of dwarf galaxies. We additionally compare our measurements with those of Read et al. (2019) for more massive dwarf galaxies, and see that these galaxies do follow the expected scaling relations.

We show the same comparison, now using the GravSphere results, in the right panel of Fig. 4.6. Again, GravSphere produces results consistent with the theoretical expectations, except for Hya II. The GravSphere measurements of our five faint dwarf galaxies are also consistent with an extrapolation of the the trend followed by the more massive dwarf galaxy sample of Read et al. (2019).

The above comparisons of the CJAM and GravSphere results against each other and against theoretical scaling relations demonstrate that the virial parameters are indeed sensitive to the dynamical modelling. Gravsphere does produce results more in line with theoretical expectations, but given that the dynamical models are not well tested in this regime, this cannot been taken in support of these models without more extensive tailored simulated data, the construction of which is outside the scope of this paper.

4.5 DISCUSSION

Here we place our results in the context of previous works (Sect. 4.5.1), and discuss how reliable our results (Sect. 4.5.2) and our dynamical analysis (Sect. 4.5.3) are.

4.5.1 Comparison to previous results

Though we presented the first dark-matter density profiles for Ant B, Leo T, Hya II, and Gru 1, dynamical masses and mass-to-light ratios have been measured before for some of these galaxies. For Ant B we have presented

the first kinematics, therefore no dynamical measurements were made before.

Simon & Geha (2007) measured a total mass of $M_{200} = (8.2 \pm 3.6) \times 10^6 M_{\odot}$ for Leo T based on its velocity dispersion and an associated mass-tolight ratio of $138 \pm 71 M_{\odot} L_{\odot}^{-1}$. This is inconsistent with our measurements of $M_{200} = 7.6^{+33.2}_{-5.4} \times 10^7 - 2.9^{+22.8}_{-2.1} \times 10^8 M_{\odot}$ and $\Upsilon(r_{200}) = 8.3^{+36.4}_{-5.9} \times 10^2 - 3.2^{+28.2}_{-2.3} \times 10^3 M_{\odot} L_{\odot}^{-1}$, which are over an order of magnitude larger. Several authors estimate the mass of Leo T within 300 pc from stellar kinematics – $M(300 \text{ pc}) = 1.30^{+0.88}_{-0.42} \times 10^7 M_{\odot}$ (Strigari et al., 2008) – or gas kinematics – $M(300 \text{ pc}) = (8.2 \pm 0.2) \times 10^6 M_{\odot}$ (Faerman et al., 2013) and $M(300 \text{ pc}) = (3.7\pm0.7)\times 10^6 M_{\odot}$ (Patra, 2018). From our three CJAM profiles for Leo T, we calculate $M(300 \text{ pc}) = 1.00^{+0.51}_{-0.42} \times 10^7 - 1.45^{+0.64}_{-0.51} \times 10^7 M_{\odot}$. This is consistent with the results of Strigari et al. (2008) and Faerman et al. (2013), but not with that of Patra (2018).

For Hya II, Kirby et al. (2015) constrain the mass within the half-light radius to $<10^{6.1} M_{\odot}$ at 95% confidence and the mass-to-light ratio within that radius to $<315 M_{\odot} L_{\odot}^{-1}$. Our measurements $M(R_{1/2}) = 2.1_{-1.0}^{+1.7} \times 10^{6} - 3.0_{-1.1}^{+2.1} \times 10^{6} M_{\odot}$ and $\Upsilon(R_{1/2}) = 5.8_{-2.6}^{+4.5} \times 10^{2} - 7.9_{-3.0}^{+5.5} \times 10^{2} M_{\odot} L_{\odot}^{-1}$ are about one standard deviation higher than this upper limit, which is likely related to the fact that we resolve an intrinsic velocity dispersion $\sigma_{\rm int} = 12.0_{-3.5}^{+5.0} \,\rm km \, s^{-1}$ that is significantly larger than the upper limit 4.5 km s⁻¹ of Kirby et al. (2015).

Gru 1 has constraints from Walker et al. (2016) on the mass within the half-light radius, $<2.5 \times 10^6 M_{\odot}$, and the total mass-to-light ratio, <2645. Our $M(R_{1/2}) = 1.1^{+2.1}_{-0.8} \times 10^6 - 1.7^{+2.9}_{-1.2} \times 10^6 M_{\odot}$ is fully consistent with this, but our $\Upsilon(r_{200}) = 7.4^{+60.2}_{-6.3} \times 10^3 - 3.2^{+33.9}_{-2.7} \times 10^4 M_{\odot} L_{\odot}^{-1}$ is an order of magnitude larger. A possible explanation for the significant differences in M_{200} and $\Upsilon(r_{200})$ for Leo T and Gru 1 is that the previous determinations were based on a bulk measurement of the intrinsic dispersion, while we determine a profile. As we discuss in Sect. 4.5.2, determining M_{200} (and by extension $\Upsilon(r_{200})$) from our profiles is hard already, and this is even more difficult when only a single dispersion is available.

Bonnivard et al. (2015a) determined astrophysical *J* and *D* factors – which are used to calculate the expected dark-matter annihilation and decay signal strength, respectively, as discussed in Sect. 4.4.2 – for a number of dwarf galaxies. These galaxies include Leo T, for which the calculated $\log_{10}(J(\alpha_c^J)/M_{\odot}^2 \text{kpc}^{-5}) = 10.7^{+0.5(+1.1)}_{-0.4(-0.8)}$ and $\log_{10}(D(\alpha_c^D)/M_{\odot} \text{kpc}^{-2}) =$ $2.1^{+0.4(+0.8)}_{-0.34}$ are very similar to our own $\log_{10}(J(\alpha_c^J)/M_{\odot}^2 \text{kpc}^{-5}) =$ $10.40^{+0.36}_{-0.34}$ -10.48^{+0.49}_{-0.36} and $\log_{10}(D(\alpha_c^D)/M_{\odot} \text{kpc}^{-2}) =$ $1.99^{+0.38}_{-0.33}$ $2.34^{+0.52}_{-0.34}$. The $\log_{10}(J(\alpha_c^J)/M_{\odot}^2 \text{kpc}^{-5}) =$ $11.91^{+0.44}_{-0.42}$ -12.02^{+0.50}_{-0.49} and $\log_{10}(D(\alpha_c^D)/M_{\odot} \text{kpc}^{-2}) = 3.17^{+0.51}_{-0.37}$ -3.45^{+0.60} of Hya II are similar to the highest measured for dwarf galaxies, which makes Hya II an interesting target for studies aiming to constrain dark-matter annihilation and decay (Alvarez et al., 2020; Bonnivard et al., 2015a). There is, however, the possibility of a bias of a factor of a few on the astrophysical factors when an incorrect halo triaxiality is assumed (Bonnivard et al., 2015b). The assumption in this paper is that the dark-matter haloes are spherical.

It is noticeable that, despite the generally weak evidence, the soliton is always the preferred model. Additionally, the cusp model is preferred over the core model in all four of the galaxies. For Eri 2 we found the same order of preference as for the galaxies in this paper. With $r_{\rm c} < 200-309$ pc (95% confidence levels), we rule out the large cores detected in some of the classical dwarf galaxies, for example $r_{\rm c} \approx 500$ pc for the dwarf irregular galaxies in the sample of Read et al. (2019).

4.5.2 Reliability of inferred parameters

Because r_{200} is larger than the radii of our most distant tracers by more than an order of magnitude, M_{200} is calculated through an intregral over a density profile that is extrapolated much beyond the measured range. If there is a bias in the profile slope, then the extrapolation can lead to a large bias in density, possibly becoming larger than the quoted random error. There is, therefore, an extra degree of uncertainty surrounding the calculated M_{200} , and it is therefore important to compare results obtained with different tools. We have seen that, while CJAM produces results that are inconsistent with the theoretical scaling relations involving M_{200} , the results of GravSphere are consistent. As we are in an as of yet unexplored mass regime, a difference between the observations and the extrapolations from more massive galaxies is however not necessarily alarming. The UFDs are deep into the territory of the missing satellites problem. It is therefore conceivable that the successful formation of a galaxy in such small haloes requires exceptional halo properties. On the other hand, our observations may be subject to selection effects, because the galaxies selected for MUSE-Faint are limited to those that can be covered in a few pointings with MUSE. It is not immediate how these selection effects influence our comparison to the theoretical scaling relations. To determine which values of M_{200} are correct, the ability of CJAM and GravSphere to recover unbiased parameters for UFDs needs to be tested with mock galaxies of the appropriate mass and with realistic numbers of measurements and measurement uncertainties. Meanwhile, to properly compare the results against theory, the scaling relations need to be extended with the results from high-resolution zoom-in simulations and need to take into account the observational selection functions in this regime. Both endeavours are beyond the scope of this paper.

The circular velocity $V(r_{1/2})$, by contrast, is derived from the mass in-

side the three-dimensional half-light radius, which is included in our data ranges. Therefore it should not be affected by a possible bias in the slope of the profile. We have confirmed this through the consistent circular velocities obtained with CJAM and GravSphere. As $V(r_{1/2})$, not V_{max} , is used as input for the procedure of Fattahi et al. (2018) to determine the amount of tidal stripping, the conclusions about stripping are similarly not significantly dependent on the modelling tool.

Because the assumed stellar mass-to-light ratios are derived from rough isochrone fits, there is an additional uncertainty for the stellar mass not included in the calculations. A change in stellar mass-to-light ratio by a factor of almost 2 did not significantly change the derived stripping parameters for Ant N, therefore this does not seem to be a major source of uncertainty for these results. This can be understood by the steepness of the $V_{\text{max}}^{\text{prog}} - M_*^{\text{prog}}$ relation, which means that even large changes in M_* do not bring the galaxy much closer to or further from the relation, therefore the inferred stripping will not be sensitive to M_* .

4.5.3 Reliability of the dynamical analysis

In the dynamical analysis we have implicitly assumed that the galaxies are in dynamical equilibrium. Though our results indicate that most, if not all, galaxies have not been significantly stripped of dark matter or stars, this does not prove dynamical equilibrium, as these results are obtained on the basis of this assumption. Regardless, it seems unlikely that galaxies on their first infall into the Milky Way, at >100 kpc distance, should have undergone significant stripping. To be more concrete, we estimate what the Jacobi radius (e.g. Binney & Tremaine, 2008, their Sect. 8.3.1) would be if Gru 1 would approach the Milky Way to $D_{\min} \approx 10$ kpc, which is the lower bound on the possible closest approach for any of our galaxies. Following Simon et al. (2011), we can estimate the Jacobi radius by taking the circular velocity of the Milky Way as $V_{\rm MW} = 220$ km s⁻¹. As the stripping parameter *x* measures whether the galaxy has been stripped of dark matter within its three-dimensional half-light radius, we take our Gru 1 measurement $M(r_{1/2}) \approx 10^{6.38} M_{\odot}$ as the satellite mass. The Jacobi radius is then

$$r_{\rm J} \approx \left(\frac{M(r_{\rm 1/2})}{3V_{\rm MW}^2 D_{\rm min}/G}\right)^{1/3} D_{\rm min} \approx 200 \,{\rm pc.}$$
 (4.20)

This is approximately equal to the three-dimensional half-light radius of Gru 1, $r_{1/2} = (4/3)R_{1/2} = 201^{+28}_{-41}$ pc (DES Collaboration, 2021a). It is therefore plausible that Gru 1 could have had its dark matter tidally stripped if the Milky Way follows the heavier model with $M_{200} = 1.6 \times 10^{12} M_{\odot}$. Its

larger ellipticity may be a hint of past tidal interaction. Jerjen et al. (2018) observed substructure in Gru 1, but this was aligned with the Large Magellanic Cloud. However, Gru 1 has not been close to the Large Magellanic Cloud according to Battaglia et al. (2022). On the other hand, in case of the light Milky Way model, where $D_{\min} \approx 100$ kpc, $r_{\rm J} \approx 900$ pc, which clearly rules out a significant tidal stripping within $r_{1/2}$. As the other four galaxies have $D_{\min} \gg 10$ kpc, we do not expect to see significant tidal stripping within $r_{1/2}$ for any of these galaxies.

The presence of binary star systems in the UFDs studied has the potential to bias the inferred intrinsic velocity dispersion. The barycentre of a binary star system traces the gravitational potential of the dark-matter halo of its host galaxy. However, when we measure the line-of-sight velocity of a star in a binary system, we see an additional contribution from the orbit of the star around the barycentre. By combining exposures from multiple epochs we effectively average over the velocity variation and obtain broadened spectral features with a mean at the barycentric velocity. For most of the galaxies presented here, we have collected data over periods of the order of a year or longer, which should mitigate the effects of binary stars with the shortest periods and consequently the largest velocities. Ant B is an exception: the data pertaining to this system was obtained over a few months. Though through the multi-epoch observations we attempt to address the worst effects of binary stars on the velocity dispersion, there is still little known about the populations of binary stars in UFDs, and therefore these stars remain a source of uncertainty.

4.6 CONCLUSIONS

We presented new observations of four (ultra-)faint dwarf galaxies, Ant B, Leo T, Hya II, and Gru 1, from the MUSE-Faint survey. We extracted stellar line-of-sight velocities, supplemented by literature velocities when available, and separated member stars from other sources. We resolved the velocity dispersion of Gru 1, which supports its classification as a galaxy. Through dynamical modelling with CJAM and GravSphere we constrained the dark-matter density profiles for these four galaxies for the first time. We used and compared cusp, core, and soliton models with CJAM and compared these with the cusp and core+tides models of GravSphere to determine whether our results are sensitive to the choice of modelling tool. We derived dynamical masses, concentrations, circular velocities, and astrophysical J and D factors from the profiles. We supplemented our galaxy sample with Eri 2, for which the CJAM dynamical modelling was done in Paper II of this series. Using the full sample of five galaxies, we furthermore compared the derived galaxy properties to expectations from theoretical

scaling relations and in that process determined how much tidal stripping these galaxies could have incurred.

We constrained the core radii of the four newly presented galaxies to $r_{\rm c}$ < 66–95 pc (68% confidence limit) or $r_{\rm c}$ < 200–309 pc (95% confidence limit). We constrained their soliton radii to $r_{\rm sol}$ < 13–112 pc (68% confidence limit) or $r_{\rm sol}$ < 0.25–1.58 kpc (95% confidence limit). These limits rule out cores of the size $r_{\rm c} \approx$ 500 pc as observed in more massive dwarf galaxies.

We find substantial Bayesian evidence (Bayes factor $10^{-0.53}$) against the core model for Leo T. The most preferred model for all galaxies is the soliton model. However, the evidence against the other models is weak, except for the aforementioned Leo T result, and we have insufficient evidence to decisively discriminate between the models for the analysed galaxies.

We find the highest values of $M_{200} = 4.2^{+33.9}_{-3.3} \times 10^8 - 1.5^{+18.6}_{-1.3} \times 10^9 M_{\odot}$ and $V_{\text{max}} = 24^{+18}_{-11} - 31^{+29}_{-12} \text{ km s}^{-1}$ for Hya II, while this is one of the fainter galaxies. The astrophysical factors $\log_{10}(J(\alpha_c^J)/M_{\odot}^2 \text{ kpc}^{-5}) = 11.91^{+0.44}_{-0.42} - 12.02^{+0.50}_{-0.49}$ and $\log_{10}(D(\alpha_c^D)/M_{\odot} \text{ kpc}^{-2}) = 3.17^{+0.51}_{-0.37} - 3.45^{+0.60}_{-0.44}$ are equivalently high for Hya II, which makes this an interesting target for studies that search for annihilation or decay signals of dark-matter particles.

We find that according to the theoretical expectations for isolated galaxy evolution and evolution after infall into the Milky Way halo, the galaxies are consistent with not having been significantly tidally stripping of dark matter within their half-light radii. This is consistent with the large distance between these satellites and the Milky Way, now and in the past. Only Gru 1 may have come close to the Milky Way, and is also indicated as the most stripped galaxy. The $V(r_{1/2})$ that these calculations are based on, are consistent between CJAM and GravSphere, as are the derived stripping parameters.

All five galaxies have a larger c_{200} than predicted for their M_{200} according to CJAM. The M_{200} is lower than expected given the M_* of these galaxies. GravSphere does produce results consistent with the theoretical scaling relations. In this case, the UFDs are consistent with $M_{200} \sim 10^9 M_{\odot}$, which is expected from models in which the smallest dwarf galaxies are re-ionization fossils. The M_{200} and c_{200} are easily biased, because their calculations rely on a large extrapolation of the density profiles to larger radii. This is also apparent in the different results produced by CJAM and Grav-Sphere. Expectations can, however, turn out to be false, therefore we cannot conclude from these results that GravSphere gives more correct results than CJAM. Further tests are required to determine which of the dynamical modelling tools provides the least biased results.

The determination of dark-matter density profiles for UFDs has only just begun. MUSE-Faint has so far provided us with velocity measurements in the centres of five faint and ultra-faint systems. With the current gener-

ation of instruments, improving on the measurements used in this paper will be expensive. Increasing the number of stars in the centres could lead to stronger constraints on cores and solitons, but will require a significant time investment. Higher-resolution spectroscopy of the central stars is also impractical with current instruments because of the crowdedness of these fields. If a future instrument could marry the spatial resolution of an integral-field spectrograph with the specral resolution of a fibre spectrograph, this would greatly improve the measurement uncertainties on the line-of-sight velocities. On the other hand, larger samples of stars at larger radii, potentially improving the constraints on the virial mass, are difficult to realize because the stellar surface density rapidly decreases outside the half-light radius. There is, however, a large number of UFDs with centres still unexplored with spectroscopy. Increasing the sample of UFDs with dark-matter density profiles will offer a more complete view of the properties of the faintest galaxies and how these relate to theory. We also hope that, with the increasing resolution of galaxy formation simulations, the theoretical scaling relations can be expanded into the ultra-faint regime. To properly compare the virial parameters of UFDs against such scaling relations, tests of different dynamical modelling tools against mock UFDs are required to determine their biases. Finally, in a follow-up paper we will study the consequences of the density profiles presented here for the nature and properties of dark matter.

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Based on observations made with ESO Telescopes at the La Silla Paranal Observatory under programme IDs 0100.D-0807, 0101.D-0300, 0102.D-0372, 0103.D-0705, and 0104.D-0199.

This research has made use of Astropy (Astropy Collaboration et al., 2018, 2013), corner.py (Foreman-Mackey, 2016), matplotlib (Hunter, 2007), NASA's Astrophysics Data System Bibliographic Services, NumPy (Harris et al., 2020), SciPy (Virtanen et al., 2020), and the colour schemes of Tol (2018).

This work has made use of data from the European Space Agency

(ESA) mission *Gaia* (https://www.cosmos.esa.int/gaia), processed by the *Gaia* Data Processing and Analysis Consortium (DPAC, https: //www.cosmos.esa.int/web/gaia/dpac/consortium). Funding for the DPAC has been provided by national institutions, in particular the institutions participating in the *Gaia* Multilateral Agreement.

Based on observations made with the NASA/ESA Hubble Space Telescope, and obtained from the Hubble Legacy Archive, which is a collaboration between the Space Telescope Science Institute (STSCI/NASA), the Space Telescope European Coordinating Facility (ST-ECF/ESA) and the Canadian Astronomy Data Centre (CADC/NRC/CSA).

This research has made use of the NASA/IPAC Extragalactic Database (NED), which is funded by the National Aeronautics and Space Administration and operated by the California Institute of Technology.

APPENDICES

4.A GRAVSPHERE

To test the robustness of our fiducial CJAM results against the choice of dynamical modelling tool, we present here the results of an alternative tool, GravSphere. GravSphere differs from CJAM in that it bins the velocity measurements and breaks the resulting degeneracy between density and anisotropy by also constraining higher velocity moments in the form of the virial shape parameters. It also allows for a radially varying velocity anisotropy profile.

The presentation of the GravSphere results follows a similar structure as for CJAM. In Figs. 4.B.4-4.B.13 we display the posteriors of the GravSphere models on the dark-matter parameters. We do not show the Plummer parameters of the stellar distribution to limit the size of the figures. M_{200} and c_{200} , or M_{200}^{prog} and c_{200}^{prog} , are well-constrained to values of $\sim 10^9 M_{\odot}$ and 17-19, respectively, for most galaxies. Hya II is noticeably more massive $(\sim 10^{11} M_{\odot})$ and less concentrated (12–13). The core and tide parameters r_{c} , *n*, $r_{\rm t}$, and δ are unconstrained and consistent with a cuspy profile, though core sizes larger than 1 kpc are allowed by the 95% upper limits for all galaxies. For most galaxies the anisotropy profile in unconstrained and consistent with isotropy. Ant B has a significant tangential anisotropy in its centre and Hya II has a non-significant preference for tangential anisotropy at all radii. There is no visible correlation between the anisotropy and the other parameters, therefore the anisotropy profiles should not influence our results. This also supports our choice for isotropy in the CJAM modelling: anisotropy is not expected to change the CJAM results. The central tangential anisotropy of Ant B will be further studied by Júlio et al. (in prep.).

From the posteriors we derive the profiles shown in Figs. 4.A.1 and 4.A.2 together with the CJAM cuspy profile for reference. The GravSphere profiles show generally the same features: the profile uncertainties are smallest and the agreement between the profiles is the best where the tracer density is highest, and the divergence between the profiles increases towards the centre. There are, however, two noticeable differences. The GravSphere profiles have smaller uncertainties than the CJAM profiles, with the difference being particularly strong between the two cusp models. Secondly, GravSphere systematically prefers shallower profiles.

We derive the same quantities from the GravSphere profiles as from the CJAM profiles and list these in Table 4.A.1. The M_{200} and c_{200} values in this Table are calculated by integrating the profiles, as was done for CJAM, and are not taken from the set of profile parameters. For the core+tides model, the M_{200} calculated here are clearly lower than the M_{200}^{prog} profile parameters that represent the virial mass of the progenitor profile. Hya II has a significantly higher M_{200} and V_{max} than the other galaxies, qualitatively similar to what we found with CJAM. The large-scale parameters are all noticeably higher than their CJAM counterparts, except for the lower c_{200} , whereas the parameters measured at or within the half-light radii are consistent between the two methods.

To compare the two GravSphere models, we estimate the Bayesian evidence with MCEvidence (Heavens et al., 2017), as we did in Paper II for the pyGravSphere models. We display the estimated evidence in Table 4.A.2. For all galaxies, the cusp model is substantially, but not significantly, preferred over the core+tides model.

We perform the same stripping analysis on the cusp model of GravSphere as on that of CJAM. We are again successful in finding a progenitor solution for all five galaxies and display the progenitor properties in Table 4.A.3. We compare the stripping parameters against the closest distances to the Milky Way ever reached in Fig. 4.A.3. This comparison paints a very consistent picture to the CJAM stripping analysis. All galaxies are again consistent with having undergone no stripping. The uncertainties for GravSphere are smaller than for CJAM, and in the case of GravSphere the Gru 1 results are no longer compatible with a more significant amount of stripping than the other satellites.

As a result of the systematically different M_{200} and c_{200} , the comparisons of the GravSphere results against the galaxy–halo scaling relations look very different than that of the CJAM results. These comparisons are show in Figs. 4.5 and 4.6 and discussed in Sect. 4.4.5.



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FIGURE 4.A.2: Recovered darkmatter density profiles of the ultra-faint dwarf galaxy Eridanus 2, for cusp and core+tides profiles, modelled with Grav-Sphere, with the CJAM cusp profile for reference. The hatched bands indicate the 68% confidence interval on the density at each radius. The central. thicker line is the median density at each radius. The galaxy's projected half-light radii are indicated with the vertical dashed lines. The markers along the bottom of each panel indicate the projected radii of the kinematic tracers.

FIGURE 4.A.1 (FACING PAGE): Recovered dark-matter density profiles of the (ultra-)faint dwarf galaxies Antlia B, Leo T, Hydra II, and Grus 1, for cusp and core+tides profiles, modelled with GravSphere, with the CJAM cusp profiles for reference. The hatched bands indicate the 68% confidence interval on the density at each radius. The central, thicker line is the median density at each radius. The galaxy's projected half-light radii are indicated with the vertical dashed lines. The markers along the bottom of each panel indicate the projected radii of the kinematic tracers.

TABLE 4.A.1: Parameters derived from the recovered dark-matter density profiles from GravSphere.

	Ant B	Leo т	Eri 2	
	cusp core+tides	cusp core+tides	cusp core+tides	
$\log_{10}(V_{\rm max}/{\rm kms^{-1}})$	$1.36^{+0.10}_{-0.08}$ $1.38^{+0.10}_{-0.08}$	$1.38^{+0.19}_{-0.18}$ $1.39^{+0.17}_{-0.17}$	$1.28^{+0.07}_{-0.06}$ $1.30^{+0.07}_{-0.06}$	
$\log_{10}(r_{200}/\text{kpc})$	$1.38^{+0.13}_{-0.11}$ $1.30^{+0.14}_{-0.12}$	$1.40_{-0.20}^{+0.23}$ $1.30_{-0.17}^{+0.19}$	$1.30^{+0.09}_{-0.08}$ $1.24^{+0.10}_{-0.10}$	
$\log_{10}(c_{200})$	$1.26^{+0.12}_{-0.12}$ $1.14^{+0.17}_{-0.22}$	$1.24_{-0.15}^{+0.14}$ $1.15_{-0.27}^{+0.19}$	$1.26^{+0.11}_{-0.10}$ $1.18^{+0.14}_{-0.19}$	
$\log_{10}(M_{200}/M_{\odot})$	$9.17_{-0.33}^{+0.38}$ $8.92_{-0.36}^{+0.42}$	$9.23_{-0.61}^{+0.68}$ $8.93_{-0.50}^{+0.57}$	$8.92_{-0.24}^{+0.27}$ $8.73_{-0.28}^{+0.31}$	
$\log_{10}(Y(r_{200})/M_{\odot}L_{\odot}^{-1})$	$3.37_{-0.33}^{+0.38}$ $3.12_{-0.36}^{+0.42}$	$4.27_{-0.61}^{+0.68}$ $3.97_{-0.50}^{+0.57}$	$4.16_{-0.24}^{+0.27}$ $3.96_{-0.28}^{+0.31}$	
$\log_{10}(V(R_{1/2})/\text{km s}^{-1})$	$1.16^{+0.04}_{-0.04}$ $1.15^{+0.04}_{-0.05}$	$1.05^{+0.06}_{-0.07}$ $1.04^{+0.06}_{-0.07}$	$1.08^{+0.04}_{-0.03}$ $1.07^{+0.04}_{-0.04}$	
$\log_{10}(M(R_{1/2})/M_{\odot})$	$7.13_{-0.08}^{+0.08}$ $7.11_{-0.09}^{+0.08}$	$6.65_{-0.14}^{+0.12}$ $6.62_{-0.15}^{+0.12}$	$6.92^{+0.07}_{-0.07}$ $6.90^{+0.08}_{-0.09}$	
$\log_{10}(Y(R_{1/2})/M_{\odot}L_{\odot}^{-1})$	$1.63^{+0.08}_{-0.08}$ $1.61^{+0.08}_{-0.09}$	$1.99_{-0.14}^{+0.12}$ $1.96_{-0.15}^{+0.12}$	$2.46^{+0.07}_{-0.07}$ $2.44^{+0.08}_{-0.09}$	
$\log_{10}(V(r_{1/2})/\text{km s}^{-1})$	$1.20^{+0.04}_{-0.04}$ $1.19^{+0.04}_{-0.04}$	$1.10^{+0.06}_{-0.07}$ $1.09^{+0.06}_{-0.07}$	$1.13^{+0.03}_{-0.03}$ $1.12^{+0.03}_{-0.04}$	
$\log_{10}(M(r_{1/2})/M_{\odot})$	$7.34_{-0.08}^{+0.08}$ $7.33_{-0.09}^{+0.08}$	$6.88^{+0.13}_{-0.15}$ $6.87^{+0.13}_{-0.15}$	$7.14_{-0.06}^{+0.07}$ $7.13_{-0.07}^{+0.07}$	
$\log_{10}(J(\alpha_{\rm c}^J)/M_{\odot}^2{\rm kpc^{-5}})$	$9.49_{-0.17}^{+0.16}$ $9.48_{-0.17}^{+0.16}$	$10.44_{-0.35}^{+0.31}$ $10.44_{-0.35}^{+0.31}$	$10.38_{-0.13}^{+0.13}$ $10.37_{-0.13}^{+0.12}$	
$\log_{10}(D(\alpha_c^D)/M_{\odot} \text{ kpc}^{-2})$	$1.90^{+0.21}_{-0.19}$ $1.83^{+0.21}_{-0.17}$	$2.71_{-0.37}^{+0.39}$ $2.63_{-0.32}^{+0.33}$	$2.80_{-0.13}^{+0.15} 2.76_{-0.12}^{+0.15}$	

H	ya 11	Gı	u 1
cusp	core+tides	cusp	core+tides
$1.85_{-0.24}^{+0.27}$	$1.78^{+0.20}_{-0.18}$	$1.15_{-0.19}^{+0.23}$	$1.17_{-0.20}^{+0.25}$
$1.92^{+0.30}_{-0.28}$	$1.62^{+0.25}_{-0.21}$	$1.16^{+0.26}_{-0.21}$	$1.12_{-0.20}^{+0.22}$
$1.15_{-0.16}^{+0.22}$	$0.81_{-0.47}^{+0.32}$	$1.29_{-0.14}^{+0.13}$	$1.23_{-0.23}^{+0.16}$
$10.78_{-0.83}^{+0.91}$	$9.90^{+0.74}_{-0.62}$	$8.51_{-0.62}^{+0.78}$	$8.40^{+0.66}_{-0.59}$
$6.91_{-0.83}^{+0.91}$	$6.03_{-0.62}^{+0.74}$	$4.95_{-0.62}^{+0.78}$	$4.83_{-0.59}^{+0.66}$
$1.07^{+0.06}_{-0.07}$	$1.06^{+0.07}_{-0.08}$	$0.94_{-0.10}^{+0.10}$	$0.89^{+0.12}_{-0.15}$
$6.36_{-0.14}^{+0.12}$	$6.34_{-0.15}^{+0.13}$	$6.42^{+0.20}_{-0.20}$	$6.32_{-0.30}^{+0.25}$
$2.79_{-0.14}^{+0.12}$	$2.78^{+0.13}_{-0.15}$	$3.16^{+0.20}_{-0.20}$	$3.06^{+0.25}_{-0.30}$
$1.12_{-0.07}^{+0.06}$	$1.12_{-0.07}^{+0.06}$	$0.98^{+0.10}_{-0.11}$	$0.89_{-0.15}^{+0.12}$
$6.60_{-0.14}^{+0.12}$	$6.59_{-0.15}^{+0.13}$	$6.64_{-0.22}^{+0.21}$	$6.32_{-0.30}^{+0.25}$
$12.04_{-0.34}^{+0.32}$	$12.07_{-0.34}^{+0.31}$	$10.91_{-0.49}^{+0.50}$	$10.82_{-0.56}^{+0.55}$
$4.22_{-0.48}^{+0.51}$	$3.92^{+0.40}_{-0.35}$	$3.28^{+0.48}_{-0.41}$	$3.24_{-0.42}^{+0.46}$

NOTES: V_{max} : maximum circular velocity; r_{200} : virial radius; c_{200} : concentration parameter; M_{200} : virial mass; Y(r): mass-to-light ratio integrated within radius r; V(r): circular velocity at radius r; $R_{1/2}$: projected half-light radius; M(r): mass within radius r; $r_{1/2}$: three-dimensional half-light radius; $J(\alpha_c^J)$: astrophysical J factor within its critical angle; $D(\alpha_c^D)$: astrophysical D factor within its critical angle.

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ż	2
U.G.J	2
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<	¢
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TABLE 4.A.2: Bayesian evidence and Bayes factors for GravSphere.

	AI	nt B	Ľ	EO T	Ë	ri 2	Hy	'a II	ΰ	ru 1
	cusp (core+tides	cusp	core+tides	cusp	core+tides	cusp	core+tides	cusp	core+tides
$\ln(Z)$	-287.43	-288.88	-291.89	-293.63	-391.59	-392.78	-295.97	-297.48	-269.83	-271.11
$\Delta \log_{10}(Z)$	0	-0.62	0	-0.76	0	-0.52	0	-0.66	0	-0.56

NOTES: $\ln(Z)$: natural logarithm of the Bayesian evidence Z; $\Delta \log_{10}(Z)$: decimal logarithm of the Bayes factor, or difference of the decimal logarithms of Bayesian evidence, relative to the best-fitting model of each galaxy.

	Ant B	Leo T	Eri 2	Hya II	Gru 1
$\log_{10}(M_*^{ m prog}/M_{\odot})$	$5.87_{-0.00}^{+0.10}$	$5.14_{-0.00}^{+0.07}$	$4.95_{-0.01}^{+0.10}$	$4.28_{-0.00}^{+0.00}$	$3.80_{-0.02}^{+0.16}$
$\log_{10}(V_{\rm max}^{\rm prog}/{\rm kms^{-1}})$	$1.45_{-0.07}^{+0.09}$	$1.40_{-0.06}^{+0.07}$	$1.39_{-0.05}^{+0.07}$	$1.35_{-0.04}^{+0.06}$	$1.33_{-0.04}^{+0.05}$
$\log_{10}(r_{1/2}^{\text{prog}}/\text{kpc})$	$-0.42_{-0.06}^{+0.06}$	$-0.67_{-0.06}^{+0.06}$	$-0.48_{-0.06}^{+0.05}$	$-0.97_{-0.07}^{+0.08}$	$-0.70_{-0.06}^{+0.06}$
$\log_{10}(V_{\rm prog}(r_{1/2}^{\rm prog})/{\rm kms^{-1}})$	$1.19_{-0.07}^{+0.08}$	$1.07_{-0.07}^{+0.10}$	$1.12_{-0.06}^{+0.08}$	$1.04_{-0.12}^{+0.14}$	$1.00_{-0.07}^{+0.09}$
$\log_{10}(x)$	$0.01_{-0.15}^{+0.12}$	$0.03_{-0.15}^{+0.13}$	$0.00^{+0.12}_{-0.14}$	$0.12_{-0.19}^{+0.16}$	$-0.04_{-0.19}^{+0.15}$
$\log_{10}(\mu_L)$	$0.01_{-0.10}^{+0.00}$	$0.02_{-0.07}^{+0.00}$	$0.01_{-0.10}^{+0.01}$	$0.02_{-0.00}^{+0.00}$	$0.00^{+0.02}_{-0.16}$

TABLE 4.A.3: Progenitor properties based on GravSphere, according to the method of Fattahi et al. (2018).

NOTES: M_*^{prog} : progenitor stellar mass; $V_{\text{max}}^{\text{prog}}$: progenitor maximum circular velocity; $r_{1/2}^{\text{prog}}$: progenitor three-dimensional half-light radius; $V_{\text{prog}}(r_{1/2}^{\text{prog}})$: progenitor circular velocity within the progenitor three-dimensional half-light radius; $x_{\text{prog}}(r_{1/2}^{\text{prog}})$: progenitor circular velocity within the progenitor three-dimensional half-light radius; $x_{\text{prog}}(r_{1/2})$: progenitor circular velocity within the progenitor three-dimensional half-light radius; $r_{\text{prog}}(r_{1/2})$: progenitor circular velocity within the progenitor three-dimensional half-light radius; $r_{\text{prog}}(r_{1/2})$ is progenitor circular velocity within the progenitor three-dimensional half-light radius. within the progenitor three-dimensional half-light radius in the present-day galaxy, versus the dark-matter mass within the progenitor three-dimensional half-light radius in the progenitor galaxy; μ_L : fraction of the stellar mass of the present-day galaxy, versus the stellar mass of the progenitor galaxy.



FIGURE 4.A.3: Stripping parameters of the galaxies, as determined with GravSphere, versus their closest distance to the Milky Way ever reached. The stripping parameters x and μ_L are measures of the fraction of dark matter and stars retained after stripping; lower values indicate more stripping has occurred. We show results for two models of the Milky Way that differ in the halo mass. In most cases, the closest distance is not the pericentre distance but the current distance, as most of these galaxies are still in their first infall. We note that Antlia B is a satellite of NGC 3109, not of the Milky Way, and that its distance to the Milky Way is therefore not relevant for its stripping parameters; its display in this figure is merely illustrative.

4.B FIGURES OF PARAMETER CONSTRAINTS

In this appendix we display the constraints on the parameters of the darkmatter density profiles. Figure 4.B.1 shows the constraints on the CJAM cusp model for each galaxy, Fig. 4.B.2 on the CJAM core model, and Fig. 4.B.3 on the CJAM soliton model. We show the constraints on the GravSphere cusp model in Figs. 4.B.4–4.B.8 and on the GravSphere core+tides model in Figs. 4.B.9–4.B.13, also for Eri 2.



FIGURE 4.B.1: Constraints on the dark-matter density profiles of the four (ultra-)faint dwarf galaxies, for the cusp model, modelled with CJAM. Units are omitted from the labels for clarity. The parameters are the characteristic dark-matter density ρ_0 in M_{\odot} kpc⁻³, the scale radius r_s in kpc, and the systemic velocity v_0 in km s⁻¹. The contours correspond to 0.5σ , 1.0 σ , 1.5 σ , and 2.0 σ confidence levels, where σ is the standard deviation of a twodimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval.







FIGURE 4.B.2: Constraints on the dark-matter density profiles of the four (ultra-)faint dwarf galaxies, for the core model, modelled with CJAM. Units are omitted from the labels for clar-The parameters are the ity. characteristic dark-matter density ho_0 in M_\odot kpc⁻³, the scale radius $r_{\rm s}$ and core radius $r_{\rm c}$ in kpc, and the systemic velocity v_0 in km s⁻¹. The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval (without arrows) or the 68% and 95% confidence limits (upper and lower arrows, respectively).







FIGURE 4.B.3: Constraints on the dark-matter density profiles of the four (ultra-)faint dwarf galaxies, for the soliton model, modelled with CJAM. Units are omitted from the labels for clarity. The parameters are the characteristic dark-matter density $\rho_{\rm cusp,0}$ in $M_{\odot}\,{\rm kpc^{-3}}$ and the scale radius $r_{\rm s}$ in kpc of the large-scale, cusp-like component, the central density $ho_{
m sol,0}$ in M_{\odot} kpc⁻³ of the soliton, the soliton radius $r_{\rm sol}$ in kpc, and the systemic velocity v_0 in km s⁻¹. The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval (without arrows) or the 68% and 95% confidence limits (upper and lower arrows, respectively).









FIGURE 4.B.4: Constraints on the dark-matter density profiles of Antlia B, for the cusp model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the virial mass M_{200} in M_{\odot} , the concentration parameter c_{200} , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval.



FIGURE 4.8.5: Constraints on the dark-matter density profiles of Leo T, for the cusp model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the virial mass M_{200} in M_{\odot} , the concentration parameter c_{200} , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval.



FIGURE 4.8.6: Constraints on the dark-matter density profiles of Eridanus 2, for the cusp model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the virial mass M_{200} in M_{\odot} , the concentration parameter c_{200} , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval.



FIGURE 4.B.7: Constraints on the dark-matter density profiles of Hydra II, for the cusp model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the virial mass M_{200} in M_{\odot} , the concentration parameter c_{200} , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval.



FIGURE 4.B.8: Constraints on the dark-matter density profiles of Grus 1, for the cusp model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the virial mass M_{200} in M_{\odot} , the concentration parameter c_{200} , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval.



FIGURE 4.8.9: Constraints on the dark-matter density profiles of Antlia B, for the core+tides model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the progenitor virial mass M_{200}^{prog} in M_{\odot} , the progenitor concentration parameter c_{200}^{prog} , the core radius r_c in kpc, the coredness parameter n, the tidal radius r_t in kpc, the negative logarithmic density slope δ beyond r_t , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval (without arrows) or the 68% and 95% confidence limits (upper and lower arrows, respectively).



FIGURE 4.B.10: Constraints on the dark-matter density profiles of Leo T, for the core+tides model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the progenitor virial mass M_{200}^{prog} in M_{\odot} , the progenitor concentration parameter c_{200}^{prog} , the core radius r_c in kpc, the coredness parameter n, the tidal radius r_t in kpc, the negative logarithmic density slope δ beyond r_t , the inner symmetrized anisotropy β_0 and outer symmetrized anisotropy β_{∞} , the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval (without arrows) or the 68% and 95% confidence limits (upper and lower arrows, respectively).



FIGURE 4.B.11: Constraints on the dark-matter density profiles of Eridanus 2, for the core+tides model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the progenitor virial mass M_{200}^{prog} in M_{\odot} , the progenitor concentration parameter c_{200}^{prog} , the core radius r_c in kpc, the coredness parameter n, the tidal radius r_t in kpc, the negative logarithmic density slope δ beyond r_t , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval (without arrows) or the 68% and 95% confidence limits (upper and lower arrows, respectively).


FIGURE 4.B.12: Constraints on the dark-matter density profiles of Hydra II, for the core+tides model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the progenitor virial mass M_{200}^{prog} in M_{\odot} , the progenitor concentration parameter c_{200}^{prog} , the core radius r_c in kpc, the coredness parameter n, the tidal radius r_t in kpc, the negative logarithmic density slope δ beyond r_t , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval (without arrows) or the 68% and 95% confidence limits (upper and lower arrows, respectively).



FIGURE 4.8.13: Constraints on the dark-matter density profiles of Grus 1, for the core+tides model, modelled with GravSphere. Units are omitted from the labels for clarity. The parameters are the progenitor virial mass M_{200}^{prog} in M_{\odot} , the progenitor concentration parameter c_{200}^{prog} , the core radius r_c in kpc, the coredness parameter n, the tidal radius r_t in kpc, the negative logarithmic density slope δ beyond r_t , the inner symmetrized anisotropy $\tilde{\beta}_0$ and outer symmetrized anisotropy $\tilde{\beta}_{\infty}$, the anisotropy transition radius r_0 in kpc, and the anisotropy transition rapidity η . The contours correspond to 0.5σ , 1.0σ , 1.5σ , and 2.0σ confidence levels, where σ is the standard deviation of a two-dimensional normal distribution. The vertical dashed lines in the one-dimensional histograms indicate the median and the 68% confidence interval (without arrows) or the 68% and 95% confidence limits (upper and lower arrows, respectively).