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Prediction of contralateral breast cancer: statistical aspects and prediction performance

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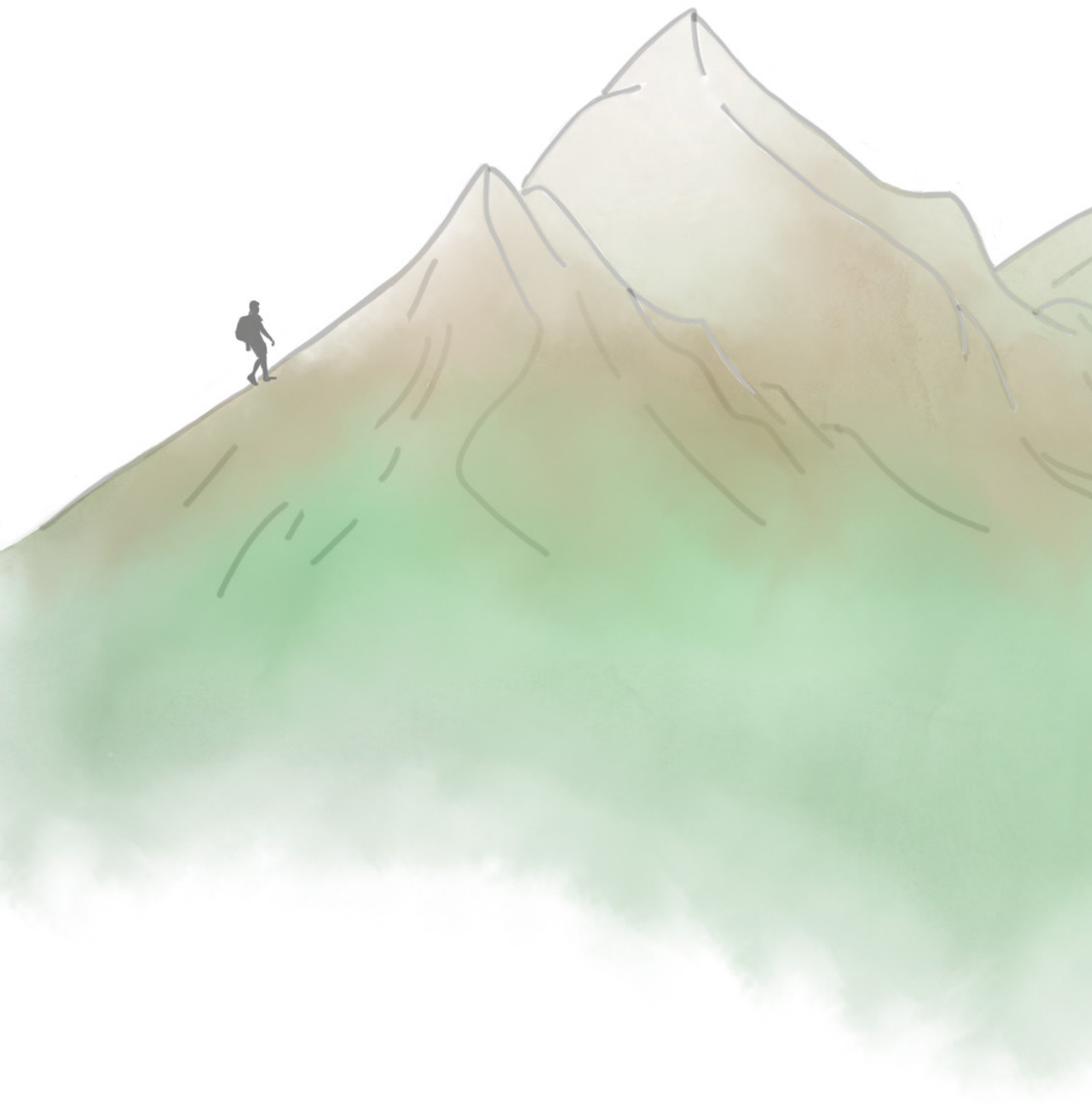
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Chapter 1

Introduction



INTRODUCTION

Breast cancer: developments and contemporary challenges

Breast cancer is the most common cancer in women in the world¹. While the incidence of breast cancer has increased over the years, survival after breast cancer diagnosis has improved in the last 50 years due to earlier detection and advanced treatment modalities; for example, in the Netherlands, 10-year survival of first primary breast cancer approximately improved by almost 40% from 39% in 1961 to 76% in 2010^{2,3}. As a consequence, breast cancer survivors may have substantial remaining lifetime to develop other cancers.

Breast cancer survivors are more likely to develop a new primary tumor in the opposite breast (defined as contralateral breast cancer) compared to healthy women to develop a first primary breast cancer⁴⁻⁸. Contralateral breast cancer is one of the biggest threats among breast cancer survivors: for example, in the Netherlands and in the United States contralateral breast cancer is the most common second primary cancer among women diagnosed with invasive breast cancer, accounting for 40-50% of all new second cancers^{9,10}. About 5 out of 100 patients with invasive breast cancer will develop a contralateral breast cancer within 10 years since the diagnosis of the first primary breast cancer (10-year cumulative incidence between 4-7%, Figure 1)^{11,12}. In addition, contralateral breast cancer patients have worse prognosis compared to patients with unilateral breast cancer¹³⁻¹⁶. Little is known about contralateral breast cancer among patients diagnosed with in situ breast cancer, a potential pre-invasive cancer occurring typically in the cell of milk ducts or lobules of the breast¹⁷.

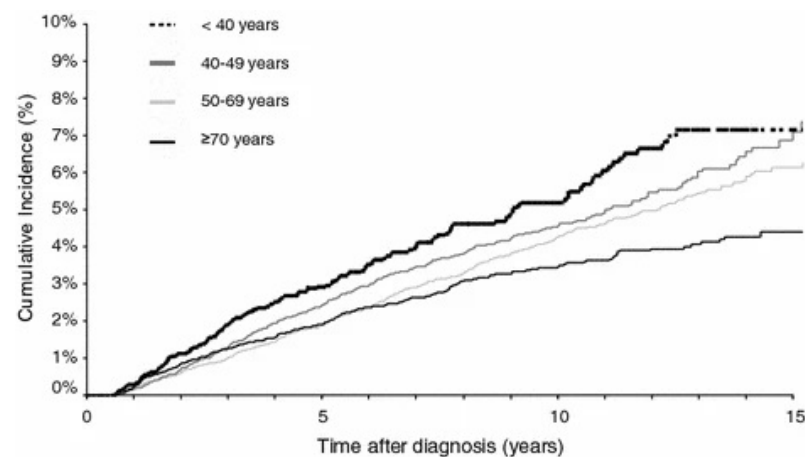


Figure 1: Cumulative incidence of contralateral breast cancer (CBC) by age and time since diagnosis (Data source: Netherlands Cancer Registry, N=45,229 index cancers; N=1,477 CBC¹⁴, reproduced with permission of Breast Cancer Research and Treatment)

Contralateral breast cancer prevention: the preventive mastectomy

Although contralateral breast cancer risk is relatively low, an increasing number of patients with first breast cancer opt for a contralateral preventive mastectomy¹⁸. The rationale behind the contralateral preventive mastectomy is to avoid contralateral breast cancer with the consequent treatments and to potentially prevent death from a secondary primary breast cancer¹⁹. Among patients with highly elevated breast cancer risk contralateral preventive mastectomy is recommended, especially in patients with genetic predisposition or strong family history of breast cancer^{20,21}. Currently, the contralateral preventive mastectomy is recommended in patients with germline mutations in *BRCA1* and *BRCA2* genes, although mutations in other breast cancer risk genes (*CHEK2*, *ATM* and *PALB2*) are suggested to also be associated with contralateral breast cancer risk²²⁻²⁵. The 10-year contralateral breast cancer risk in women with *BRCA1/2* germline mutations was estimated between 20-30% (Figure 2)^{20-22,26}. Although the contralateral breast cancer risk is considerably high in women with *BRCA1/2* germline mutation, only between 1-5% of the European-descent general breast cancer population has a mutation in these genes^{20,22,27}. Consequently, the choice of contralateral preventive mastectomy remains still debatable in a large part of general breast cancer population without any genetic predisposition. Furthermore, the increasing usage of (neo)adjuvant systemic therapies (chemo and endocrine therapy), intended to prevent breast cancer recurrences, has also been demonstrated to indirectly reduce the risk/incidence of contralateral breast cancer^{12,18}.

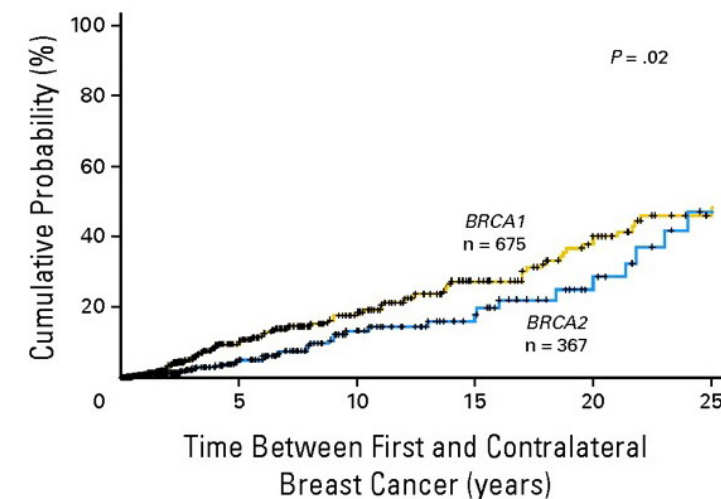


Figure 2: cumulative incidence of contralateral breast cancer in patients with *BRCA1/2* germline mutation (Data source: the German Consortium for Hereditary Breast and Ovarian Cancer, N=1,042; CBC=135²⁶, reproduced with permission from Journal of Clinical Oncology)

Decision-making for mastectomy

Psychological factors play a substantial role in a patient's decision regarding contralateral preventive mastectomy and in the outcome perceptions^{18,28,29}. The risk reducing benefit of the surgery is commonly recognized. Contralateral preventive mastectomy mostly avoids a new breast cancer diagnosis and the subsequent new treatments^{18,28}. As a consequence, contralateral preventive mastectomy might improve survival of first breast cancer patients. On the other hand, this intervention is not without negative consequences: approximately 30 out of 100 of women experience difficulties with body image, feminine identity, and sexual intimacy after surgery¹⁸. In addition, about 15-20% of patients who undergo contralateral preventive mastectomy may experience postoperative complications leading to higher medical costs and a potential lower quality of life²⁹⁻³¹. Contralateral preventive mastectomy complications at (or about) the time of first breast cancer diagnosis may cause delays in initiating adjuvant systemic therapies increasing chance of breast cancer recurrences^{29,30}. The benefit of avoiding the potential subsequent second breast cancer treatments should be correctly weighed against the costs of a negative body image and the potential postoperative complications. This harm and costs evaluation may be important during the consultation between patients and physicians to take a decision about the contralateral preventive mastectomy.

What is the role for prediction models in contralateral breast cancer prevention?

An appropriate risk prediction is crucial to more objectively quantify harms and benefit for a clinical decision making. Individualized contralateral risk prediction might help shared decision-making of physicians and patients about prevention strategies for those at high contralateral breast cancer risk, and to avoid unnecessary contralateral preventive mastectomies when contralateral breast cancer risk is low. Thus, contralateral breast cancer risk should be formally calculated to help patients and physicians during the decision making process towards preventive strategies, especially regarding contralateral preventive mastectomy¹⁹. This ambition may be successfully achieved under several conditions. First of all, the predicted risks should be sufficiently accurate and reliable. Good quality of data and performance assessment of the predicted risks is essential to evaluate prediction accuracy or to investigate the reasons causing inaccurate estimations. Secondly, the expected benefit of a clinical decision should be precisely quantified weighing pros and cons regarding preventive strategies. Last but not least, as long as predictions are accurate and the expected benefit is properly quantified, risk communication is really important in informing patients and physicians. Different methods of risk visualization may facilitate risk communication and the use of prediction tools in clinical practice³².

Regression is the most widely statistical technique used to develop a risk prediction model and to provide absolute risk prediction³³. A risk prediction model exploits the relation between predictors and the outcome of interest in a representative sample of patients. In

many cancer studies, the main outcome of interest is time until an event occurs, generally known as survival time. The methods considering survival time as outcome are defined as survival analysis³⁴. However, when the event (e.g., death) does not occur in all individuals by the end of the follow-up, the true survival time is not known. This analytical problem is defined as censoring. Typically, censoring occurs when: a person does not experience the event of interest before the study ends, a person is lost to follow-up during the study, or a person withdraws from the study. The latter may happen when a competing event occurs. Let contralateral breast cancer event be the event of interest, patients may withdraw from the study because of dying. Therefore, death is a competing event that precludes the contralateral breast cancer from happening. Statistical models accounting for both censoring, and competing risks exist and are widely used in clinical practice such as in cardiology and oncology³⁵⁻³⁷. The most common statistical regression models for survival analysis with or without competing risks are the Cox proportional hazard regression and the Fine and Gray regression model³⁷.

Evaluation of performance and utility of risk prediction models

The statistical performance of a risk prediction model is important to validly support decision-making. A risk prediction model's performance is measured usually in terms of discrimination and calibration. The former is the ability of the model to identify subjects with good outcome and with poor outcome^{38,39}. The latter is the agreement between observed and predicted outcome³⁸. Both can be evaluated in the development data as internal validation or in independent data as external validation. The latter assessment provides an indication about the generalizability and the transportability of the risk prediction model in a new setting^{40,41}. An increasing number of performance measures have been proposed in the last two decades for survival models. Many extend to the case of competing risks. However, clear guidance is lacking for a comprehensive assessment of the performance for survival and competing risks models⁴²⁻⁴⁴. Moreover, a model may show good performance in terms of discrimination and calibration, while both measures are unable to provide an answer to the question whether a risk prediction model should be used in practice to guide clinical decision making⁴⁵.

Net benefit is a relative novel measure to evaluate the clinical utility of risk prediction models and diagnostic tests weighting benefit and harms of a clinical decision making in public health^{46,47}. Early detection and disease prevention are two of the most important goals in medicine. Physicians generally accept to recommend to persons or patients a certain number of unnecessary preventive strategies or treatments for the benefit to early detect or prevent a disease. This implies that the cost of missing the early detection or prevention of a certain disease (defined as false negatives) is typically more important than the cost of unnecessary preventive strategies or treatments recommendation (defined as false positives). The nationwide mammography screening program is a clear

example: public health physicians accept to recommend a high number of unnecessary screenings in a large population of healthy women to early detect a breast cancer with the aim to anticipate treatment and improve prognosis. This is also feasible because mammography screenings are considered as an acceptable safe procedure with a low number of side effects. In disease prevention, treatments or preventive strategies like surgeries may be more harmful than the mammography screening. For example, as previously mentioned, a certain number of complications after a contralateral preventive mastectomy may be possible.

Imagine having to decide about contralateral preventive mastectomy in 1000 patients diagnosed with first breast cancer. As previously reported, about 50 out of 1000 patients will develop a cancer in the contralateral breast in 10 years (i.e., as previously reported an expected 5% 10-year cumulative incidence). Suppose physicians recommend contralateral preventive mastectomy to all breast cancer patients irrespective of their age, potential germline mutations, family history and the other first breast cancer characteristics. We define this strategy as “intervention to all”. This means we prevent 50 contralateral breast cancers (i.e., 5% benefit) at the cost of 950 unnecessary surgeries (i.e., 95% harm). Now, suppose that another strategy (named “alternative strategy”, e.g., using a risk prediction model) is available and it reduces the number of unnecessary surgeries to 450, but preventing only 40 contralateral breast cancers. Is reducing 500 unnecessary surgeries at the cost of not preventing 10 contralateral breast cancers a good trade-off? To answer this question, it is important that physicians define how many patients should unnecessary undergo the contralateral preventive mastectomy to prevent one contralateral breast cancer. For example, a physician thinks that no more than 25 patients should undergo the surgery to prevent one contralateral breast cancer: this implies that not preventing a contralateral breast cancer is twenty-four times more harmful than undergoing an unnecessary preventive surgery. This 1:25 ratio would imply a decision threshold of 4%, and a relative weight of unnecessary surgery as 1/24 that of missing one contralateral breast cancer. The result of the net benefit calculation is reported in Table 1.

The net benefit is 1% and 2% for the strategy “interventions to all” and “alternative strategy”, respectively. In other words, assuming the same number of unnecessary interventions, the “alternative strategy” prevents 20 contralateral breast cancers per 1000 patients at risk. The “intervention to all” strategy leads to prevent less contralateral breast cancers (i.e., 10) than the “alternative strategy”. Thus, the net benefit of the “alternative strategy” is higher than the “intervention to all” strategy using 1/24 as weight of benefit and harms. However, physicians may have different opinions about how many patients should undergo unnecessary surgeries to prevent one disease. For this reason, net benefit calculation may be possible to define which strategy has higher net benefit using different exchange rates⁴⁶⁻⁴⁸.

Table 1: an example of net benefit calculation

How many unnecessary mastectomies a physician is willing to accept to prevent a contralateral breast cancer?	Number of patients with first breast cancer: 1000 Expected number of contralateral breast cancers in 10 years: 50				
	Exchange rate	Strategies	Benefit	Harm	Net Benefit = benefit - (harm × exchange rate)
25	1/24	Interventions to all	5% (50/1000)	95% (950/1000)	5% - (95% × 1/24) = 1%
		Alternative strategy	4% (40/1000)	45% (450/1000)	4% - (45% × 1/24) = 2%

The goal of this thesis is to develop, validate and evaluate the potential clinical utility of a contralateral breast cancer prediction model to provide contralateral breast cancer prediction at 5 and 10 years since diagnosis of first primary breast cancer. Frameworks of assessing prediction performance in time-to-event models with or without competing risks are proposed using motivating examples in breast cancer.

THESIS OUTLINE

We set out to develop a risk prediction model for contralateral breast cancer, named PredictCBC, using international population-based and hospital-based studies (Table 2, Chapter 2).

Table 2: Data sources used in the thesis

Source	Country	Description	Chapter
Amsterdam Breast Cancer Study (ABCS)	the Netherlands	Hospital-based study	2-3-4
Breast Cancer Association Consortium (BCAC)	International	Population and hospital-based studies	2-3-4
Breast Cancer Outcome Study of Mutation (BOSOM)	the Netherlands	Hospital-based study	2-3-4
Erasmus Medical Center (EMC)	the Netherlands	Hospital-based study	2-3-4
Hereditary Breast and Ovarian cancer study (HEBON)	the Netherlands	Population-based study*	4
the Netherlands Cancer Registry (NCR)	the Netherlands	Population-based study	2-3-4-5-7

*selection through clinical genetic centers

Using the same data (Table 2), we evaluated and compared the prediction performance of PredictCBC with other tools available to calculate the contralateral breast cancer risk in clinical practice: CBCrisk and the Manchester formula (Chapter 3). We updated PredictCBC models using more clinical and genetic information available including body mass index, parity, *CHEK2* c.1100del, and polygenic risk score to potentially improve the contralateral breast cancer risk prediction performance for decision making (Chapter 4). We estimated the contralateral breast cancer risk in patients with ductal carcinoma in situ, a possible precursor of breast cancer since less is known about contralateral breast cancer risk in comparison with invasive breast cancer patients (Chapter 5). Finally, we provide frameworks of how to assess prediction performance in time-to-event models with and without competing risks using motivating examples in breast cancer as a guidance for researchers and practitioners interested in risk prediction (Chapter 6 and Chapter 7).

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