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## Progressive Indexes

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### 1 Introduction

Data scientists perform exploratory data analysis to discover unexpected patterns in large collections of data. This process is done with a hypothesis-driven trial-and-error approach [52]. They query data segments that could potentially provide insights, test their hypothesis, and either zoom in on the same segment or move to a different one depending on the insights gained.

Fast responses to queries are crucial to allow for interactive data exploration. The study by Liu et al. [41] shows that any delay larger than 500ms (the “interactivity threshold”) significantly reduces the rate at which users make observations and generate hypotheses. When dealing with small data sets, providing answers within this interactivity threshold is possible without utilizing indexes. However, exploratory data analysis is often performed on larger data sets as well. In these scenarios, indexes are required to speed up query response times.

Index creation is one of the major difficult decisions in database schema design [15]. Based on the expected workload, the database administrator (DBA) needs to decide whether creating a specific index is worth the overhead in creating and maintaining it. Creating indexes up-front is especially challenging in exploratory and interactive data analysis, where queries are not known in advance, workload patterns change frequently, and interactive responses are required. In these scenarios, data scientists load their data and immediately want to start querying it without waiting for index

construction. In addition, it is also not certain whether or not creating an index is worth the investment at all. We cannot be sure that the column will be queried frequently enough for the large initial investment of creating a full index to pay off.

In spite of these challenges, indexing remains crucial for improving database performance. When no indexes are present, even simple point and range selections require expensive full table scans. When these operations are performed on large data sets, indexes are essential to ensure interactive query response times. Two main strategies aim to release the DBA of having to choose which indexes to create manually.

(1) Automated index selection techniques [1, 14, 58, 23, 13, 11, 44, 53] accomplish this by attempting to find the optimal set of indexes given a query workload, taking into account the benefits of having an index versus the added costs of creating the entire index and maintaining it during modifications to the database. However, these techniques require a priori knowledge of the expected workloads and do not work well when the workload is not known or changes frequently. Hence they are not suitable for interactive data exploration.

(2) Adaptive Indexing techniques such as Database Cracking [36, 21, 50, 49, 26, 35, 37, 47, 46, 25, 34, 29] are a more promising solution. They focus on automatically and incrementally building an index as a side effect of querying the data. An index for a column is only initiated when it is first queried. As the column is queried more, the index is refined until it eventually approaches a full index’s performance. In this way, the cost of creating an index is smeared out over the cost of querying the data many times, though not necessarily equally, and there is a smaller initial overhead for starting the index creation. However, since the index is refined only in the areas targeted by the workload, convergence to a full index is not guaranteed, and partitions can have different sizes. The query’s performance degrades when a less refined part of the index is queried, resulting in performance spikes whenever the workload changes.

In this chapter, we introduce a new incremental indexing technique called *Progressive Indexing*. It differs from other indexing solutions in that the indexing budget (i.e., the amount of time spent on index creation and refinement) can be controlled. We provide two indexing budget flavors: a fixed indexing budget, where the user defines a fixed amount of time to spend on indexing per query, and an adaptive indexing budget, where the indexing budget is adapted so that the total time spent on query execution remains constant. We refer to the fixed indexing budget as Progressive Indexing and the adaptive indexing budget as Greedy Progressive Indexing. As a result, both Progressive Indexing and Greedy Progressive Indexing complements existing automatic indexing techniques by offering predictable performance and deterministic convergence

independent of the workload.

## 1.1 Contributions

The main contributions of this chapter are:

- We introduce several novel Progressive Indexing techniques and investigate their performance, convergence, and robustness in the face of various realistic synthetic workload patterns and real-life workloads.
- We provide a cost model for each of the Progressive Indexing techniques. The cost models are used to adapt the indexing budget automatically.
- We experimentally verify that the Progressive Indexing techniques we propose provide robust and predictable performance and convergence regardless of the workload or data distribution.
- We provide a decision tree to assist in choosing an indexing technique for a given scenario.
- We provide Open-Source implementations of each of the techniques we describe and their benchmarks.<sup>1</sup>

## 1.2 Outline

This chapter is organized as follows. Section 2 depicts related research performed on automatic/adaptive index creation. In Section 3, we describe our novel Progressive Indexing techniques and discuss their benefits and drawbacks. Section 4 describes the cost-models used to adapt our indexing budget automatically. In Section 5, we perform an experimental evaluation of each of the novel methods we introduce, and we compare them against Adaptive Indexing techniques. Finally, in Section 6 we draw our conclusions and present a decision tree to assist in choosing which Progressive Indexing technique to use.

## 2 Related Work

In this section, we discuss the state-of-the-art of Adaptive Indexing in terms of performance and robustness. Section 2.1 we discuss possible cracking kernels to get

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<sup>1</sup>Our implementations and benchmarks are available at <https://github.com/pdet/ProgressiveIndexing>

the partitioning as fast as possible. In Section 2.2 we discuss three different Adaptive Indexing algorithms that attempt to improve cracking’s robustness problem.

## 2.1 Cracking Kernels

A cracking kernel [47, 25] is the central part of how the partitioning of a piece is done. This section focuses on two partitioning kernels. First, we present the branching kernel, which uses if-else clauses to decide when to swap elements. Second, we describe the predicated kernel that uses predication to avoid branch mispredictions.

### Branching Kernel

The branching kernel is the one used in the Standard Cracking implementation and has a clear inspiration from quicksort’s partitioning [27]. Listing 1 depicts the kernel for the integer data type. It receives as input the array, the pivot, and the boundaries of the partition  $posL$  and  $posR$ . The algorithm, inspects all vector elements, and increase  $posL$  in case the element  $data[posL]$  is less than the pivot and increases  $posR$  in case the element  $data[posR]$  is greater than or equal to the pivot. In other words, it simply moves the cursors if the elements are already in the correct position in reference to the pivot. If it finds both  $data[posL]$  and  $data[posR]$  that are not in the correct position, it swaps them and move the cursors. The main problem with this kernel is that swapping the data in the if-else clauses causes an increase in branch mispredictions and an overall decrease in performance, as demonstrated in Boncz et al. [10].

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**Listing 1** Branching Kernel

---

```

1 void branching_kernel(int& data, int pivot, size_t posL, size_t posR){
2     while (posL < posR){
3         if (data[posL] < pivot){
4             posL++;
5         }
6         else if (data[posR] >= pivot){
7             posR--;
8         }
9         else{
10            swap(data[posL++], data[posR--])
11        }
12    }
13 }
```

---

## Predicated Kernel

The predicated kernel removes the if-else clauses to avoid branch misprediction costs. Listing 2 demonstrates the predicated kernel for integers. Like the branching kernel, we iterate over the vector. In lines 3 and 4, we store the values we will inspect in this iteration. Lines 5,6, and 7 store integers that inform if a given element must be swapped. For example, if  $data[posL]$  is lower than  $pivot$ , that means that  $data[posL]$  is already in its correct position, hence the  $start\_has\_to\_swap$  variable will hold 0. Lines 8 - 11 effectively swap the data and modify the cursors with respect on the information in the  $start\_has\_to\_swap$ ,  $end\_has\_to\_swap$ , and  $has\_to\_swap$  variables. The predicated kernel has an extremely predictable cost since it will always execute the same code, independent of branches.

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**Listing 2** Predicated Kernel

---

```

1 void predicated_kernel(int& data, int pivot, size_t posL, size_t posR){
2     while (posL < posR){
3         int l_value = data[posL];
4         int r_value = data[posR];
5         int start_has_to_swap = l_value >= pivot;
6         int end_has_to_swap = r_value < pivot;
7         int has_to_swap = start_has_to_swap * end_has_to_swap;
8         data[posR] = !has_to_swap * l_value + has_to_swap * r_value;
9         data[posL] = !has_to_swap * r_value + has_to_swap * l_value;
10        posL+= !start_has_to_swap + has_to_swap;
11        posR -= !end_has_to_swap + has_to_swap;
12    }
13 }
```

---

## 2.2 Adaptive Indexing for Robustness

### Stochastic Cracking [26]

Stochastic Cracking minimizes the unforeseen performance issues from cracking. Instead of using query predicates as pivots, a random element from the to-be-cracked piece is used as the partitioning pivot. Hence this decreases the workload dependency from cracking.

Figure 3-1 depicts an example of Stochastic Cracking. From our example, the cracker column is initially unpartitioned. When executing the first query that requests all elements greater than 15, a random element from the column is selected as a pivot.

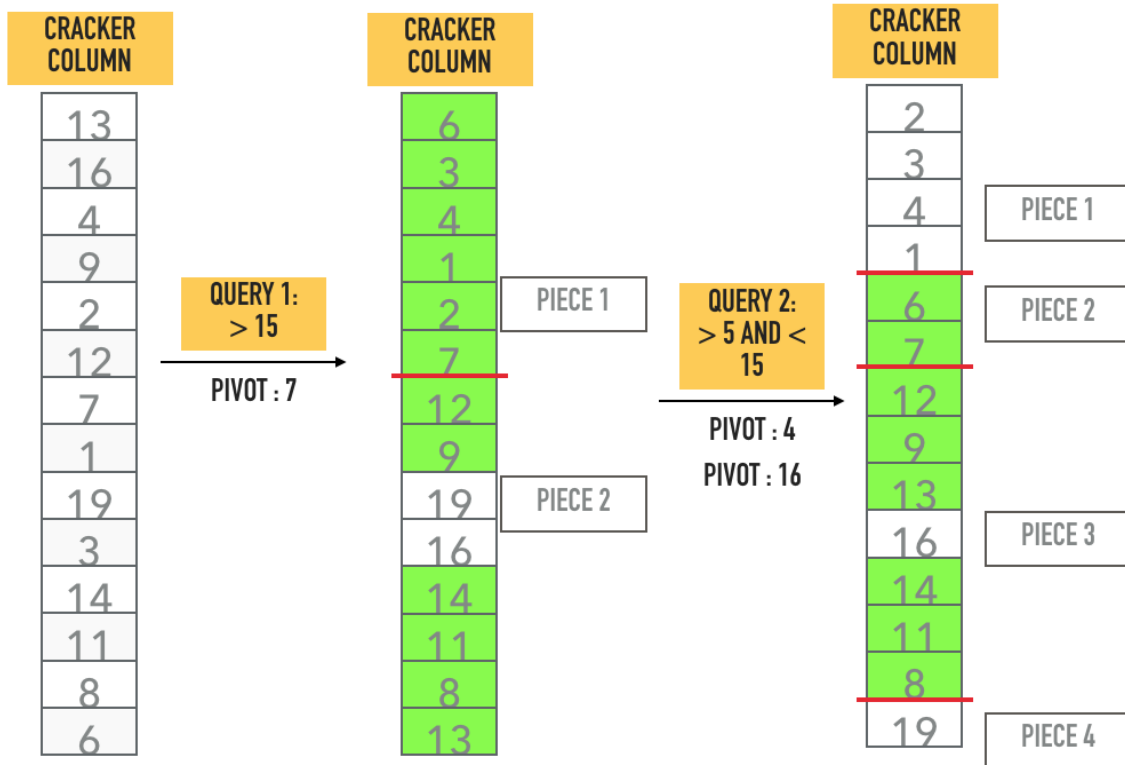


Figure 3-1: Standard Cracking executing two queries.

In our example, the element 7, the column is then partitioned around 7, and both pieces must be scanned to answer the query. When query 2 is executed requesting all elements between 5 and 15, *Piece 1* is pivoted with an element within the piece, in this case, 4, and the same happens with *Piece 2*, with pivot 16 being selected to partition it. After finishing the partition, only piece 2 (i.e., all elements over 4) and piece 3 (i.e., all elements higher than 7 and lower or equal to 16) must be scanned.

Not using the filter predicates as query pivots can result in the execution engine reading more data than necessary even after the partitioning for that query. However, sudden changes in the workload pattern will not have the same impact as in Standard Cracking.

### Progressive Stochastic Cracking [26]

Progressive Stochastic Cracking progressively performs Stochastic Cracking. It takes two input parameters, the size of the L2 cache and the number of swaps allowed in one iteration (i.e., a percentage of the total column size). When performing Stochastic Cracking, Progressive Stochastic Cracking will only perform at most the maximum allowed number of swaps on pieces larger than the L2 cache. If the piece fits into the

L2 cache, it will always perform a complete crack of the piece.

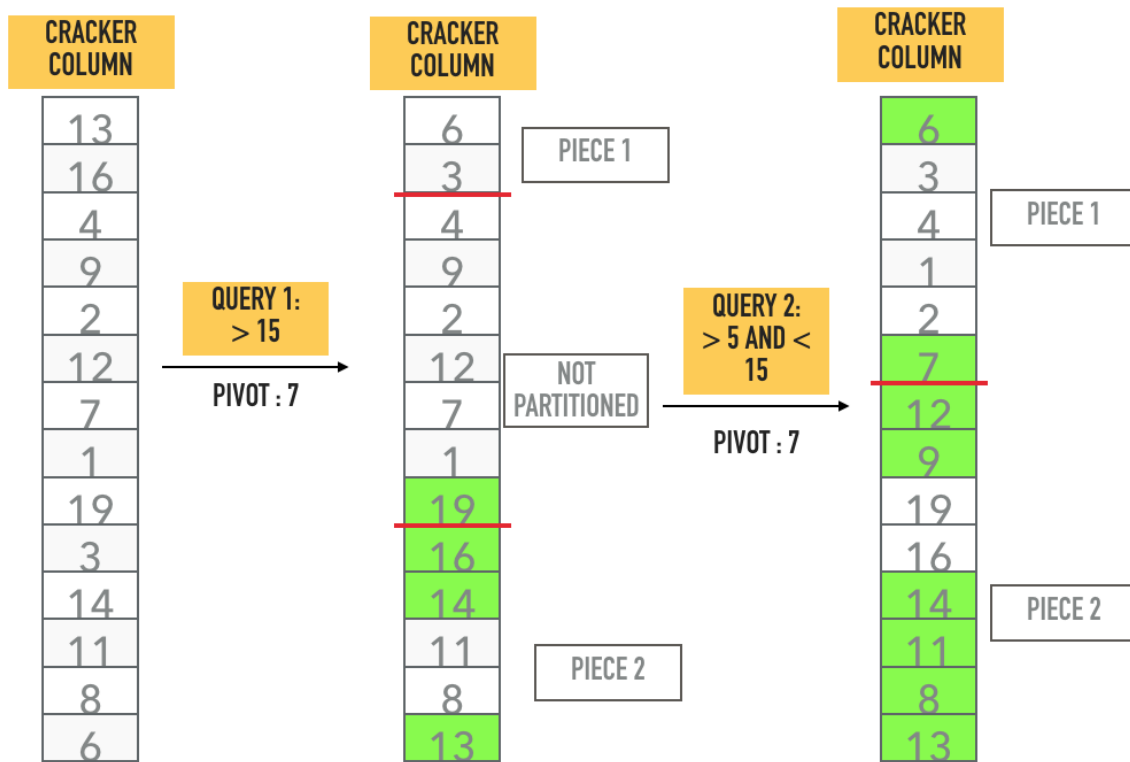


Figure 3-2: Progressive Stochastic Cracking with maximum swaps = 2 and L2 Cache Size = 8kb.

Figure 3-2 depicts an example of Progressive Stochastic Cracking, where the L2 Cache Size fits two integers and the at most two swaps can be performed per query. Like Stochastic Cracking, the pivots are also selected randomly from within the piece that will be partitioned. In our first query, the pivot chosen is 7. The difference is that when executing this query, we stop pivoting after swapping two elements. When executing *Query 2*, we finish the partition with pivot 7 before picking new pivots.

### Coarse-Granular Index [50]

The Coarse-Granular Index improves Stochastic Cracking’s robustness by creating  $k$  partitions when the first query is executed using equal-width binning. It also allows for creating any number of partitions instead of limiting the number of partitions to two, letting the DBA decide on  $k$ , choosing between the trade-off of the higher cost of the first query versus building a more robust index.

Figure 3-3 depicts an example of the Coarse-Granular Index set to create four partitions. When executing the first query, the algorithm will perform 3 cracking



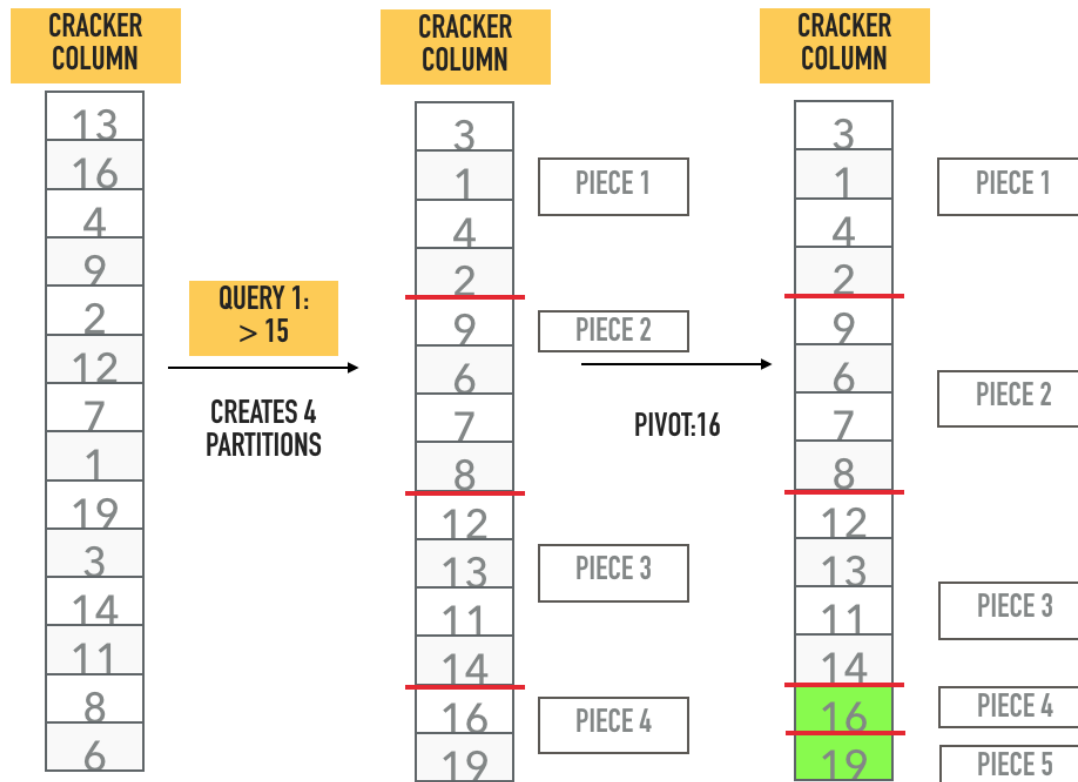


Figure 3-3: Coarse Granular-Index creating  $k = 4$  partitions in the first query.

iterations from the equi-width binning (i.e., since our data goes from 1 to 20, that means the pivots will be 5,10, and 15). After it, a standard Stochastic Cracking iteration happens. At that point, it is only necessary to check *Piece 4* since it holds all elements over 15. A random pivot from within the piece is selected, in this case, 16, and the query answer is produced.

### Adaptive Adaptive Indexing [49]

Adaptive Adaptive Indexing is a general-purpose algorithm for Adaptive Indexing. It has multiple parameters tuned to mimic the data access of different Adaptive Indexing techniques (e.g., Database Cracking, Sideways Cracking, Hybrid Cracking). It also uses radix partitioning and exploits software-managed buffers using nontemporal streaming stores to achieve better performance [51].

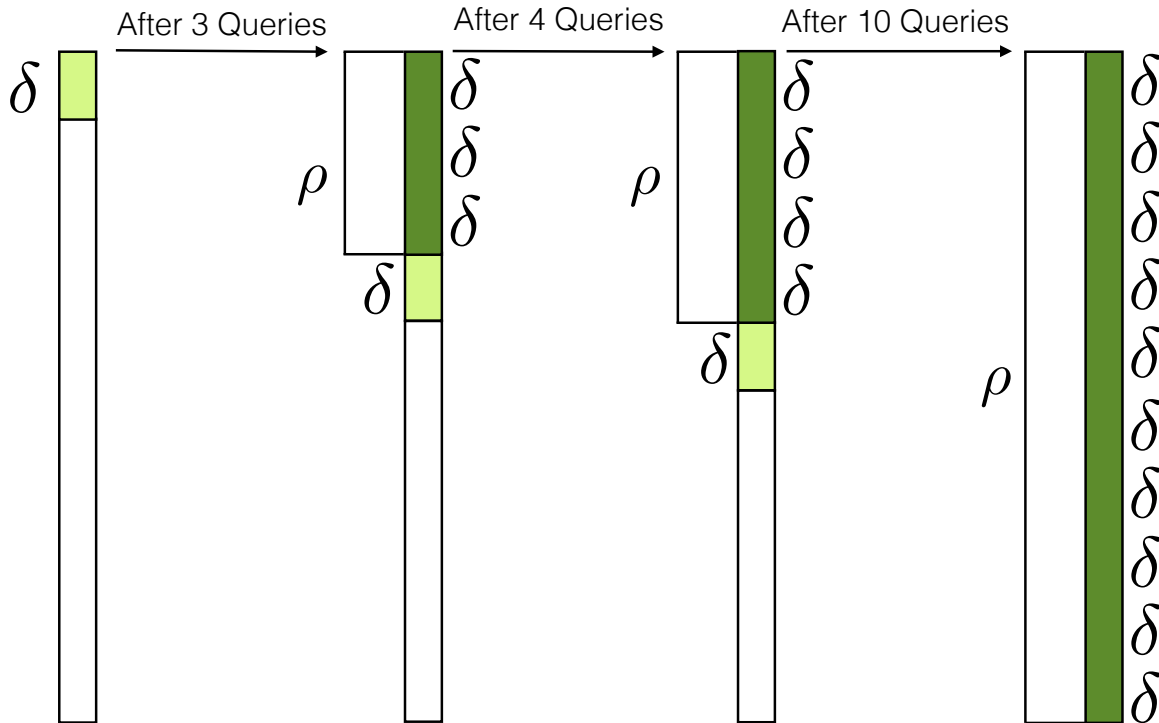


Figure 3-4: Creation phase of Progressive Indexing.

### 3 Progressive Indexing

In this section, we introduce *Progressive Indexing*. The core features of Progressive Indexing are that (1) the indexing overhead per query is controllable, both in terms of time and memory requirements, (2) it offers robust performance and deterministic convergence regardless of the underlying data distribution, workload patterns, or query selectivity, and (3) the indexing budget can be automatically tuned so more expensive queries spend less extra time on indexing while cheaper queries spend more. To allow for robust query execution times regardless of the data, we avoid branches in the code and use predication when possible [48, 10].

As a result of the small initial cost, Progressive Indexing occurs without significantly impacting worst-case query performance. Even if the column is only queried once, only a small penalty is incurred. On the other hand, if the column is queried hundreds of times, the index will reliably converge towards a full index, and queries will be answered at the same speed as with an a-priori built full index.

All Progressive Indexing algorithms progress through three canonical phases to eventually converge to a full B+-tree index: the *creation phase*, the *refinement phase*, and the *consolidation phase*. Each phase's work can be divided between multiple queries, keeping the extra indexing effort per query strictly limited.

**Creation Phase.** The creation phase progressively builds an initial “crude” version of the index by adding another  $\delta$  fraction of the original column to the index with each query. Query execution during the creation phase is performed in three steps (visualized in Figure 3-4):

1. Perform an index lookup on the  $\rho$  fraction of the data that has already been indexed;
2. Scan the not-yet-indexed  $1 - \rho$  fraction of the original column;  
*and while doing so,*
3. Expand the index by another  $\delta$  fraction of the total column.

As the index grows and the fraction  $\rho$  of the indexed data increases, an ever-smaller fraction of the base column has to be scanned, progressively improving query performance. Once all the base column data has been added to the index, the creation phase is followed by the refinement phase.

**Refinement Phase.** With the base column no longer required to answer queries, we only perform lookups into the index to answer queries. While doing these lookups, we further refine the index, progressively converging towards a fully ordered index. In the refinement phase, we focus on refining parts of the index required for query processing. After these parts have been refined, the refinement process starts processing the neighboring parts. Once the index is fully ordered, the refinement phase is followed by the consolidation phase.

**Consolidation Phase.** With the index fully ordered, we progressively construct a B+-tree from it since a B+-Tree provides better data locality and thus is more efficient than binary search when executing very selective queries. Once the B+-tree is completed, we use it exclusively to answer all subsequent queries. The consolidation phase is the same for all progressive algorithms. All algorithms end their refinement phase with a sorted array. The B+-tree is then constructed on top of that sorted array in a bottom-up fashion. Figure 3-5 depicts an example of the construction phase for Progressive Quicksort in the right-most part of the figure labeled *Consolidation*. In this example, the B+-Tree stored 4 elements per node. Hence we start constructing the last level of the inner nodes pointing to one element every four elements. In this case, the B+-Tree nicely ends with one inner node that is also the root. However, if there were more elements, we would fully construct this level, link all nodes, and proceed to the upper level and repeat this strategy.

In the following section, we discuss the details of four different Progressive Indexing implementations. Section 3.1 describes Progressive Quicksort as a progressive version of quicksort, aiming to achieve good performance independent of query patterns and data distributions. In Section 3.2 we present Progressive Radixsort - Most Significant Digit as the radixsort algorithm this index is based on, we expect good performance over uniform distributions. In Section 3.3 we present Progressive Bucketsort, inspired by bucketsort equi-height, which is expected to present excellent performance with highly skewed data distributions. Finally, in Section 3.4 we present Progressive Radixsort - Least Significant Digit, where we aim to optimize for workloads that contain only point queries.

### 3.1 Progressive Quicksort

Figure 3-5 depicts snapshots of the creation phase, the refinement phase, and the consolidation phase of Progressive Quicksort. We discuss the creation and refinement phases in detail in the following paragraphs.

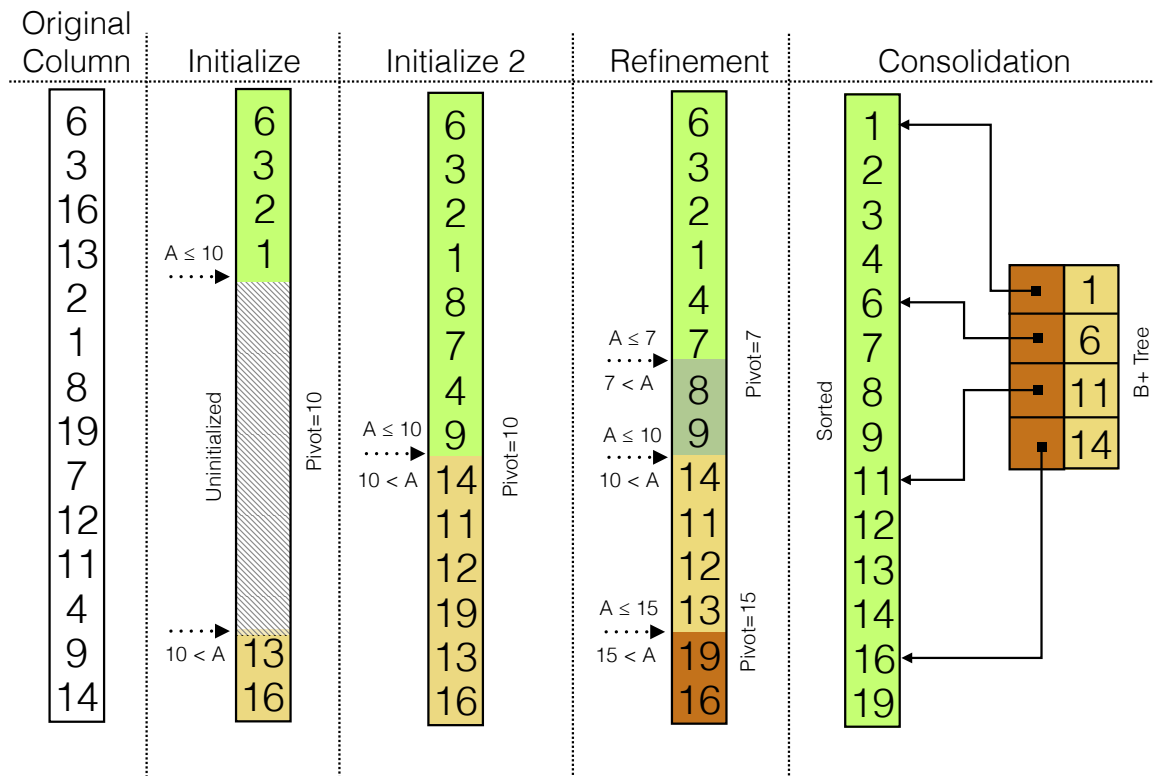


Figure 3-5: Progressive Quicksort.

### **Creation Phase**

In the first iteration, we allocate an uninitialized column of the same size as the original column and select a pivot. The pivot is selected by taking the average value of the smallest and largest value of the column. In Figure 3-5, pivot 10 is the average of 1 and 19. If sufficient statistics are available, the median value of the column could be used instead. Unlike Adaptive Indexing, the pivot selection is not impacted by the query predicates. We then scan the original column and copy the first  $N * \delta$  elements to either the top or bottom of the index, depending on their relation to the pivot. In this step, we also search for any elements that fulfill the query predicate and afterward scan the not-yet-indexed  $1 - \rho$  fraction of the column to compute the complete answer to the query. In subsequent iterations, we scan either the top, bottom, or both parts of the index based on how the query predicate relates to the chosen pivot.

### **Refinement Phase**

We refine the index by recursively continuing the quicksort in-place in the separate sections. The refinement consists of swapping elements in-place inside the index around the pivots of the different segments. When the pivoting of a segment is completed, we recursively continue the quicksort in the child segments. We maintain a binary tree of the pivot points. In this tree's nodes, we keep track of the pivot points and how far along the pivoting process we are. To do an index lookup, we use this binary tree to find the array sections that could match the query predicate and only scan those, effectively reducing the amount of data to be accessed even when the full pivoting has not been completed yet.

When we reach a node that is smaller than the L1 cache, we sort the entire node instead of recursing any further. After sorting a node entirely, we mark it as sorted. When two children of a node are sorted, the entire node itself is sorted, and we can prune the child nodes. As the algorithm progresses, leaf nodes will keep on being sorted and pruned until only a single fully sorted array remains.

## **3.2 Progressive Radixsort (MSD)**

Figure 3-6 depicts snapshots of the creation phase, the refinement phase, of Progressive Radixsort (MSD). We discuss both phases in detail in the following paragraphs.

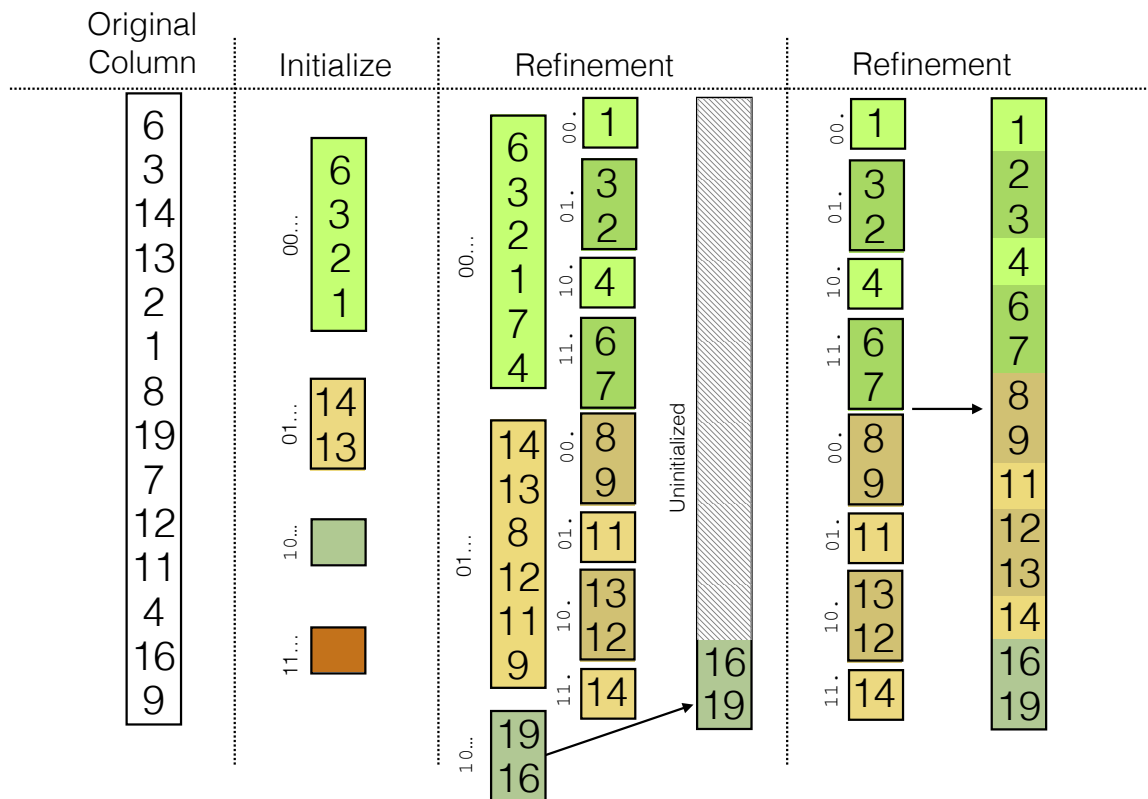


Figure 3-6: Progressive Radixsort (MSD).

### Creation Phase

In the creation phase of Progressive Radixsort, we perform the radixsort partitioning into buckets located in separate memory regions. We start by allocating  $b$  empty buckets. Then, while scanning the original column, we place  $N * \delta$  elements into the buckets based on their most significant  $\log_2 b$  bits. We then scan the remaining  $1 - \rho$  fraction of the base column. In subsequent iterations, we scan the  $[0, b]$  buckets that could potentially contain elements matching the query predicate to answer the query in addition to scanning the remainder of the base column.

**Bucket Count.** Radix clustering performs a random memory access pattern that randomly writes in  $b$  output buckets. To avoid excessive cache- and TLB-misses, assuming that each bucket is at least of the size of a memory page, the number  $b$  of buckets, and thus the number of randomly accessed memory pages, should not exceed the number of cache lines and TLB entries, whichever is smaller [9]. Since our machine has 512 L1 cache lines and 64 TLB entries, we use  $b = 64$  buckets.

**Bucket Layout.** To avoid allocating large regions of sequential data for every bucket, the buckets are implemented as a linked list of blocks of memory that each

hold up to  $s_b$  elements. When a block is filled, another block is added to the list, and elements will be written to that block. This adds some overhead over sequential reads/writes as for every  $s_b$  elements there will be a memory allocation and random access, and for every element that is added, the bounds of the current block have to be checked.

### **Refinement Phase**

In the refinement phase, all elements in the original column have been appended to the buckets. In this phase, we recursively partition by the next set of  $\log_2 b$  most significant digits. For each of the buckets, this results in creating another set of  $b$  buckets in each of the refinement phases, for a total of  $b*b$  buckets in the second phase. To avoid the overhead of managing these buckets to become bigger than the overhead of actually performing the radix partitioning, we avoid re-partitioning buckets that fit into the L1 cache and instead immediately insert the values of these buckets in sorted order into the final sorted array, as shown in Figure 3-6. As the buckets themselves are ordered (i.e., for two buckets  $b_i$  and  $b_{i+1}$ , we know  $e_i < e_{i+1} \forall e_i \in b_i, e_{i+1} \in b_{i+1}$ ), we know the position of each bucket in the final sorted array without having to consider any elements in the other buckets.

We keep track of the buckets using a tree in which the nodes point towards either the leaf buckets or towards a position in the final sorted array if the leaf buckets have already been merged in there. This tree is used to answer queries on the intermediate structure. When we get a query, we look up which buckets we have to scan based on the query predicates' most significant bits. We then scan the buckets or the final index, where required.

When the first iteration of the refinement phase is completed, we recursively continue with the next set of  $\log_2 b$  most significant digits until all the elements have been merged and sorted into the final index. At that point, we construct our B+-tree index from the single fully sorted array.

## **3.3 Progressive Bucktersort**

Progressive Bucktersort (Equi-Height) is very similar to Progressive Radixsort (MSD). The main difference is in the way the initial partitions (buckets) are determined. Instead of radix clustering, which is fast but yields equally sized partitions only with uniform data distributions, we perform a value-based range partitioning to yield equally sized partitions also with skewed data, at the expense that determining the

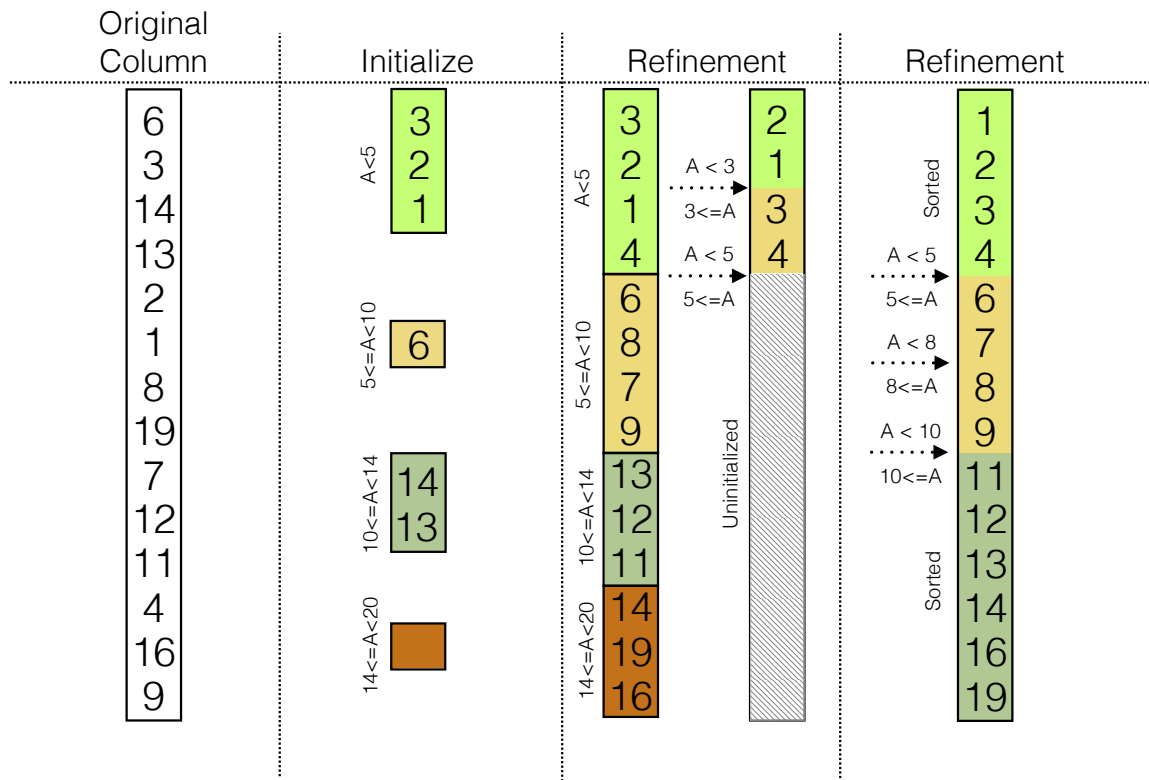


Figure 3-7: Progressive Bucket Sort

bucket that a value belongs to is more expensive. Figure 3-7 depicts a snapshot of the creation phase and two snapshots of the refinement phase. In the following, we discuss these two phases in detail.

**Bucket Count.** To optimize for writing and reading from the buckets, our implementation of Progressive Bucketsort uses 64 buckets, as discussed in Section 3.2.

### Creation Phase

Progressive Bucketsort operates in a very similar way to Progressive Radixsort (MSD). Instead of choosing the bucket an element belongs to based only on the most significant bits, the bucket is chosen based on a set of bounds that more-or-less evenly divide the set elements into the separate buckets. These bounds can be obtained either in the scan to answer the first query or from existing statistics in the database (e.g., a histogram).



### Refinement Phase

In the refinement phase, all elements in the original column have been appended to the buckets. We then merge the buckets into a single sorted array. Unlike with Progressive Radixsort (MSD), we do not recursively keep on using Progressive Bucketsort. This is because the overhead of finding and maintaining the equi-height bounds for each sub-bucket is too large. Instead, we sort the individual buckets into the final sorted list using Progressive Quicksort. Using a progressive algorithm to sort individual buckets protects us from performance spikes caused by sorting large buckets.

The buckets are merged into the final sorted index in order. As such, we always have a single iteration of Progressive Quicksort active at a time in which we are performing swaps. After all the buckets have been merged and sorted into the final index, we have a single fully sorted array from which we can construct our B+-tree index.

### 3.4 Progressive Radixsort (LSD)

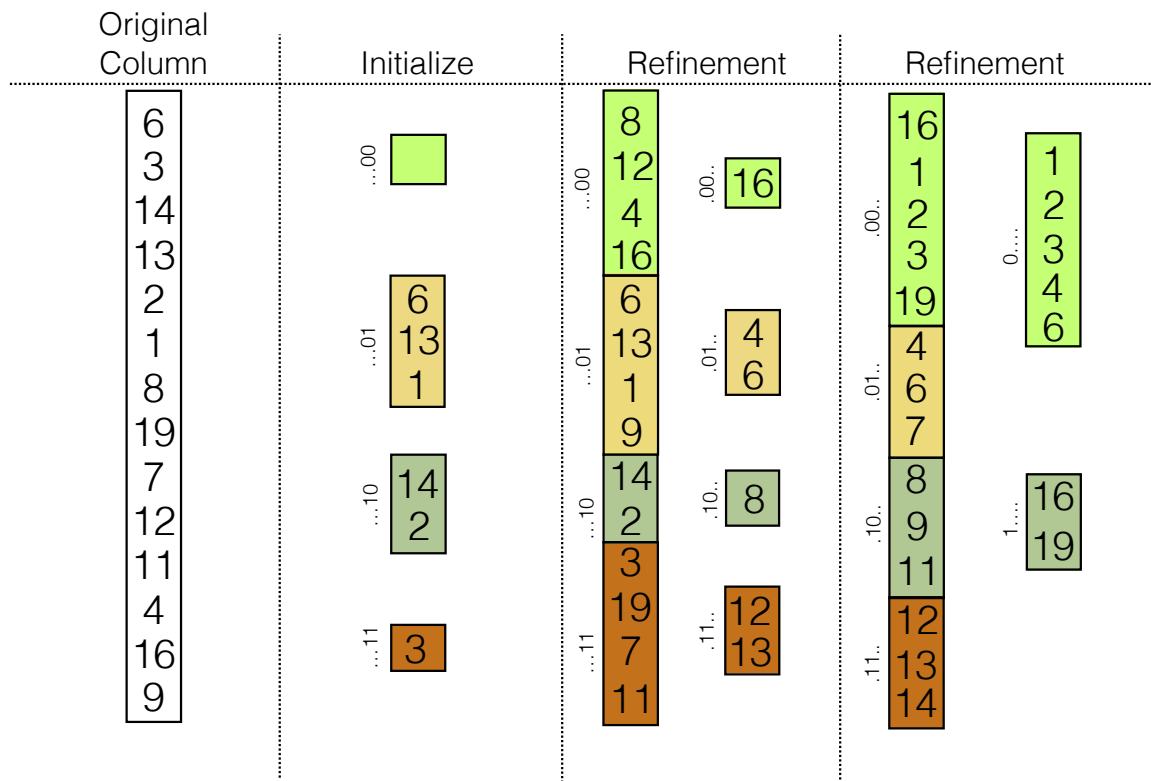


Figure 3-8: Progressive Radixsort (LSD).

Progressive Radixsort Least Significant Digits (LSD) performs a progressive radix clustering on the least significant bits during the creation and refinement phase. Figure 3-8 depicts a snapshot of the creation phase and two snapshots of the refinement phase. In the following, we discuss these two phases in detail.

**Bucket Count.** To optimize for writing and reading from the buckets, our implementation of Progressive Radixsort (LSD) uses 64 buckets, as discussed in Section 3.2.

### Creation Phase

This algorithm’s creation phase is similar to the creation phase of Progressive Radixsort (MSD), except that we partition elements based on the least-significant bits instead of the most-significant bits. We can use the buckets created to speed up point queries because we only need to scan the bucket in which the query value falls. However, unlike the buckets created for the Progressive Radixsort (MSD) and Progressive Bucketsort, these intermediate buckets cannot be used to speed up range queries in many situations. Because the elements are inserted based on their least-significant bits, the buckets do not form a value-based range-partitioning of the data. Consequently, we will have to scan many buckets, depending on the domain covered by the range query.

### Refinement Phase

In the refinement phase, we move elements from the current set of buckets to a new set of buckets based on the next set of significant bits. We repeat this process until the column is sorted. How many iterations this takes depends on the bucket count and the column’s value domain, which we obtain from the  $[min, max]$  values. We can compute the amount of required iterations with the formula  $\lceil \log_2(max - min) / \log_2(b) \rceil$ . For example, for a column with values in the range of  $[0, 2^{16})$  and 64 buckets, the amount of iterations required before convergence is  $\lceil \log_2(2^{16}) / \log_2(64) \rceil = 3$ .

## 4 Greedy Progressive Indexing

The value of  $\delta$  determines how much time is spent constructing the index and hence determines the indexing budget. Greedy Progressive Indexing allows the user to select between setting either a fixed indexing budget or an adaptive indexing budget. For the fixed indexing budget, the user provides the desired indexing budget  $t_{budget}$  to

Table 3.1: Parameters for Greedy Progressive Quicksort Cost Model.

System	$\omega$	cost of sequential page read (s)
	$\kappa$	cost of sequential page write (s)
	$\phi$	cost of random page access (s)
	$\gamma$	elements per page
Data set & Query	$N$	number of elements in the data set
	$\alpha$	% of data scanned in partial index
Index	$\delta$	% of data to-be-indexed
	$\rho$	% of data already indexed
Progressive Quicksort	$h$	height of the binary search tree
Progressive Radixsort	$b$	number of buckets
	$s_b$	max elements per bucket block
	$\tau$	cost of memory allocation (s)
B+-Tree	$\beta$	tree fanout

spend on indexing for the first query. We then select the value of  $\delta$  based on this budget and use that  $\delta$  for the remainder of the workload. The adaptive indexing budget allows the user to specify the desired indexing budget for the first query  $t_{budget}$ . The first query will then execute in time  $t_{adaptive} = t_{scan} + t_{budget}$ . After the first query, the value of  $\delta$  will be adapted such that the query cost will stay equivalent to  $t_{adaptive}$  until the index is converged.

**Cost Model.** We use a cost model to determine how much time we can spend on indexing when working with the adaptive indexing budget. The cost model takes into account the query predicates, the selectivity of the query and the state of the index in a way that is not sensitive to different data distributions or querying patterns and does not rely on having any statistics about the data available.

## 4.1 Greedy Progressive Quicksort

The parameters of the Greedy Progressive Quicksort cost model are summarized in Table 3.1.

### Creation Phase

The total time taken in the creation phase is the sum of (1) the scan time of the base table, (2) the index lookup time, and (3) the additional indexing time. The scan time is given by multiplying the number of pages we need to scan ( $\frac{N}{\gamma}$ ) by the amount of time it takes for a sequential page access ( $\omega$ ), resulting in  $t_{scan} = \omega * \frac{N}{\gamma}$ . The pivoting time (i.e., index construction time) consists of scanning the base table pages and writing the pivoted elements to the result array. The pivoting time is therefore

obtained by multiplying the time it takes to scan and write a page sequentially ( $\kappa + \omega$ ) by the number of pages we need to write, resulting in  $t_{pivot} = (\kappa + \omega) * \frac{N}{\gamma}$ .

The total time taken for the initial indexing process is given by multiplying the scan time by the fraction of the base table we need to scan. Initially, we need to scan the entire base table, but as the fraction of indexed data ( $\rho$ ) increases, we need to scan less. Instead, we scan the index to answer the query. The amount of data we need to scan in the index depends on how the query predicates relate to the pivot. The fraction of data that we need to scan is given by  $\alpha$  and can be computed for a given set of query predicates. The total fraction of the data that we scan is  $1 - \rho + \alpha - \delta$ . The fraction of the data that we index in each step is  $\delta$ . Hence the total time taken is given by  $t_{total} = (1 - \rho + \alpha - \delta) * t_{scan} + \delta * t_{pivot}$ .

**Indexing Budget.** In this phase, we set delta such that  $\delta = \frac{t_{budget}}{t_{pivot}}$ . For the fixed indexing budget, we select this  $\delta$  for the first query and keep on using this  $\delta$  for the remainder of the workload. For the adaptive indexing budget, we use this formula to select the  $\delta$  for each query.

### Refinement Phase

In the refinement phase, we no longer need to scan the base table. Instead, we only need to scan the fraction  $\alpha$  of the data in the index. However, we now need to (1) traverse the binary tree to figure out the bounds of  $\alpha$ , and (2) swap elements in-place inside the index instead of sequentially writing them to refine the index. The cost for traversing the binary tree is given by the height of the binary tree  $h$  times the cost of a random page access  $\phi$ , resulting in  $t_{lookup} = h * \phi$ . For the swapping of elements, we perform predicated swapping to allow for a constant cost regardless of how many elements we need to swap. Therefore the cost for swapping is equivalent to the cost of sequential writing (i.e.,  $t_{swap} = \kappa * \frac{N}{\gamma}$ ). The total cost in this phase is therefore equivalent to  $t_{total} = t_{lookup} + \alpha * t_{scan} + \delta * t_{swap}$ .

**Indexing Budget.** In this phase, we set delta such that  $\delta = \frac{t_{budget}}{t_{swap}}$  for the adaptive indexing budget.

### Consolidation Phase

In the consolidation phase, we use binary search in the sorted array until the B+-Tree levels are complete. This results in  $t_{lookup} = \log_2(n) * \phi$ . To construct the B+-Tree, we copy every  $\beta$  element from one level to the next. Therefore the cost of copying the elements is the cost of access a random element from the current level and sequentially

write it to the next, defined by  $t_{copy} = N_{copy} * \kappa * \gamma$ . The total cost in this phase is equivalent to  $t_{total} = t_{lookup} + \alpha * t_{scan} + \delta * t_{copy}$ .

**Indexing Budget.** In this phase, we set delta such that  $\delta = \frac{t_{budget}}{t_{copy}}$  for the adaptive indexing budget.

## 4.2 Greedy Progressive Radixsort (MSD)

This section describes the cost model for both the creation and refinement phases of Greedy Progressive Radixsort (MSD). The consolidation phase follows the same cost model as described in Section 4.1. The parameters are summarized in Table 3.1.

### Creation Phase

In the creation phase, the total time taken is the sum of (1) the scan time of the base table, (2) the index lookup time, and (3) the time it takes to add elements to buckets. The scan time of the base table is equivalent to the scan time ( $t_{scan}$ ) given in Section 3.1. Scanning the buckets for the already indexed data has equivalent performance to performing a sequential scan plus the random accesses we need to perform every  $s_b$  elements, hence the scan time of the buckets is equivalent to  $t_{bscan} = t_{scan} + \phi * \frac{N}{s_b}$ . As we determine which bucket an element belongs to only based on the most significant bits, finding the relevant bucket for an element can be done using a single bitshift. As we chose the bucket count such that all bucket regions can fit in cache, the cost of writing elements to buckets is equivalent to sequentially writing them ( $\kappa$ ). We need to perform a memory allocation every  $s_b$  entries, which has a cost of  $\tau$ . This results in a total cost of bucketing equal to  $t_{bucket} = (\kappa + \omega) * \frac{N}{\gamma} + \tau * \frac{N}{s_b}$ . The total cost is therefore  $t_{total} = (1 - \rho - \delta) * t_{scan} + \alpha * t_{bscan} + \delta * t_{bucket}$ .

**Indexing Budget.** In this phase, we set delta such that  $\delta = \frac{t_{budget}}{t_{bucket}}$ . For the fixed indexing budget, we select this  $\delta$  for the first query and keep on using this  $\delta$  for the remainder of the workload. For the adaptive indexing budget, we use this formula to select the  $\delta$  for each query.

### Refinement Phase

The total time taken for a query is the sum of (1) the time taken to scan the required buckets to answer the query predicates and (2) the time taken to perform the radix partitioning of the elements. The time taken to scan the buckets is the same as in the creation phase,  $\alpha * t_{bscan}$ . The time taken for the radix partitioning is  $t_{bucket} = (\kappa + \omega) * \frac{N}{\gamma} + \tau * \frac{N}{s_b}$ . The total cost is therefore  $t_{total} = \alpha * t_{bscan} + \delta * t_{bucket}$ .

**Indexing Budget.** In this phase, we set delta such that  $\delta = \frac{t_{budget}}{t_{bucket}}$  for the adaptive indexing budget.

### 4.3 Greedy Progressive Bucketsort

In this section, we describe the cost model for the creation phase of Greedy Progressive Bucketsort. The refinement and consolidation phases follow the same cost model described in Section 4.1. The parameters are summarized in Table 3.1.

#### Creation Phase

In the creation phase, the cost of the algorithm is identical to that of Progressive Radixsort (MSD) except that determining which element a bucket belongs to now requires us to perform a binary search on the bucket boundaries, costing an additional  $\log_2 b$  time per element we bucket. This results in the following cost for the initial indexing process  $t_{total} = (1 - \rho - \delta) * t_{scan} + \alpha * t_{bscan} + \delta * \log_2 b * t_{bucket}$ .

**Indexing Budget.** In this phase, we set delta such that  $\delta = \frac{t_{budget}}{\log_2 b * t_{bucket}}$ . For the fixed indexing budget, we select this  $\delta$  for the first query and keep on using this  $\delta$  for the remainder of the workload. For the adaptive indexing budget, we use this formula to select the  $\delta$  for each query.

### 4.4 Greedy Progressive Radixsort(LSD)

This section describes the cost model for both the creation and refinement phases of Greedy Progressive Radixsort (LSD). The consolidation phase follows the same cost model as described in Section 4.1. The parameters are summarized in Table 3.1.

#### Creation Phase

The cost model for the Progressive Radixsort (LSD) is also equivalent to the cost model of the Progressive Radixsort (MSD), except the value of  $\alpha$  is likely to be higher for range queries (depending on the query predicates) as the elements that answer the query predicate are spread in more buckets. As scanning the buckets is slower than scanning the original column, we also have a fallback when  $\alpha == \rho$  we scan the original column instead of using the buckets to answer the query.

**Refinement Phase**

In this phase, we scan  $\alpha$  fraction of the original buckets to answer the query and move  $\delta$  fraction of the elements into the new set of buckets. This results in the following cost for the refinement process:  $t_{total} = \alpha * t_{b_{scan}} + \delta * t_{b_{bucket}}$ .

**Indexing Budget.** In this phase, we set delta as  $\delta = \frac{t_{budget}}{t_{bucket}}$  for the adaptive indexing budget.

## 5 Experimental Analysis

In this section, we evaluate the proposed Progressive Indexing methods and the performance characteristics they exhibit. In addition, we provide a comparison of the performance of the proposed methods with Adaptive Indexing methods.

### 5.1 Setup.

We implemented all our Progressive Indexing algorithms in a stand-alone program written in C++. We included implementations of the Adaptive Indexing algorithms provided by the authors and implemented an adaptive cracking kernel algorithm that picks the most efficient kernel when executing a query, following the decision tree from Haffner et al. [25]. Both the Progressive Indexing algorithms and the existing techniques were compiled with GNU g++ version 7.2.1 using optimization level -O3. All experiments were conducted on a machine equipped with 256 GB of main memory and an 8-core Intel Xeon E5-2650 v2 CPU @ 2.6 GHz with 20480 KB L3 cache.

### Workloads

In the performance evaluation, we use two data sets a real data set called Skyserver and a synthetic data set.

### Skyserver

The Sloan Digital Sky Survey<sup>2</sup> is a project that maps the universe. The data set and interactive data exploration query logs are publicly available via the SkyServer<sup>3</sup> website. Similar to Halim et al. [26] we focus the benchmark on the range queries that are applied on the *Right Ascension* column of the *PhotoObjAll* table. The data set

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<sup>2</sup><https://www.sdss.org/>

<sup>3</sup><http://skyserver.sdss.org/>

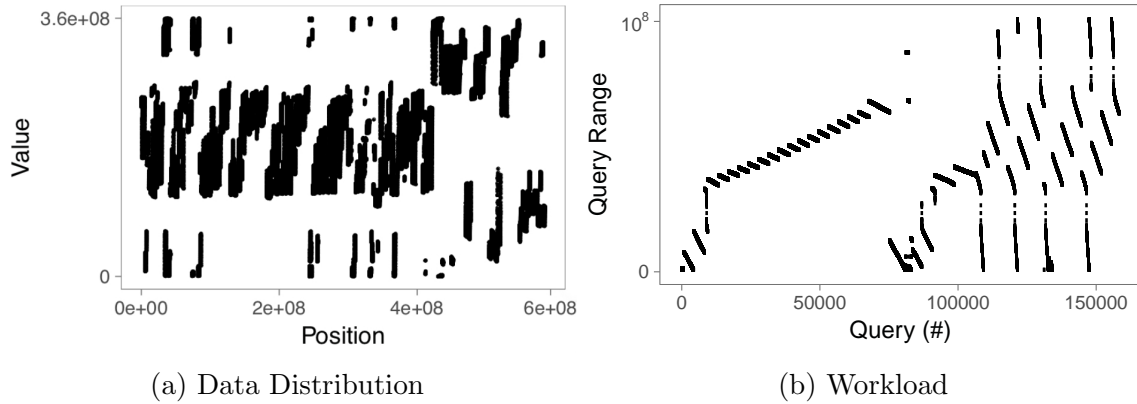


Figure 3-9: Skyserver

contains almost 600 million tuples, with around 160,000 range queries that focus on specific sections of the domain before moving to different areas. The data and the workload distributions are shown in Figure 3-9.

### Synthetic

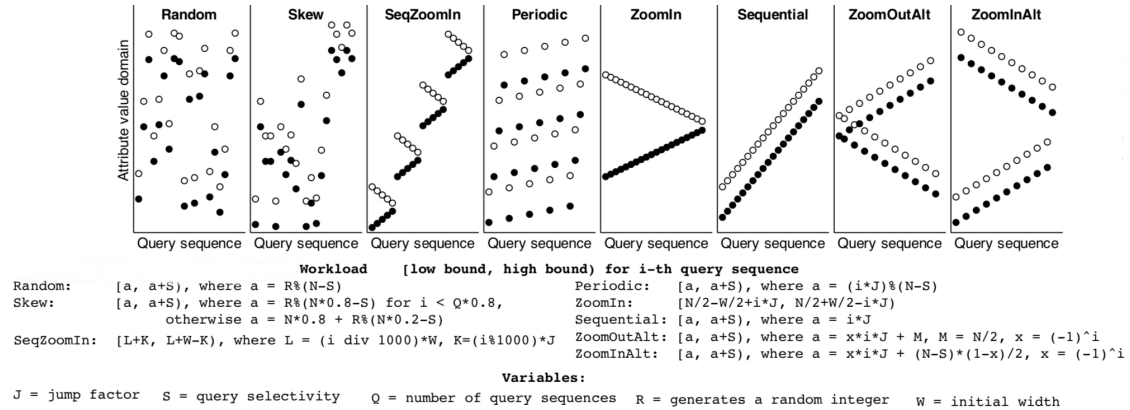


Figure 3-10: Synthetic Workloads [26].

**Synthetic.** The synthetic data set is composed of two data distributions, consisting of  $10^8$  or  $10^9$  8-byte integers distributed in the range of  $[0, n)$ , i.e., for  $10^9$  the values are in the range of  $[0, 10^9)$ . We use two different data sets. The first one is composed of unique integers that are uniformly distributed. In contrast, the second one follows a skewed distribution with non-unique integers where 90% of the data is concentrated in the middle of the  $[0, n)$  range. The synthetic workload consists of  $10^6$  queries in the form `SELECT SUM(R.A) FROM R WHERE R.A BETWEEN  $V_1$  AND  $V_2$` . The values for  $V_1$  and  $V_2$  are chosen based on the workload pattern. The different workload patterns and their mathematical description are depicted in Figure 3-10.



## 5.2 Delta Impact

The  $\delta$  parameter determines the performance characteristics shown by the Progressive Indexing algorithms. For  $\delta = 0$ , no indexing is performed, meaning that algorithms resort to performing full scans on the data, never converging to a full index. For  $\delta = 1$ , the entire creation phase will be completed immediately during the first query execution. Between these two extremes, we are interested in seeing how different values of the  $\delta$  parameter influence the performance characteristics of the different algorithms.

To measure the impact of different  $\delta$  parameters on the different algorithms, we execute the SkyServer workload using a  $\delta \in [0.005, 1]$ . We measure the time taken for the first query, the number of queries until pay-off, the number of queries necessary for full convergence, and the total time spent executing the entire workload.

### First Query.

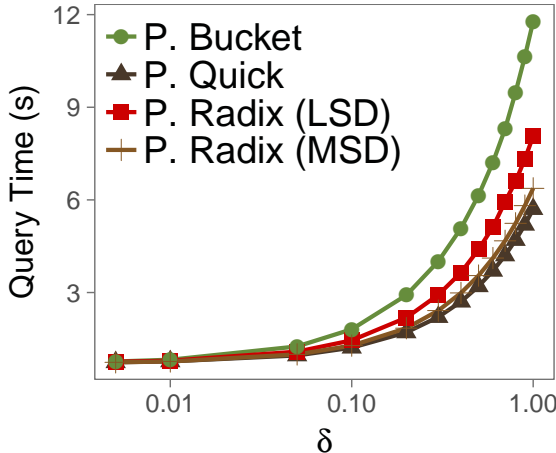


Figure 3-11: First Query.

Figure 3-11 shows the performance of the first query for varying values of  $\delta$ . The first query’s performance degrades as  $\delta$  increases since each query does extra work proportional to  $\delta$ . For every algorithm, however, the amount of extra work done differs.

We can see that Bucketsort is impacted the most by increasing  $\delta$ . This is because determining which bucket an element falls into costs  $O(\log b)$  time, followed by a random write for inserting the element into the bucket. Radixsort, despite its similar nature to Bucketsort, is impacted much less heavily by an increased  $\delta$ . This is because determining which bucket an element falls into costs constant  $O(1)$  time. Quicksort

experiences the lowest impact from an increasing  $\delta$ , as elements are always written to only two memory locations (the top and bottom of the array), the extra sequential writes are not very expensive.

### Pay-Off.

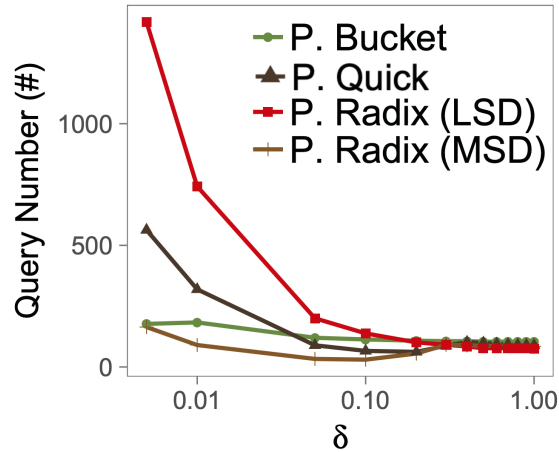


Figure 3-12: Pay-Off.

Figure 3-12 shows the number of queries required until the Progressive Indexing technique becomes worth the investment (i.e., the query number  $q$  for which  $\sum_q t_{prog} \leq \sum_q t_{scan}$ ) for varying values of  $\delta$ . We observe that with a very small  $\delta$ , it takes many queries until the indexing pays off. While a small  $\delta$  ensures low first query costs, it significantly limits the progress of index-creation per query, and consequently, the speed-up of query processing. With increasing  $\delta$ , the number of queries required until pay-off quickly drops to a stable level.

We see that Radixsort (LSD) needs a very high amount of queries to pay-off for low values of  $\delta$ . This is because the intermediate index cannot accelerate range queries until the index fully converges. When the value of  $\delta$  is high, the index converges faster and can be utilized to answer range queries earlier. Quicksort also has a high time to pay-off with a low delta because the intermediate index can only be used to accelerate range queries that do not contain the pivots. Hence in the early stages of the index, the table often needs to be scanned. Bucketsort and Radixsort (MSD) do not suffer from these problems. Hence they pay-off fast even with lower values for  $\delta$ .

### Convergence.

The  $\delta$  parameter affects the convergence speed towards a full index. When  $\delta = 0$ , the index will never converge, and a higher value for  $\delta$  will cause the index to converge

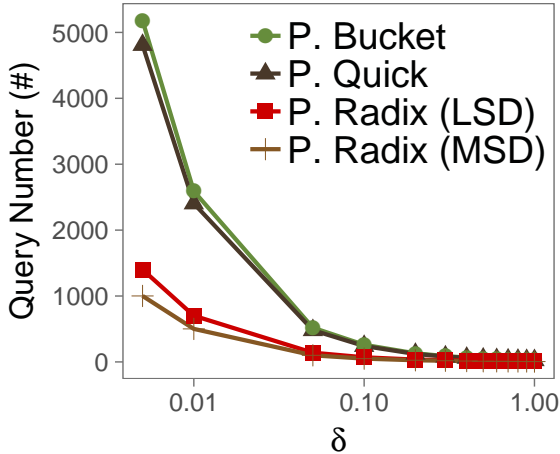


Figure 3-13: Convergence.

faster as more work is done per query on building the index.

Figure 3-13 shows the number of queries required until the index converges towards a full index. We see that Radixsort converges the fastest, even with a low  $\delta$ . It is followed by Quicksort and then Bucketsort.

The reason Radixsort converges in so few iterations is because it uses radix partitioning, which means that after  $\lceil \log_2(n)/\log_2(b) \rceil = \lceil \log_2(10^9)/\log_2(64) \rceil = 5$  partitioning rounds the index is fully converged. Bucketsort uses Quicksort pivoting, which requires more passes over the data.

**Cumulative Time.**

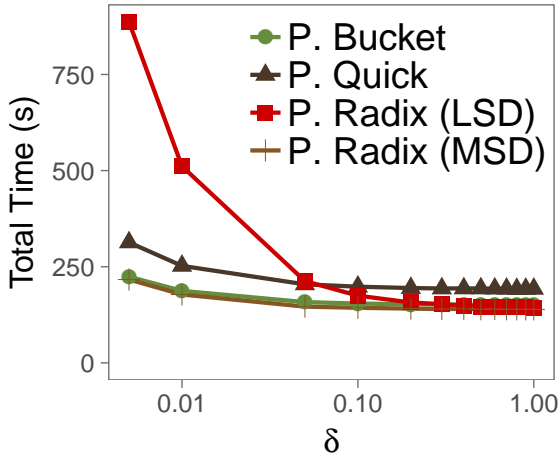


Figure 3-14: Total Time.

As we have seen before, a high value for  $\delta$  means that more time is spent constructing the index, meaning that the index converges towards a full index faster. While earlier

queries take longer with a higher value of  $\delta$ , subsequent queries take less time. Another interesting measurement is the cumulative time spent on answering a large number of queries. Does the increased investment in index creation earlier on pay off in the long run?

Figure 3-14 depicts the cumulative query cost. We can see that a higher value of  $\delta$  leads to a lower cumulative time. Converging towards a full index requires the same amount of time spent constructing the index, regardless of the value of  $\delta$ . However, when  $\delta$  is higher, that work is spent earlier on (during fewer queries), and queries can benefit from the constructed index earlier.

Progressive Quicksort and Radixsort (LSD) perform poorly when the delta is low. For Quicksort, this is because it will take many queries to finish our pivoting in one element. While in Radixsort (LSD), the intermediate index that is created cannot be effectively used to answer range queries before it fully converges, meaning a long time until convergence results in poor cumulative time. Progressive Bucketsort and Radixsort (MSD) perform better than Progressive Quicksort for all values of  $\delta$ , with Radixsort (MSD) slightly outperforming Bucketsort.

Another observation here is that the cumulative time converges rather quickly with an increasing delta. The cumulative time with  $\delta = 0.25$  and  $\delta = 1$  are almost identical for all algorithms, while the penalization of the initial query continues to increase significantly (recall Figure 3-11).

### 5.3 Cost Model Validation

For both the fixed indexing budget and the adaptive indexing budget of Greedy Progressive Indexing, we need the cost models presented in Section 4 to estimate the actual query processing and index creation costs. For the fixed indexing budget, we need the cost model to compute the initial value of  $\delta$  based on the desired indexing budget. For the adaptive indexing budget, we need the cost model to adapt the value of  $\delta$  for each query to the current minimum query cost.

In this set of experiments, we experimentally validate our cost models. To use the cost models in practice, we need to obtain values for all of the constants used, such as the scanning speed and the cost of a cache miss. Since these constants depend on the hardware, we perform these operations when the program starts up and measure how long it takes to perform these operations. The measured values are then used as the constants in our cost model.

**Fixed Indexing Budget.**

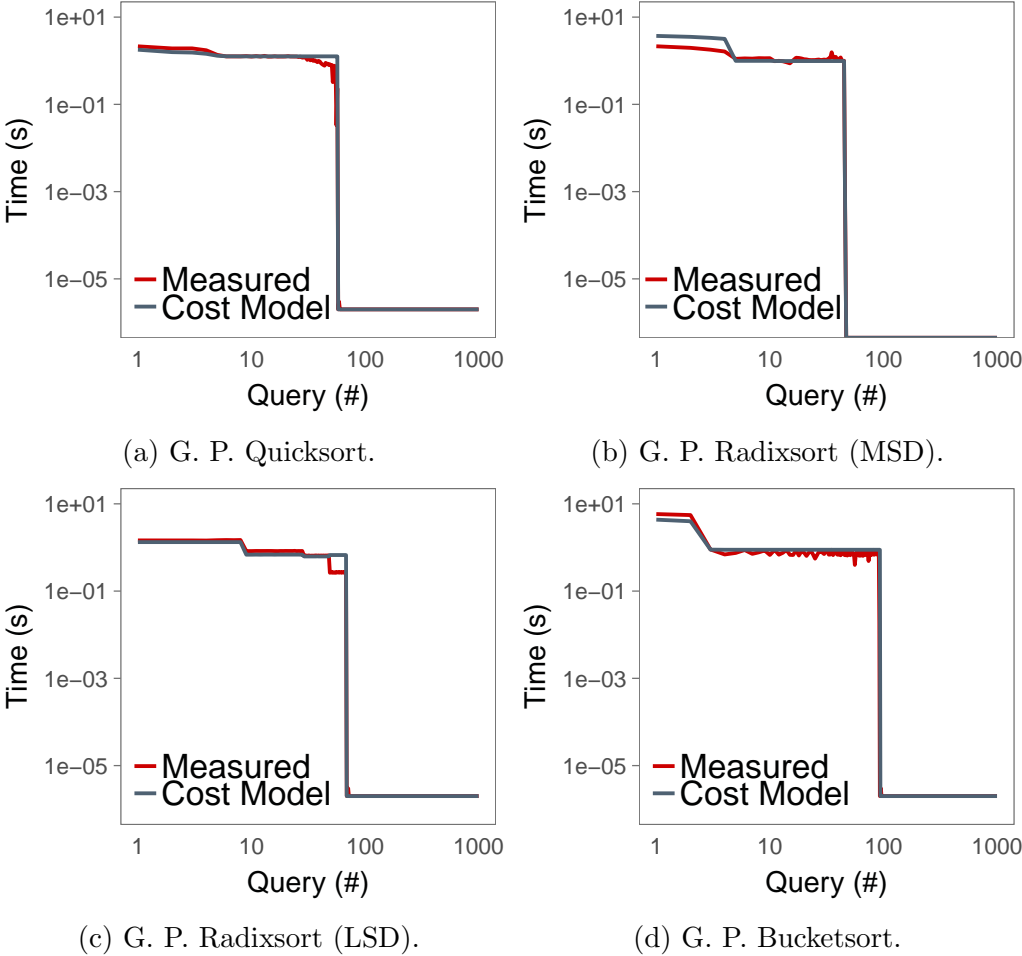


Figure 3-15: SkyServer Workload with Fixed Indexing Budget (all axes in log scale)

Before diving into the details of choosing a variable  $\delta$  per query for the adaptive indexing budget, we first experimentally validate our cost models. We run the SkyServer benchmark with a constant  $\delta = 0.25$  for the entire query sequence and compare the measured execution times with the times predicted by our cost models.

Figure 3-15 shows the results for all four Greedy Progressive Indexing techniques we propose. The graphs depict the individual phases of our algorithms (cf., Section 3) and show that significant improvements in query performance happen mainly with the transition from one phase to the next. Given that  $\delta$  determines the fraction of data that is to be considered for index refinement with each query (rather than a fraction of the full scan cost), the different techniques depict different per query cost, depending on the respective index refinement operations performed as well as the efficiency of the respective partially built indexes. The graphs also show that our cost

models predict the actual costs well, accurately predicting each phase transition and the point when the full index has been finalized, and no further indexing is required.

**adaptive indexing budget.**

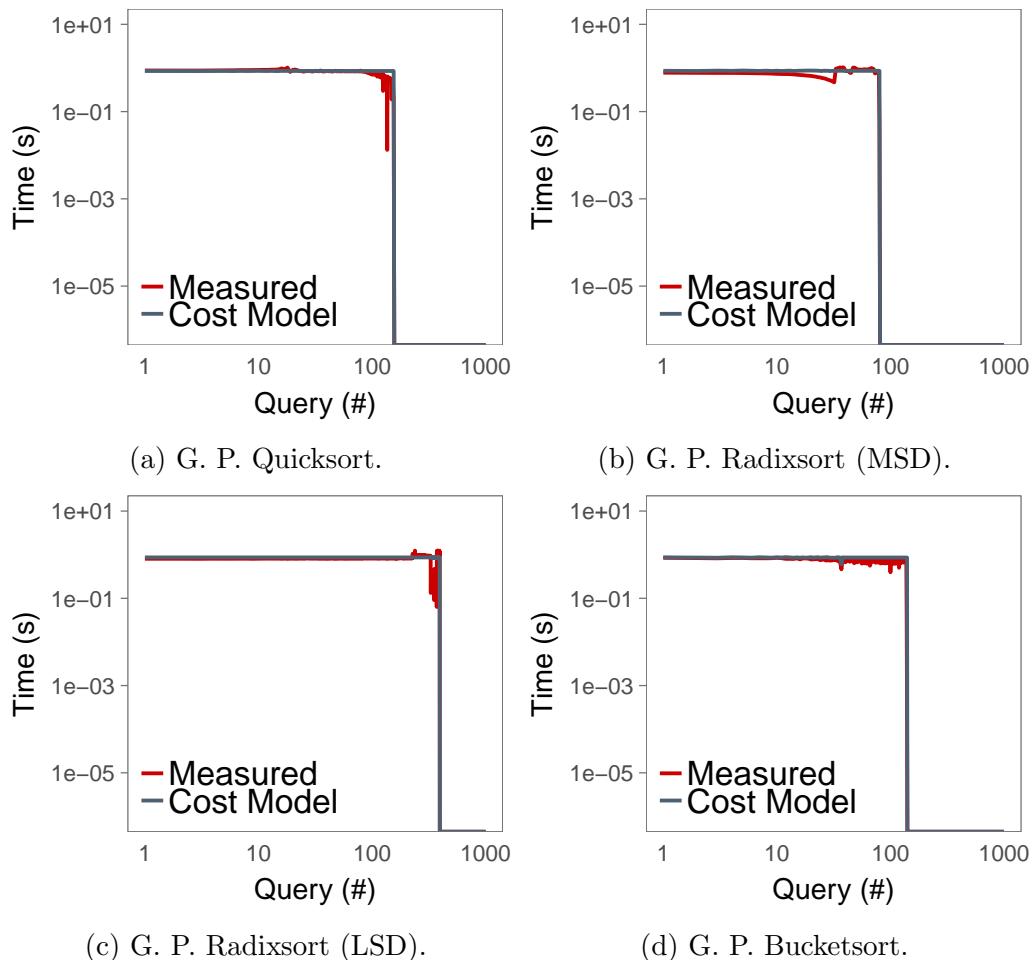


Figure 3-16: SkyServer Workload with adaptive indexing budget (all axes in log scale)

With our cost models validated, we now run the SkyServer benchmark with all four Greedy Progressive Indexing techniques with the adaptive indexing budget. We select  $t_{budget} = 0.2 * t_{scan}$ , i.e., the indexing budget is selected as 20% of the full scan cost. Figure 3-16 depicts the results of this experiment for each of the algorithms. In all graphs, we observe that the total execution time stays close to constant at a high level, matching the given budget until the index is fully built, and no further refinement is required.

In Figure 3-16a, the measured and predicted time are shown for the Greedy Progressive Quicksort algorithm. Initially, the cost model accurately predicts the

performance of the algorithm. However, close to convergence, the cost model predicts a slightly higher execution time. As the pieces become smaller, they start fitting inside the CPU caches entirely, which results in faster swaps than predicted by our cost model.

In Figure 3-16b, the measured and predicted time are shown for the Greedy Progressive Radixsort (MSD) algorithm. In the initialization phase, the cost model matches the measured time initially, but the measured time slightly decreases below the cost model as the initialization progresses. This is because the data distribution is relatively skewed, which results in the same buckets being scanned for every query, which will then be cache resident and faster than predicted. In the refinement phase, there are some minor deviations from the cost model caused by smaller radix partitions fitting in CPU caches, which our cost model does not accurately predict.

In Figure 3-16c, the measured and predicted time are shown for the Greedy Progressive Radixsort (LSD) algorithm. The cost model accurately predicts the performance of the initialization and refinement phases of the algorithm but results in several spikes later in the refinement phase. These spikes occur because the workload we are using consists of very wide range queries. These range queries can only take advantage of the LSD index depending on the exact range queries issued. Thus, certain queries can be answered much faster using the index, whereas others cannot use the index at all. As our cost model is pessimistic, this results in the measured time being faster than the predicted time.

In Figure 3-16d, the measured and predicted time are shown for the Greedy Progressive Bucketsort algorithm. In the initialization phase, the cost model closely matches the measured time. After it, Greedy Progressive Quicksort is used to merge the different buckets into a single sorted array. The different iterations of Greedy Progressive Quicksort each have small downwards spikes when the pieces start fitting inside the CPU caches.

## 5.4 Interactivity Threshold

In the previous workload, we have shown our cost models' effectiveness at staying on a specific interactivity threshold. In this experiment, we want to show how the algorithms perform at different interactivity thresholds based on the full scan cost. In this experiment, we show three different scenarios: (1) the interactivity threshold is below the full scan cost, (2) the interactivity threshold is above the full scan cost, and (3) the interactivity threshold decreases with the number of queries issued.

**Threshold Below Full Scan Cost.**

In the first scenario, the initial runs will always be above the interactivity threshold as even the full scan cannot reach it. In this scenario, we start by setting  $\delta$  to 0.25. In Section 5.2 we determined this provides a fast convergence rate while not heavily penalizing the initial queries. After the index has reached the state where it can answer queries below the interactivity threshold,  $\delta$  is set such that the query cost stays on the interactivity threshold until convergence.

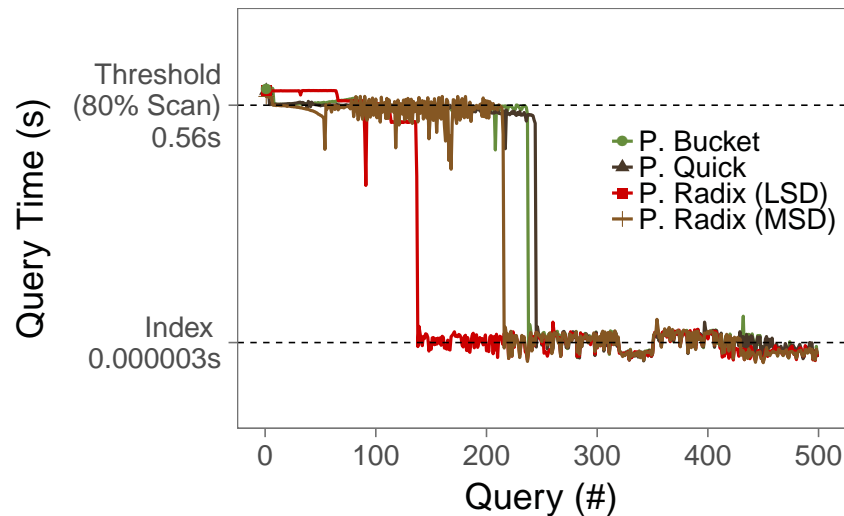


Figure 3-17: Threshold of 80% Scan Cost (Y-Axis in log scale)

Figure 3-17 shows the results for this experiment. We can see that all queries start above the interactivity threshold, after which they gradually move towards it. The Greedy Progressive Quicksort and Radixsort (MSD) quickly reach the interactivity threshold. The Radixsort (LSD) takes the longest to reach it. This is because the wide range queries cannot take advantage of the LSD radix index structure to speed up answering the queries. However, because it stays on the  $\delta$  of 0.25 the longest, i.e., it performs more indexing work with more initial queries, it does converge the fastest.

Figure 3-18 shows the time spent on indexing versus the time spent on query processing for the Greedy Progressive Quicksort in this scenario. At the start, a significant amount of time is spent on indexing as the interactivity threshold cannot be reached yet. After the index is sufficiently converged, the interactivity threshold can be reached, and the fixed  $\delta = 0.25$  is replaced by a variable per-query  $\delta$  as discussed in Section 5.2, which is initially rather small given that the time budget between query processing cost and interactivity threshold is small. As more data gets indexed, the query processing cost gradually decreases. Consequently,  $\delta$  is gradually



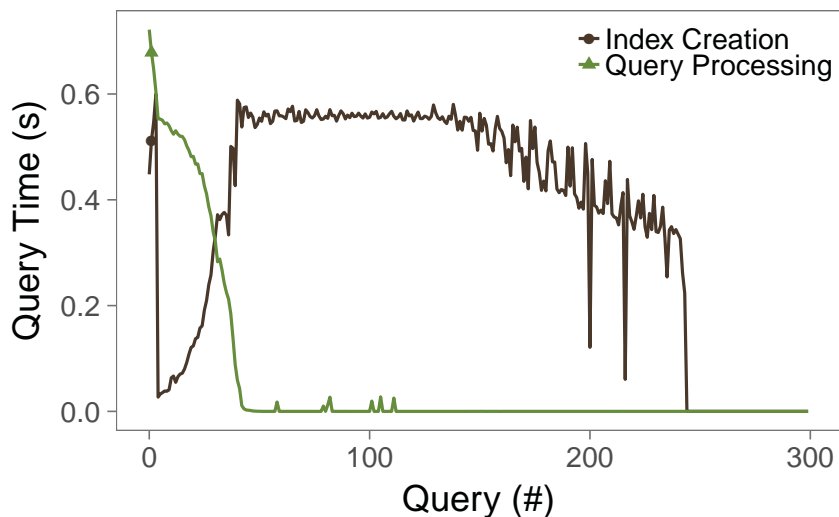


Figure 3-18: Progressive Quicksort - Query Processing vs. Index Creation

increased, allowing to spend more time on index creation per query until the index fully converges.

### Threshold Above Full Scan Cost.

In the second scenario, all the greedy algorithms can stay on the interactivity threshold above the full scan cost. The only difference is the time until convergence for each of the algorithms. These differ based on how much extra time we can spend on index creation, which depends on how much the interactivity threshold is above the full scan cost. For this reason, we performed two separate experiments, one where the interactivity threshold is  $1.2x$  the full scan cost and one where it is  $2x$  the full scan cost.

Figure 3-19 shows the experiment results where the threshold is  $1.2x$  the scan cost. In this experiment, the Radixsort (MSD) converges the fastest, and the Radixsort (LSD) converges the slowest. This is because the intermediate index created by the Radixsort (LSD) cannot be effectively used to speed up the range queries, and the  $\delta$  will stay at a fixed low number until convergence. As the interactivity threshold is so close to a full scan, this value will be very low. The other indexes can use the intermediate index to speed up the query processing, resulting in an increasing  $\delta$  that improves convergence time.

Figure 3-20 shows the results of the experiment where the threshold is  $2x$  the scan cost. In this experiment, the Radixsort (LSD) converges the fastest. While the intermediate index still cannot speed up the query, as the full scan only takes

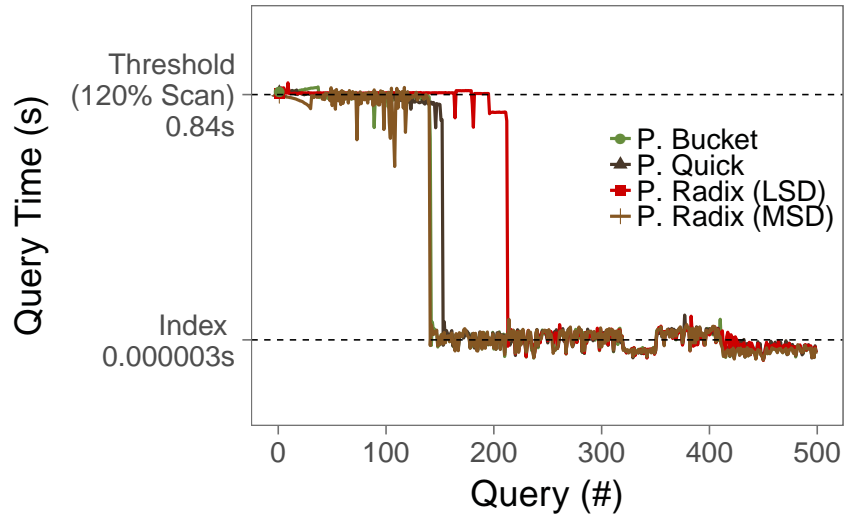


Figure 3-19: Threshold of 120% Scan Cost (Y-Axis in log scale)

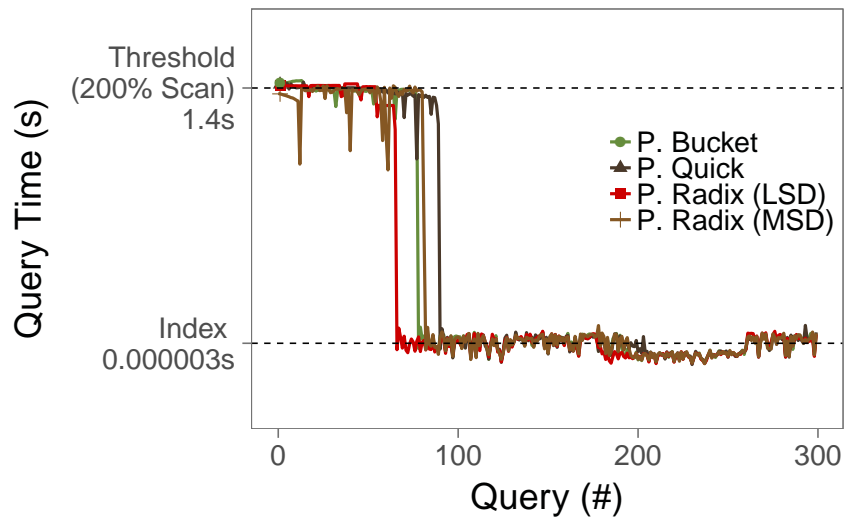


Figure 3-20: Threshold of 200% Scan Cost (Y-Axis in log scale)

up half the interactivity threshold, the amount of time spent on index refinement is significantly higher than in the previous experiment for all algorithms. As the Progressive Radixsort (LSD) has the fastest convergence, as shown in Figure 3-13, it is now the fastest converging algorithm.

## 5.5 Varying Interactivity

So far, we have used the same fixed interactivity threshold for all queries. Fully exploiting the time budget between this threshold and pure query processing cost for index creation ensures faster convergence towards a full index. However, it also results

in a rather discrete behavior: All initial queries (including index refinement) take as long as allowed by the interactivity threshold. Once the full index is entirely built, query times abruptly drop to the optimal times using the index. This behavior might not always be desirable. Instead, a more gradual convergence of the query execution times from the given interactivity threshold to the optimal case might be preferred, possibly at the expense of slightly slower convergence.

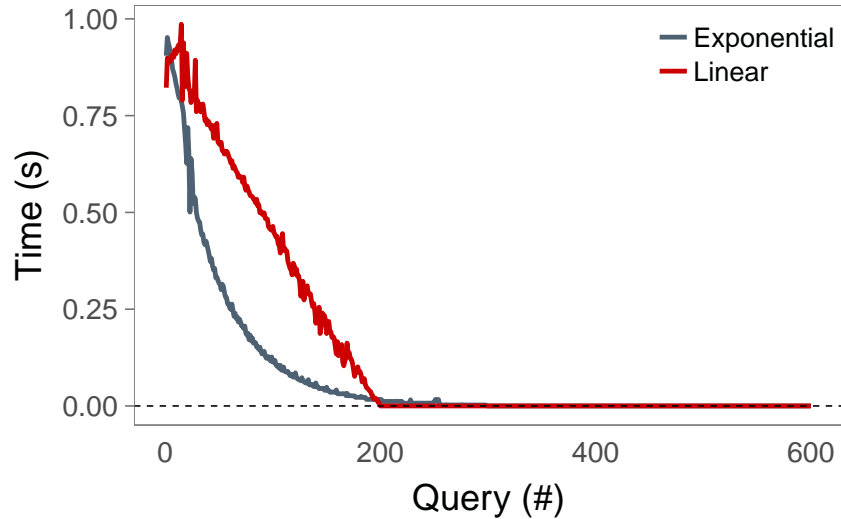


Figure 3-21: Exponential and Linear Decay

We can mimic such behavior by monotonously decreasing the interactivity threshold with the query sequence, ensuring that at any time, the interactivity threshold remains high enough so that the queries can be completed within that threshold. Again, using our cost model, we can automatically determine the respective values for  $\delta$ . We perform two experiments using linear and exponential decay formulas to model the decreasing the interactivity threshold depicted in Figure 3-21.

For the linear decay, we set our formula as  $t_q = I - r * q$  where  $I$  is the initial interactivity threshold,  $t_q$  is the total time spent on query number  $q$ , and  $r$  is the decreasing ratio. We use the following formula to calculate the decay ratio  $r = -\frac{t_{FI} - I}{n}$  where  $t_{FI}$  is the estimated full index time and  $n$  is the amount of queries until convergence to time  $t_{FI}$ . For this experiment, we use Progressive Quicksort with  $n = 200$  and the initial interactivity threshold set to  $1.2x$  the full scan time. We can see that we can gradually push down the execution time as the index converges by gradually decreasing the interactivity threshold.

For the exponential decay, we use the exponential decay formula  $t_q = I(1 - r)^q$ . To determine  $r$ , we use the following formula  $r = 1 - \sqrt[n]{\frac{t_{FI}}{I}}$ . For this experiment, we use Progressive Quicksort with  $n = 300$  and the initial interactivity threshold set to  $1.2x$

the full scan time. Like the linear decay, we can see that the measured time closely follows the interactivity threshold.

## 5.6 Adaptive Indexing Comparison

In this section, we will be comparing the greedy Progressive Indexing techniques with existing Adaptive Indexing techniques. In particular, we focus on Standard Cracking (STD), Stochastic Cracking (STC), progressive Stochastic Cracking (PSTC), Coarse Granular Index (CGI), and Adaptive Adaptive Indexing (AA).

The implementations for the Full Index, Standard Cracking, Stochastic Cracking, and Coarse Granular Index were inspired by the work done in Schuhknecht et al. [50]<sup>4</sup>. The implementation for Progressive Stochastic Cracking was inspired by the work done in Halim et al. [26]<sup>5</sup>. Progressive Stochastic Cracking is run with the allowed swaps set to 10% of the base column. The implementation for the Adaptive Adaptive Indexing algorithm has been provided to us by the authors of the Adaptive Adaptive Indexing work [49], and we use the manual configuration suggested in their paper.

We compare all the Progressive Indexing techniques that we have introduced in this work: Greedy Progressive Quicksort (PQ), Greedy Progressive Bucketsort (PB), Greedy Progressive Radixsort LSD (PLSD), and Greedy Progressive Radixsort MSD (PMSD). For each of the techniques, we use an adaptive indexing budget where we set  $t_{budget} = 0.2 * t_{scan}$ , i.e., the cost of each query will be equivalent to  $1.2 * t_{scan}$  until convergence.

For reference, we also include the timing results when only performing full scans on the data (FS) and when constructing a full index immediately on the first query (FI). The full scan implementation uses predication to avoid branches, and the full index bulk loads the data into a B+-tree, after which the B+-tree is used to answer subsequent queries.

**Metrics.** The metrics that we are interested in are the time taken for the first query, the number of queries required until convergence, the robustness of each of the algorithms, and the cumulative response time. The robustness we compute by taking the variance of the first 100 query times.

Table 3.2: SkyServer Results

Index	First Q	Convergence	Robustness	Cumulative
FS	0.75	x	0	118743.7
FI	34.10	1	x	121.4
STD	5.26	x	0.290	1082.2
STC	4.99	x	0.250	245.6
PSTC	4.89	x	0.240	254.5
CGI	5.71	x	0.320	1008.9
AA	8.50	x	0.800	188.4
PQ	0.90	150	0.002	202.9
PMSD	0.90	119	0.030	157.5
PLSD	0.81	368	3.4e-05	377.4
PB	0.83	138	0.009	166.4

### SkyServer Workload

In this part of the experiments section, we execute the full SkyServer workload using different indexing techniques. The results for each of the indexing techniques are shown in Table 3.2. The algorithms have been divided into three sections: the baseline, the Adaptive Indexing techniques, and the Progressive Indexing techniques.

The results for the baseline techniques are not very surprising. The full scan method is the most robust, as we use predication, and no index is constructed. The cost of each query is identical. The full scan method is also the cheapest method for the first query’s cost as no time is spent on indexing at all. The full scan, however, takes significantly longer to answer the full workload than the other methods. Answering the full workload takes almost 30 hours, whereas all the other techniques finish the entire workload under 20 minutes. The full index lies at the other extreme. It takes  $50x$  longer to answer the first query while the index is being constructed. However, it has the lowest cumulative time as the index can quickly answer all of the remaining queries.

For the Adaptive Indexing techniques, we can see that their first query cost is significantly lower than that of a full index but still significantly higher than that of a full scan. Each of the Adaptive Indexing methods performs a significant amount of work copying the data and cracking the index on the first query, resulting in a very high cost for the first query. They do achieve a significantly faster cumulative time than the full scans. However, in sum, they take longer than the full index to answer the workload. Standard Cracking and Coarse Granular Indexing perform particularly

<sup>4</sup>[https://infosys.uni-saarland.de/publications/uncracked\\_pieces\\_sourcecode.zip](https://infosys.uni-saarland.de/publications/uncracked_pieces_sourcecode.zip)

<sup>5</sup><https://github.com/felix-halim/scrack>

poorly because of the workload’s sequential nature, as shown in Figure 3-9. Stochastic Cracking and Adaptive Indexing perform better as they do not choose the pivots based on the query predicates. Adaptive Adaptive Indexing has the best cumulative performance, consistent with the results in Schuhknecht et al. [49].

The Progressive Indexing methods all have approximately the same cost for the first query, which is  $1.2x$  the scan cost. This is by design as we set the indexing budget  $t_{budget} = 0.2 * t_{scan}$  for each of the algorithms. The main difference between the algorithms is the robustness and the time until convergence. As we are executing range queries, the Radixsort LSD performs the worst. The LSD partitioning cannot help answer the range queries, and hence, the intermediate index does not speed up the workload before convergence. Radixsort MSD performs the best, as the data set is rather uniformly distributed. The radix partitioning works to efficiently create a partitioning of the data, which can be immediately utilized to speed up subsequent queries. For each of the Progressive Indexing methods, we see that they converge relatively early in the workload. As we have set every query to take  $1.2 * t_{scan}$  until convergence, a significant amount of time can be spent on constructing the index for each query, especially in later queries when the intermediate index can already be used to obtain the answer efficiently. We also note that the Progressive Indexing methods have a significantly higher robustness score than the Adaptive Indexing methods. Progressive Indexing presents up to 4 orders of magnitude lower query variance when compared to the Adaptive Indexing techniques. This is achieved by our cost model balancing the per query execution cost to be (almost) the same until convergence, while Adaptive Indexing suffers from many performance spikes.

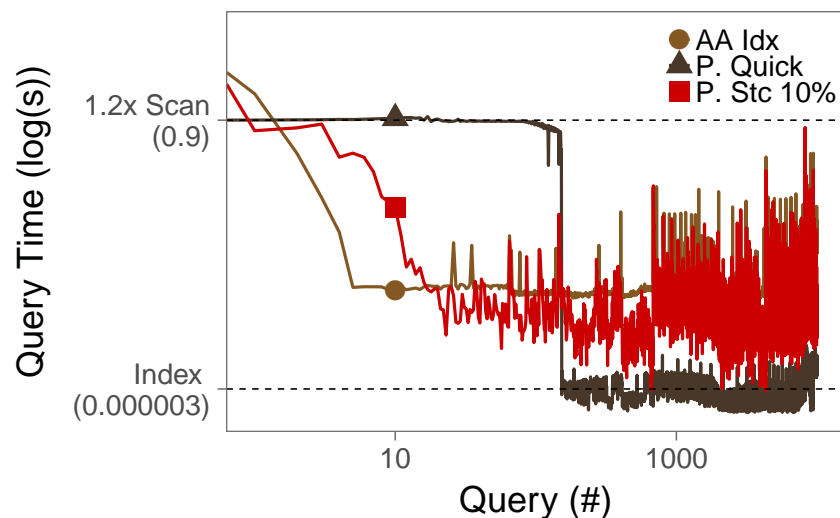


Figure 3-22: Progressive Quicksort vs Adaptive Indexing. (all axes in log scale)

The execution time for each of the queries in the SkyServer workload is shown in Figure 3-22. For clarity, we focus on the best Adaptive Indexing methods (Adaptive Adaptive Indexing in terms of cumulative time, and Progressive Stochastic 10% in terms of first query cost and robustness) and Progressive Quicksort. We can see that both the Adaptive Indexing methods start with a significantly higher first query cost and then fall quickly. Neither of them sufficiently converges, however, and both continue to have many performance spikes. On the other hand, Progressive Quicksort starts at the specified budget and maintains that query cost until convergence, after which the cost drops to the cost of a full index.

### Synthetic Workloads

In this part of our experiments, we execute all synthetic workloads described in Section 5.1. All results are presented in tables. Each table is divided into four parts, each representing one set of experiments. The first three are on data with  $10^8$  elements and use random distribution, skewed distribution, and only point queries, respectively. The final one is on  $10^9$  elements on random distribution. With the exception of point queries and the ZoomIn and SeqZoomIn workloads, all queries have 0.1 selectivities. From the Adaptive Indexing techniques, Adaptive Adaptive Indexing presents the best cumulative time. Hence we select it for comparison. As previously, we set the indexing budget  $t_{budget} = 0.2 * t_{scan}$  for each Progressive Indexing algorithm.

Table 3.3 depicts the cost of the first query for all algorithms. All Progressive Indexing algorithms present a similar first query cost, which accounts for approximately  $1.2x$  the scan cost, as chosen in our setup. Adaptive Indexing has a higher cost due to the complete copy of the data and its full partition step in the first query. In general, Progressive Indexing has one order of magnitude faster first query cost than Adaptive Indexing.

Table 3.4 depicts the cumulative time of fully executing each workload. We can see that Progressive Indexing outperforms Adaptive Indexing in most workloads under uniform random data, except for the skewed and the periodic workload. This comes with no surprise since Adaptive Indexing techniques have been designed to refine, and boost access, to frequently accessed parts of the data. From the progressive algorithms, radixsort (MSD) is the fastest since radixsort can outperform other techniques under randomly distributed data.

For the skewed distribution, Adaptive Indexing outperforms Progressive Indexing in almost all workloads due to its refinement strategy. However, Progressive Indexing outperforms Adaptive Indexing for ZoomIn/Out workloads since each query accesses a

Table 3.3: First query cost

	Workload	PQ	PB	PLSD	PMSD	AA
Uniform Random	SeqOver	0.15	0.15	0.14	0.14	1.4
	ZoomOutAlt	0.15	0.15	0.14	0.14	1.4
	Skew	0.15	0.15	0.14	0.14	1.4
	Random	0.15	0.15	0.14	0.14	1.4
	SeqZoomIn	0.15	0.15	0.14	0.14	1.4
	Periodic	0.15	0.15	0.14	0.14	1.4
	ZoomInAlt	0.15	0.15	0.14	0.14	1.4
	ZoomIn	0.15	0.15	0.14	0.14	1.4
Skewed	SeqOver	0.15	0.15	0.14	0.14	1.5
	ZoomOutAlt	0.15	0.15	0.14	0.13	1.5
	Skew	0.15	0.15	0.14	0.13	1.5
	Random	0.15	0.15	0.13	0.13	1.5
	SeqZoomIn	0.15	0.15	0.14	0.13	1.5
	Periodic	0.15	0.15	0.14	0.13	1.5
	ZoomInAlt	0.15	0.15	0.14	0.14	1.5
	ZoomIn	0.15	0.15	0.14	0.14	1.5
Point Query	SeqOver	0.15	0.15	0.21	0.14	1.4
	ZoomOutAlt	0.15	0.15	0.21	0.14	1.4
	Skew	0.15	0.15	0.21	0.14	1.4
	Random	0.15	0.15	0.21	0.14	1.4
	Periodic	0.15	0.15	0.21	0.14	1.4
	ZoomInAlt	0.15	0.15	0.21	0.14	1.4
10 <sup>9</sup>	SeqOver	1.5	1.5	1.4	1.7	13.9
	Skew	1.5	1.5	1.4	1.7	13.8
	Random	1.5	1.5	1.4	1.7	25.4

different partition in different boundaries of the data, which leads to Adaptive Indexing accessing large unrefined pieces in the initial queries. From the progressive algorithms, bucketsort presents the fastest times since it generates equal-sized partitions for skewed data distributions.

For point queries, radixsort (LSD) outperforms all algorithms in all workloads since its intermediate index can be used early on to accelerate point queries.

Finally, for the 10<sup>9</sup> data size, Progressive Indexing manages to outperform adaptive indexing even for the skewed workload. The key difference here is that the chunks of unrefined data are bigger, and Progressive Indexing actually spends the time fully converging them into small pieces. At the same time, Adaptive Indexing must manage larger pieces of data.

Table 3.5 presents the robustness of the indexing algorithms. Progressive Indexing presents up to four orders of magnitudes less variance than Adaptive Indexing. This is due to the design characteristic of Progressive Indexing to inflict a controlled indexing



Table 3.4: Cumulative Time

	Workload	PQ	PB	PLSD	PMSD	AA
Uniform Random	SeqOver	19.0	17.9	48.2	16.2	20.7
	ZoomOutAlt	20.7	28.3	59.5	26.7	22.1
	Skew	18.8	17.7	48.1	15.9	10.1
	Random	24.7	22.8	53.1	21.1	29.1
	SeqZoomIn	22.0	20.9	53.5	19.3	21.1
	Periodic	23.3	22.0	63.9	20.4	18.4
	ZoomInAlt	20.8	23.3	54.2	21.6	21.7
	ZoomIn	167.0	165.0	210.0	164.0	277.0
Skewed	SeqOver	21.8	30.0	59.7	21.7	17.5
	ZoomOutAlt	21.5	30.2	64.4	63.7	41.1
	Skew	17.4	15.3	45.5	17.3	5.7
	Random	24.0	21.6	51.5	23.8	23.9
	SeqZoomIn	23.3	21.2	52.6	23.1	18.3
	Periodic	23.3	21.3	64.2	23.3	17.0
	ZoomInAlt	22.2	25.1	54.8	21.8	33.5
	ZoomIn	938.0	919.0	934.0	917.0	1655.0
Point Query	SeqOver	16.7	15.7	13.2	14.0	15.1
	ZoomOutAlt	17.7	15.8	13.0	14.0	15.5
	Skew	16.6	15.5	12.7	13.7	5.6
	Random	18.4	16.5	13.6	14.7	14.4
	Periodic	16.8	15.7	13.0	14.3	5.7
	ZoomInAlt	17.7	15.9	13.2	14.1	15.2
10 <sup>9</sup>	SeqOver	516	493	924	480	653
	Skew	538	513	885	487	582
	Random	773	718	1579	692	1104

penalty. For uniform random and skewed distributions, radixsort LSD presents the least variance. This is due to the cost model noticing that the intermediate index created by LSD cannot be used to boost query access, hence knowing the precise cost of executing the query (i.e., a full scan cost). However, for point queries, the intermediate index from LSD can already be used, which reduces the cost model accuracy.

## 6 Summary

This chapter introduces Progressive Indexing, a novel incremental indexing technique that offers robust and predictable query performance under different workloads. Progressive techniques perform indexing within an interactivity threshold and provide a balance between fast convergence towards a full index together with a small performance penalty for the initial queries. We propose four different Progressive Indexing

Table 3.5: Robustness

	Workload	PQ	PB	PLSD	PMSD	AA
Uniform Random	SeqOver	2.4e-04	5.8e-04	2.2e-05	2.1e-04	0.02
	ZoomOutAlt	1.7e-04	6.0e-04	2.1e-05	2.1e-04	0.02
	Skew	2.5e-04	6.2e-04	2.9e-05	2.3e-04	0.02
	Random	2.1e-04	6.5e-04	2.3e-05	2.0e-04	0.02
	SeqZoomIn	2.3e-04	5.5e-04	2.6e-05	2.1e-04	0.02
	Periodic	2.4e-04	6.6e-04	1.9e-05	2.1e-04	0.02
	ZoomInAlt	2.4e-04	5.4e-04	2.2e-05	2.1e-04	0.02
	ZoomIn	2.3e-04	3.8e-04	3.1e-05	1.4e-04	0.02
Skewed	SeqOver	3.7e-04	7.5e-04	1.6e-05	2.5e-03	0.03
	ZoomOutAlt	3.1e-04	7.6e-04	1.4e-05	2.7e-04	0.03
	Skew	3.5e-04	7.9e-04	1.4e-05	2.5e-03	0.03
	Random	3.4e-04	7.8e-04	1.9e-05	2.5e-03	0.03
	SeqZoomIn	3.6e-04	8.5e-04	1.4e-05	2.5e-03	0.03
	Periodic	3.2e-04	8.2e-04	1.5e-05	2.4e-03	0.03
	ZoomInAlt	3.4e-04	7.5e-04	1.4e-05	2.5e-03	0.02
	ZoomIn	1.9e-05	2.3e-04	1.4e-05	1.4e-03	0.02
Point Query	SeqOver	2.4e-04	7.0e-04	1.5e-03	2.2e-04	0.02
	ZoomOutAlt	1.8e-04	6.3e-04	1.6e-03	2.1e-04	0.02
	Skew	2.6e-04	6.8e-04	1.6e-03	2.3e-04	0.02
	Random	2.2e-04	6.6e-04	1.6e-03	2.5e-04	0.02
	Periodic	2.2e-04	6.8e-04	1.1e-03	2.1e-04	0.02
	ZoomInAlt	2.3e-04	6.8e-04	1.5e-03	3.3e-04	0.02
10 <sup>9</sup>	SeqOver	0.02	0.03	2.8e-04	0.04	2.1
	Skew	8.1e-03	0.03	1.0e-04	0.03	2.1
	Random	0.01	0.03	2.4e-04	0.02	7.0

techniques and develop cost models for all of them that allow automatic tuning of the budget. We show how they perform with both real and synthetic workloads and compare their performance against Adaptive Indexing techniques. Based on

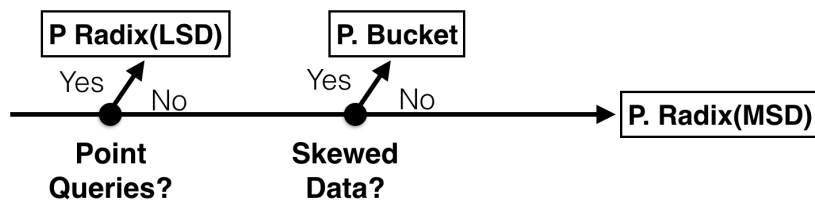


Figure 3-23: Progressive Indexing Decision Tree.

each algorithm's main characteristics and the results of our experimental evaluation, we conclude our work with the decision tree shown in Figure 3-23, which provides recommendations on which technique to use in different situations. In this chapter, we only present an algorithm to index unidimensional columns. However, queries frequently have filters on multiple columns. In the next chapter, we will describe how

to create a Progressive Index that indexes multiple dimensions.