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Geometry of vegetation patterns: understanding patterns in dryland ecosystems and beyond

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Geometry of Vegetation Patterns

*Understanding patterns in dryland ecosystems and
beyond*

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*To Dikkie and Patat.
To those who still don't have access to education.*

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