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It's just a phase: high-contrast imaging with patterned liquid-crystal phase plates to facilitate characterization of exoplanets

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Citation

Doelman, D. S. (2021, June 22). *It's just a phase: high-contrast imaging with patterned liquid-crystal phase plates to facilitate characterization of exoplanets*. Retrieved from <https://hdl.handle.net/1887/3191978>

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Cover Page



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Issue Date: 2021-06-22

2 | The vAPP coronagraph: creating dark holes in PSFs all over the world

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Accepted by Applied Optics

Over the last decade, the vector-apodizing phase plate (vAPP) coronagraph has been developed from concept to on-sky application in many high-contrast imaging systems on 8-m class telescopes. The vAPP is an geometric-phase patterned coronagraph that is inherently broadband, and its manufacturing is enabled only by direct-write technology for liquid-crystal patterns. The vAPP generates two coronagraphic PSFs that cancel starlight on opposite sides of the point spread function (PSF) and have opposite circular polarization states. The efficiency, that is the amount of light in these PSFs, depends on the retardance offset from half-wave of the liquid-crystal retarder. Using different liquid-crystal recipes to tune the retardance, different vAPPs operate with high efficiencies ($> 96\%$) in the visible and thermal infrared ($0.55\ \mu\text{m}$ to $5\ \mu\text{m}$). Since 2015, seven vAPPs have been installed in a total of six different instruments, including Magellan/MagAO, Magellan/MagAO-X, Subaru/SCEXAO, and LBT/LMIRcam. Using two integral field spectrographs installed on the latter two instruments, these vAPPs can provide low-resolution spectra ($R\sim 30$) between $1\ \mu\text{m}$ and $5\ \mu\text{m}$. We review the design process, development, commissioning, on-sky performance, and first scientific results of all commissioned vAPPs. We report on the lessons learned and conclude with perspectives for future developments and applications.

2.1 Introduction

Many different coronagraphs have been proposed since the creation of the first solar coronagraph in 1939 by Bernard Lyot (Lyot, 1939). Originally, the existing coronagraph concepts could be organized in a family tree (Mawet et al., 2012). However, this tree was cut down in the Lorentz Center workshop paper (Ruane et al., 2018), because new developments in coronagraph design lead to the merging of various branches. Due to its simplicity, an adapted version of the Lyot coronagraph is still the most used coronagraph for ground-based high-contrast imaging systems. The use of Lyot coronagraphs resulted in many scientific breakthroughs in understanding exoplanets and circumstellar disks. Preliminary results of the two largest exoplanet surveys are presented by Nielsen et al. (2019) (GPIES) and Vigan et al. (2020) (SHINE), and a summary paper on circumstellar disks was presented by Avenhaus et al. (2018).

The Lyot coronagraph and other focal-plane coronagraphs require accurate centering of the star on their focal-plane masks. Pupil-plane coronagraphs do not have this disadvantage, as the coronagraphic PSF does not change significantly with position in the field of view. The Apodizing Phase Plate (APP) coronagraph is a single-optic pupil-plane coronagraph (Codona et al., 2006; Kenworthy et al., 2007). An APP modifies the phase in the pupil plane to create regions in the PSF where the star light is suppressed, so-called dark zones. A pupil-plane coronagraph has some distinct advantages over a focal-plane coronagraph. First, the coronagraph is simple because it consists of only a single optic, making it easy to install in any high-contrast imaging instrument. Second, the coronagraphic performance is insensitive to tip-tilt errors caused by vibrations or residual wavefront from the adaptive optics system. Moreover, tip-tilt insensitivity is good for the near-infrared (3-5 μm) where nodding is required to remove the background. With nodding the PSF moves over a large distance ($\gg \lambda/D$) on the detector and alignment with a focal plane mask afterwards takes time and the final position is not always the same, resulting in PSF differences. For a pupil-plane coronagraph no realignment is required after nodding, increasing the on-axis time. Third, the coronagraph design can easily be adapted to include complex pupil shapes (e.g. segments/spiders). Fourth, all objects have the coronagraphic PSF, enabling high-contrast imaging of binary systems. These advantages contributed to success of the APP, having imaged multiple substellar companions (e.g. β Pictoris b, discovering HD100546 b and HD 984, (Quanz et al., 2010; Quanz et al., 2013; Meshkat et al., 2015)). Disadvantages of pupil-plane coronagraphs are the high intensity of the stellar PSF often resulting in saturation, the lower planet throughput due to the reshaping of the PSF, and the larger inner working angle with respect to the current best focal-plane coronagraphs. More specifically for the APP, the properties of the diamond-turned phase plate limited the exoplanet yield. As the APP applies dynamic (chromatic) phase, the APP performance is only optimal for a single wavelength, and the dark zone contrast is degraded for broadband light. More importantly, the diamond turning requires smooth phase transitions, which limited the APP designs to an outer working angle of $9 \lambda/D$ and restricted dark

zones to a single side of the PSF.

The vector-Apodizing Phase Plate (vAPP) coronagraph is an upgraded version of the APP coronagraph and induces geometric (or Pancharatnam-Berry) phase (Pancharatnam, 1956; Berry, 1987) for circularly polarized light (Snik et al., 2012; Otten et al., 2014a). The vAPP generates two coronagraphic PSFs that have dark zones on opposite sides of the point spread function and have opposite circular polarization states, see Fig. 2.1. The vAPP is a patterned half-wave retarder where the fast-axis orientation changes as a function of position. The induced phase, ϕ , is equal to plus/minus twice the fast-axis orientation θ : $\phi = \pm 2\theta$, with opposite sign for the opposite circular polarization states. Geometric phase is by definition achromatic, and the efficiency, the percentage of light that acquires this phase, depends on the retardance offset from half-wave. The broadband performance of the vAPP is therefore determined by the retardance as a function of wavelength. The vAPP is manufactured with liquid-crystal technology. A direct-write system is used to print the desired fast-axis orientation pattern in a liquid-crystal photo-alignment layer that has been deposited on a substrate (Miskiewicz & Escuti, 2014). The induced orientation depends on the linear polarization of the incoming light of the direct-write system. Multiple layers of self-aligning birefringent liquid-crystals are deposited on top with varying thickness and twist, carefully designed to generate the required half-wave retardance (Komanduri et al., 2012, 2013). The stack is referred to as a multi-layered twisted retarder (MTR). By tuning the twist and thickness of layers in the MTR, very high efficiencies ($> 96\%$) can be achieved for large wavelength ranges, e.g. $2 - 5\mu\text{m}$ (Otten et al., 2014a).

As opposite circular polarization states create a PSF with a dark hole on opposite sides, the vAPP implements circular polarization splitting to separate two complementary dark holes. The relative intensity of the two coronagraphic PSFs depends on the circular polarization state of the incoming light. A vAPP for broadband imaging is obtained in combination with a polarizing beamsplitter (e.g. a Wollaston prism) and a quarter-wave plate, but the non-coronagraphic PSFs corresponding to various polarization leakage terms degrade the contrast in the dark holes (Snik et al., 2012; Otten et al., 2014a; Bos et al., 2018). The polarization leakage can be separated from the coronagraphic PSFs by adding a grating pattern (= phase tilt) to the phase pattern, i.e. the “grating-vAPP” (gvAPP) (Otten et al., 2014b). The gvAPP has the same advantages as all pupil-plane coronagraphs, and also overcomes two limitations of the vAPP. First, no polarization splitting or filtering optics are required due to the grating. Second, the gvAPP has two dark holes on opposite side, increasing the search space by a factor two. This comes at the cost of a factor of two in exoplanet throughput, with half of the light being imaged at the bright side of one of the two coronagraphic PSFs. We note that for unknown companions this factor is the same when using an APP, having to rotate the APP to image both sides. Advantages of the two vAPP dark holes are that they have the same AO performance, such that one PSF can be used as a reference for post processing (Otten et al., 2017), and that the antisymmetric PSF is beneficiary for wavefront sensing (Bos et al., 2019). Moreover, the direct-write system is capable of writing much finer structures ($\sim 1\mu\text{m}$) compared to diamond

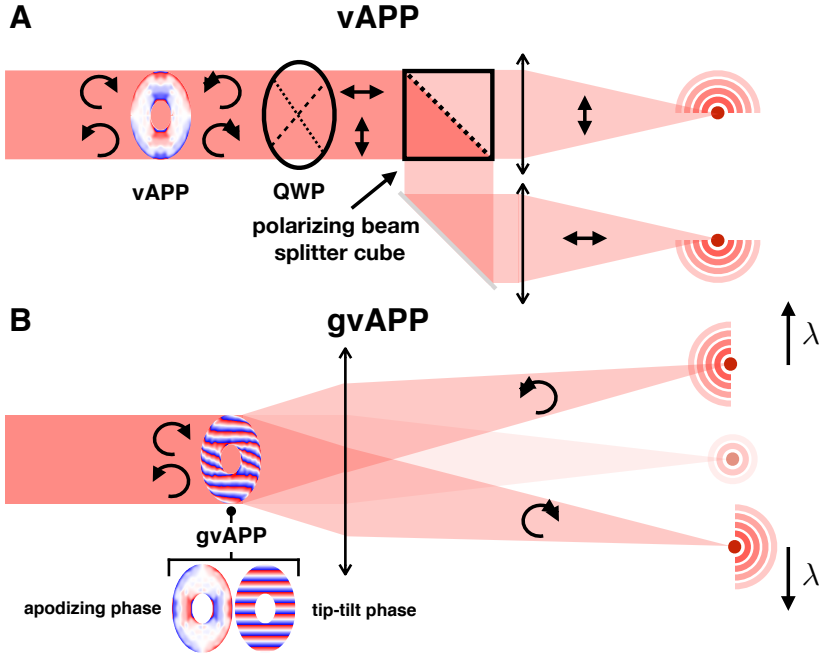


Figure 2.1: Schematic of two different vAPP implementations. *Top:* The vAPP, where PSFs with dark zones on opposite sides and opposite polarization states are separated using a quarter-wave plate and a polarizing beam-splitter. *Bottom:* The gvAPP where polarization states are separated by adding a phase ramp (= polarization grating) to the vAPP phase pattern, which generates opposite tilt for light with left- and right-circular polarization, adapted from (Bos et al., 2018).

turning ($\sim 50\mu\text{m}$) and has the ability to write discontinuous phase steps. These properties enable a tremendously increased phase pattern complexity that can be used for holography (Haffert et al., 2018) and manufacture more optimal phase patterns (Doelman et al., 2020).

A third kind of vAPP is the double-grating vAPP (dgvAPP). The dgvAPP combines a gvAPP with a second polarization grating on a separate substrate (Doelman et al., 2020). This second grating is identical to the gvAPP grating and has the opposite effect, diffracting both the main beams back on axis. Polarization leakage of the liquid-crystal film on the first substrate is diffracted outside the dark zone by the second grating, reducing the total on-axis polarization leakage by multiple orders of magnitude. Because both beams are recombined, the phase pattern needs to produce a 360° dark zone, which requires more extreme patterns, increases the inner boundary of the dark zone, and generally reduces the PSF-core throughput. However, the planet light is also recombined in the dark zone, so the throughput is a factor 2 higher.

A common property is that all vAPP implementations is that they operate over 100% bandwidth with extremely high efficiency ($> 96\%$).

2.2 Design of a gvAPP

The design of a gvAPP starts with the optimization of an APP phase pattern. The goal of the optimization is to null the stellar PSF in the dark zone to a very high degree with respect to the PSF core, e.g 10^{-5} . We define the contrast as this ratio of flux in the dark zone divided by the flux in the PSF core and it depends on the focal plane coordinates, see Fig. 2.2. Light has to be diffracted from the stellar PSF core to null the dark zone, reducing the intrinsic Strehl ratio of the star. We define the Strehl ratio as the summed flux of the non-coronagraphic stellar PSF core in an aperture divided by the summed flux of energy in the coronagraphic stellar PSF core using the same aperture. In simulation without noise this aperture has a diameter of one pixel, and for all other applications it is common to use a diameter of $\sim 1.4\lambda/D$ (Ruane et al., 2018). Destructively interfering the star light in the dark zone results in constructive interference of the light on the opposite side of the PSF. A reduction of the stellar Strehl ratio is unwanted, as the Strehl ratio of the companion PSF is affected in the same way. Therefore, the optimization simultaneously maximizes the Strehl ratio of the stellar PSF, while minimizing the flux inside the dark zone. This optimization problem is highly non-linear in the complex phase exponential. Consequently, first attempts at calculating APP patterns did not aim to find the optimal solution, their aim was to find solutions that are close. These attempts used phase iteration techniques (Codona & Angel, 2004; Codona et al., 2006) or a modified Gerchberg-Saxton (GS) algorithm (Kostinski & Yang, 2005) and were moderately successful. They have shown that these methods can produce a dark zone of any shape with extreme contrasts ($< 10^{-10}$) (Keller, 2016), yet their Strehl ratios are low for small inner working angles. Another set of solutions were generated by adapting

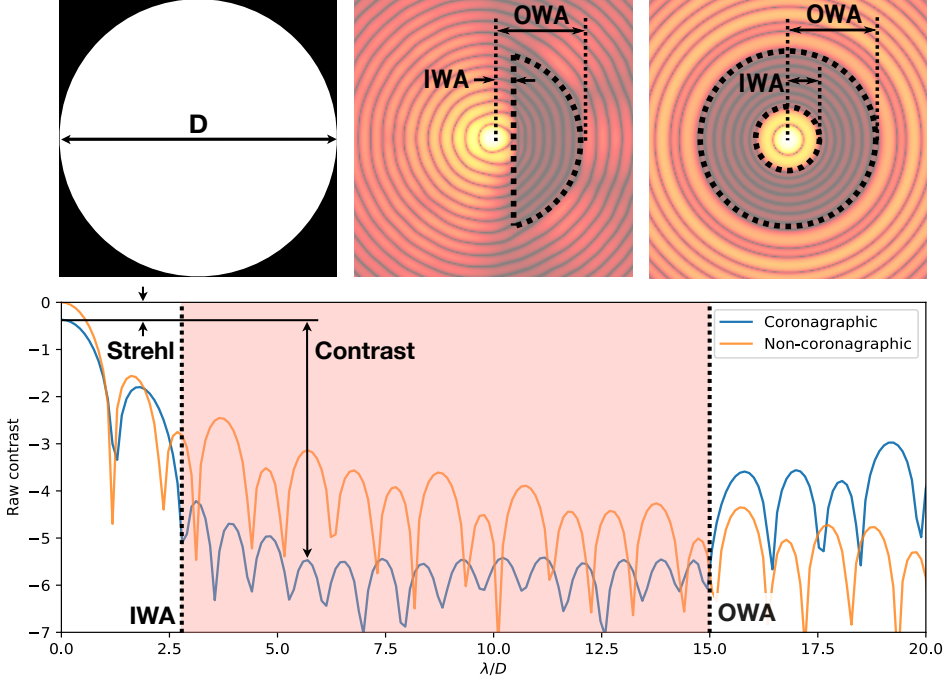


Figure 2.2: Definitions of the dark zone properties. *Top left*: The pupil of the telescope. *Top middle*: A D-shaped dark zone ($\log_{10}$ scale). *Top right*: An annular dark zone ($\log_{10}$ scale). *Bottom*: PSF slice of a non-coronagraphic and coronagraphic design (annular). Adapted from Por (2017).

the global optimization algorithms for shaped-pupil coronagraphs to include phase (Carlotti, 2013). This algorithm produces APPs with regions containing several discrete phases and sharp transitions in between these regions. This algorithm was improved to yield *globally* optimal solutions with unity amplitude across the pupil, smooth phase patterns for 180° and D-shaped dark zones, and $0-\pi$ solutions for 360° dark zones (Por, 2017). As this last algorithm allows both phase and amplitude modulation in the pupil, this proves empirically that APPs are the globally optimal solutions for pupil-plane coronagraphs.

2.2.1 Dark zone considerations

The globally optimal solutions are critical to ensure a high exoplanet yield. However, it is not the full story. As shown in (Por, 2017), there is a trade-off between inner working angle (IWA), outer working angle (OWA), contrast, and Strehl. The definitions of the four properties can be found in Fig. 2.2. For focal-plane coronagraphs, the IWA is defined as the smallest angular separation at which the total energy throughput of an off-axis source reaches 50% of the maximum through-

put (Ruane et al., 2018). For pupil-plane coronagraphs this can be adapted to the smallest angular separation where the planet throughput reaches 50% of the maximum throughput in the region where the contrast reaches the target contrast. Equivalently, the OWA is defined as the largest angular separation where the planet throughput still reaches 50% of the maximum throughput in the region where the contrast reaches the target contrast. A good choice of these parameters can be different for every planetary system, observing conditions, wavelength, telescope design and instrument performance. This becomes clear by using a metric that defines a planet detection given instrument limits. In Ruane et al. (2018), the integration time Δt that is required for a 1σ detection is given by

$$\Delta t \propto \left[\frac{\eta_s + \sum_n a_n}{\eta_p^2 - b^2/\epsilon^2} \right], \quad (2.1)$$

where η_s fraction of available star light detected at the planet location, η_p fraction of available planet light detected, and ϵ is the planet-to-star flux ratio. The factor a_n represents noise factors like the background or detector noise such that $\sigma_n^2 = a_n N_\star$, with $N_\star$ the total signal from star in photo-electrons. In the same way $\sigma_{\text{speck}} = b N_\star$, which represents the speckle noise. In this framework, η_p is directly proportional to the vAPP Strehl and the contrast is given by η_s/η_p . We do not minimize Δt with vAPP optimization due to several complicating factors. However, we can use this equation to explore the impact of design choices. Here we outline some of the considerations when choosing these parameters.

1. *Strehl*: The Strehl ratio of a vAPP design impacts the planet throughput for the full field of view. In the case of the photon noise limit, Eq. 2.1 becomes $\Delta t = \eta_s/\eta_p^2$, demonstrating that Strehl greatly impacts the integration time that results in a 1σ detection. The gvAPP already has the disadvantage of reducing the planet throughput by a factor of 2, so keeping the Strehl high is crucial for good performance. The definition of a high Strehl is somewhat arbitrary given the impact of the shape of the telescope pupil, AO performance and presence of other noise sources. Therefore, we use the Strehl mostly for a trade-off between the other dark zone properties.

2. *Contrast*: For ground-based high-contrast imaging systems, the intrinsic contrast of a coronagraph is almost never reached. AO residuals and non-common path errors result in quasi-static speckles that limit the performance. In addition, atmospheric jet streams create a wind-driven halo, as the temporal lag between the application of the wavefront correction and the evolving turbulence (Cantalloube, F. et al., 2020). Designing a gvAPP with an intrinsic contrast much lower than the expected raw contrast does not yield the optimal performance. This is clear from Eq. 2.1, where planet is not detected in the presence of speckle noise if $\eta_p < b/\epsilon$ (negative integration time), independent of η_s . Yet, removing bright PSF structures by creating a dark zone reduces speckle pinning, i.e. speckles that are spatially confined to secondary maxima in the diffraction limited PSF (Bloemhof et al., 2001). Taking into account speckle pinning, it can be argued that a design contrast lower than the expected AO-limited contrast does result in an improved performance, although that has not been studied in detail. For inner working

angles $> 2.0\lambda/D$ and a central obscuration lower than 30%, a design contrast of 10^{-4} results in Strehl ratios higher than 70% (Por, 2017). This design contrast is already significantly lower than the raw contrast of extreme AO systems. Another consideration is that constant contrast in the dark zone will yield the highest Strehl, although the changes in Strehl are minor for lower contrasts further out. These considerations lead to the conclusion that a more optimal gvAPP design has a contrast that decreases gradually with the estimated AO residuals and becomes constant at a point where other noise factors take over, such as detector noise or background noise ($\sim 10^{-6}$). An example of such a design contrast is shown in Fig. 2.2. In this case, the vAPP design contrast can be determined by AO simulations and verified with end-to-end simulations of the performance.

3. *IWA*: All indirect detection methods for exoplanets (e.g. transit, radial-velocity, astrometry), show that there is a huge fraction of planets that is currently out of reach for direct imaging. While these methods are biased to find these close-in planets, it shows that a small IWA is a critical to find new worlds with direct imaging. However, the Strehl ratio is also very dependent on the IWA. For 10^{-6} contrast, an OWA of $8\lambda/D$, and a central obscuration of 10% changing the IWA from 2.05 to 1.75 λ/D reduces the Strehl from 60% to 20% (Por, 2017). Furthermore, the gain of a smaller inner working angle is usually limited. Uncorrected low-order aberrations, both atmospheric or non-common path, reduce the performance at the smallest separations for ground-based telescopes.

4. *OWA*: The outer working angle has limited impact on the Strehl of APP designs, while the dark zone area increases with the OWA squared. The non-coronagraphic PSF contains only a small fraction of the energy outside of $10\lambda/D$, so increasing the contrast in this region results in a small decrease in Strehl as well. In these regions the SNR of the exoplanets is not dominated by the contrast, however. Further out, techniques like ADI are more effective in removing speckles, the wind-driven halo and PSF structures. Thermal background in the near- and mid-infrared ($\lambda > 2\mu\text{m}$) or detector noise start to dominate the SNR. It is therefore unnecessary for most applications to create a gvAPP with a $OWA > 20\lambda/D$. There is no general design that works for any telescope or wavelength range. All gvAPP designs are different because the optimal phase pattern depends on the telescope aperture and properties like the AO performance and background noise. It is therefore advisable to perform a grid search to find the trade-offs between IWA, OWA, contrast at the IWA and the slope of the contrast as function of radius. An example grid could be the IWA between 1.8 and 2.3 λ/D in steps of 0.1, the OWA between 12 and 20 λ/D in steps of 1, the $\log(\text{contrast})$ between $10^{-3.5}$ and 10^{-5} in steps of 0.5, and a slope between 0.25 and 0.5 $\log(\text{contrast})$ per λ/D in steps of 0.05.

Another consideration is the dark zone shape itself. A gvAPP with D-shaped dark zones provides phase solutions with higher Strehl ratios compared to 180 degree dark zones with identical inner working angles. This difference in Strehl increases for smaller inner working angles ($< 2.5\lambda/D$), which is why the D-shape is used in most gvAPPs. The impact of the D-shape on observing is discussed in section 2.3.1. An interesting trade-off exists for planet detection at larger IWAs

($> 3\lambda/D$). Beyond this IWA threshold, the designs with an annular dark zone will have a Strehl ratio that can be competitive with D-shaped dark zones. While the Strehl ratio of designs with annular dark zones are still significantly lower, dgvAPPs with annular dark zones have twice the planet throughput compared to a gvAPP. The origin of this factor two is that half of the planet light is imaged on the bright side of the coronagraphic PSF for a gvAPP. The trade-off between D-shaped and annular dark zones is highly dependent on the telescope pupil, as a central obscuration size and spider thickness greatly impact the Strehl of annular dark zone designs. We note that comparing Strehl ratios with a factor two correction factor for planet throughput and the same contrast levels does not necessarily select the best of the two. There are other factors that are more difficult to add to this trade-off. For example, a dgvAPP will not have wavelength smearing due to grating diffraction, companions will be inside the dark zone for all parallactic angles, post-processing is different, and a gvAPP requires a larger field of view. Because factors like these are difficult to quantify, we did not attempt a general trade-off study. So far, only one dgvAPP has been installed on the large binocular telescope (LBT). The pupil of the LBT is favourable with a central obscuration ratio of $\sim 11\%$ and thin spiders that were not included in the design. Moreover, a vAPP with an annular dark zone was installed on the William Herschel Telescope (WHT), which was designed for an off-axis 1-m pupil without central obscuration and spiders.

2.2.2 Optimization of the APP design

The optimization of the APP starts with a pupil definition. Existing HCI instruments usually have a pupil camera where the pupil can be measured or have their own mask to define the pupil. Extreme caution is warranted when defining the pupil, as the maxima and minima of the phase pattern will be located near the pupil edges. An error in pupil definition leads to a stark reduction in vAPP performance. For this reason we define an APP pupil, which is the undersized version of the true pupil to accommodate alignment errors, definition errors, and pupil movement. Drastic undersizing increases the IWA, negatively impacts Strehl with thicker spiders and a larger central obscuration ratio, and reduces throughput by removing effective telescope area. Therefore, this balance results in an undersizing of the instrument pupil by 2-5%, depending on the amplitude of the expected pupil movement and the alignment tolerances, and in coordination with the instrument team. In addition, it can be beneficial to change the orientation of the dark zones depending on the pupil shape. Spiders add narrow diffraction structures that locally enhance the PSF intensity. A D-shaped dark zone can, depending on the orientation with respect to the pupil, overlap with one or more spider diffraction structures. Removing these structures leads to a decrease in Strehl, so if there is freedom to choose the dark zone orientation the straight edge should be oriented parallel to two spiders. Residual atmospheric dispersion, detector ghosting effects, the FOV of an IFS or the orientation of a slit or image slicer can limit this design freedom.

For a given set of APP parameters and a pupil definition, we use the optimization solver, Gurobi Optimizer (Gurobi Optimization, 2020), to calculate the optimal solution. Computer memory and run time limitations limit the APP phase pattern to 100×100 pixels and a dark zone up to $14 \lambda/D$. For N pixels in the pupil plane, the optimization problem scales as N^2 in computer memory and $N^{3.5}$ in run time. These scaling laws also hold true for pixels in the focal plane for the OWA. Hence, it is not possible to calculate the APP design at the full resolution that is used in the direct-write system, which is on the order of a 1000×1000 pixels. We therefore adopt a two-stage approach for finding the vAPP phase pattern. First we find the optimal APP phase pattern for a downsampled version of the APP pupil. If necessary we decrease the OWA to the $14 \lambda/D$ limit set by the computer memory. This downsampled version also does not contain additional dark zones for the coronagraphic PSF with opposite circular polarization or dark zones that minimize crosstalk with the leakage term or additional holograms. In section 2.2.3 the use of these additional dark zones and holograms is explained. Secondly, we upscale this low-resolution APP phase pattern design with Fourier upsampling (Soummer et al., 2007) and use this solution as a prior for the second stage. This second stage adds all dark zones and corrects any errors made during the upsampling of the low-resolution phase pattern. We use a modified Gerchberg-Saxton (GS) algorithm (Gerchberg, 1972) for this stage. This algorithm does not guarantee an optimal solution like the global optimizer does. However, with the starting point already quite close the optimal solution, the GS algorithm is likely to converge before unacceptable Strehl losses occur.

An example for resulting phase patterns after the first and second stage are shown in Fig. 2.3. In practice, we find that limiting the design contrast during the first stage of optimization often increases the Strehl of the final design. Typically, for a final design contrast $< 10^{-4}$ the design contrast during the first stage should be between 10^{-2} and $10^{-3.5}$ to recover a new solution with the highest Strehl. Both optimization stages are implemented in HCIPy (Por et al., 2018) and an example of vAPP optimization using only GS can be found in its documentation¹.

2.2.3 Adding functionality with holograms

Enabled only by the accurate and high-resolution of the direct-write process and the liquid-crystal properties, it is possible to add capabilities to all types of vAPPs. Here we will discuss two capabilities, focal-plane wavefront sensing (FPWFS) and reference spots for astrometry and photometry. Both capabilities have solutions based on holograms. We define holograms as PSF copies imaged off-axis, which can be biased with a wavefront aberration. In essence, the vAPP PSFs are also holograms. Combining multiple holograms into a single phase screen is possible through multiplexing wavefronts into a single phase screen, as described in (Dong et al., 2012; Wilby et al., 2017; Doelman et al., 2018). A multiplexed phase screen directs light to multiple holograms, each with a different PSF. These holograms can be added anywhere in the focal plane up to the Nyquist limit, with any bias, and

¹<https://docs.hcipy.org>

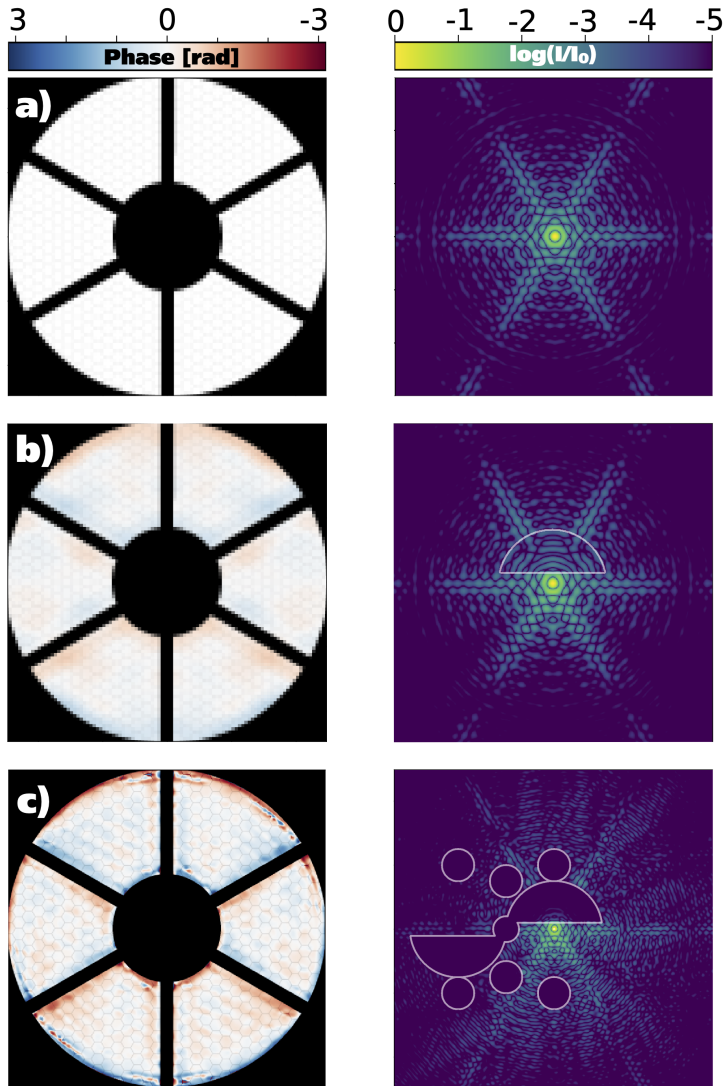


Figure 2.3: Optimization of an APP pattern, showing the phase pattern (left) and corresponding PSF (right). **a)** The low-resolution input pupil for the global optimizer and the corresponding PSF. **b)** Output of the global optimizer for a lower contrast (10^{-3}) and a smaller dark zone, indicated by the white lines. **c)** High-resolution APP design created using the Gerchberg-Saxton algorithm on the Fourier-scaled global optimal APP design. Additional dark zones have been added for the opposite coronagraphic PSF, the leakage PSF and additional holograms.

with any amplitude mixing ratio. Due to circular-polarization splitting, adding a holographic copy at a certain position in the focal plane will necessarily also add a hologram with opposite bias at the location mirrored in the optical axis. These properties of holograms make them very diverse and easily adapted for FPWFS and reference spots. A natural extension is to generate multiple coronagraphic PSFs per polarization state. For example, it is possible to position two coronagraphic PSFs for one polarization such that they precisely overlap with the two coronagraphic PSFs of the opposite polarization state. The advantage is that the otherwise polarized coronagraphic PSFs now become unpolarized (Bos et al., 2020). This has benefits for including polarimetry and/or focal-plane wavefront sensing with the vAPP. One important downside is that multiplexing many holograms results in significant crosstalk. Crosstalk adds PSFs at locations that are the vector-addition of the individual gratings and multiples thereof.

Photometric and astrometric reference spots

For accurate photometry of a companion the vAPP already has an advantage compared to focal-plane coronagraphs. The coronagraphic PSFs themselves provide a photometric reference, given that the two PSFs are not saturated. Otherwise the leakage PSF can serve as photometric reference if it is not too affected by speckles. However, it does have a different spectrum due to the wavelength dependence of the diffraction efficiency. A solution is an unbiased reference spot, which is a copy of the non-coronagraphic PSF. Multiplexing unbiased wavefronts with the vAPP results in reference PSFs that can be used both for photometry and astrometry. For other coronagraphs, such spots have been generated using the deformable mirror or static phase screen. A full summary of these efforts can be found in Bos (2020) and references therein. Moreover, the vector speckle grid that is proposed in Bos (2020) produces speckles that are effectively incoherent with the underlying halo, which greatly improve the photometric and astrometric accuracy. By multiplexing the vAPP with two holograms with opposite phase modulation on the opposite polarization states, this vector speckle grid is easily implemented in the vAPP coronagraph. Astrometry with a vector speckle grid could provide astrometric solutions with a precision of $< 0.01\lambda/D$ (Bos, 2020), however this has not yet been tested on-sky.

Focal-plane wavefront sensing

Adding a bias wavefront to holograms changes their sensitivity to the incoming wavefront. Holographic modal focal-plane wavefront sensing is possible because of these variations (Keller, 2016). FPWFS is critical to remove non-common path aberrations (NCPA), aberrations from optics after the AO system, which are therefore unseen by the AO wavefront sensor. An example of a focal-plane wavefront sensor is the coronagraphic modal wavefront sensor (cMWS) (Wilby et al., 2017; Haffert et al., 2018), which provides simultaneous coronagraphic imaging and focal-plane wavefront sensing with the science point-spread function. The cMWS creates

multiple holograms, each biased with a different wavefront mode drawn from a suitable basis set. The normalized difference between the PSF copies with opposite circular-polarization state responds linearly to the corresponding aberration mode present in the input wavefront. The main advantage of this wavefront sensor is that the monitoring the Strehl ratios of the holograms and the wavefront reconstruction are straightforward and can be done at high speeds and with the actual science camera, independent from the dark hole(s). Moreover, no modulation of the wavefront is required. Multiplexing holograms removes light from the coronagraphic PSF, and for efficient wavefront sensing each mode takes away $\sim 1\%$ of Strehl, on top of the already lower vAPP Strehl. The trade-off between modal coverage, sensitivity and Strehl is difficult to optimize, as it is a priori unclear how much the selected wavefront modes contribute to speckles. The cMWS has successfully been tested with the Leiden exoplanet instrument (LEXI) (Haffert et al., 2018), and in lab demonstrations of Magellan/MagAO-X (Miller et al., 2019). Another method for FPWFS is an adaptation of phase diversity (PD) (Gonsalves, 1982). Where classical PD requires an in-focus and out-of-focus image, phase diversity holograms are biased with defocus of opposite amplitude, similar to the cMWS with a larger bias. This larger bias results in an increase in modes that can be reconstructed, while decreasing the average intensity of the hologram. So compared to the cMWS, a larger fraction of the incoming light is diffracted to the PD holograms, e.g. 10% instead of 1%. This FPWFS method was implemented in the Subaru/SCExAO (Doelman et al., 2017), Magellan/MagAO-X (Miller, 2018) and HiCIBaS instruments. A different implementation of PD is described in Por & Keller (2016), directly reconstructing the focal-plane electric field in the dark zone. Coronagraphic PSF copies are created with each a unique probe in the dark zone, making use of the pairwise nature of the holograms (Keller, 2016). The unaltered science PSF is still available, providing the same advantages as the cMWS, but adding the capability to sense all modes corresponding to the dark zone. Interestingly, the coronagraphic PSFs themselves can also be designed to encode wavefront information in the bright field by including a pupil-plane amplitude asymmetry. The added advantage of the vAPP is that there are two coronagraphic PSFs, with opposite bright fields that cover all of the spatial frequencies. This reduces the number of modes that can otherwise not be measured by one coronagraphic PSF (Sun, 2019). We refer to such vAPP designs as Asymmetric Pupil vAPPs (APvAPPs), and was successfully implemented by Bos et al. (2019). They show that if the pupil is asymmetric, both odd and even modes can be recovered from the coronagraphic PSFs only. Earlier versions of an asymmetric pupil wavefront sensor (Martinache, 2013) could not be combined with a coronagraph. A non-linear model-based wavefront sensing algorithm was proposed by (Bos et al., 2019) and is limited, due to computational considerations, to the first ~ 100 Zernike modes, yet it showed nearly an order of magnitude improvement in contrast between 2 and $4 \lambda/D$ with the internal source, and on-sky the gain was a factor of 2. Spatial linear dark field control (LDfC) (Miller et al., 2017, 2019) is also a very powerful combination with the APvAPP. LDfC empirically derives a linear relationship between DM actuation and focal-plane intensity re-

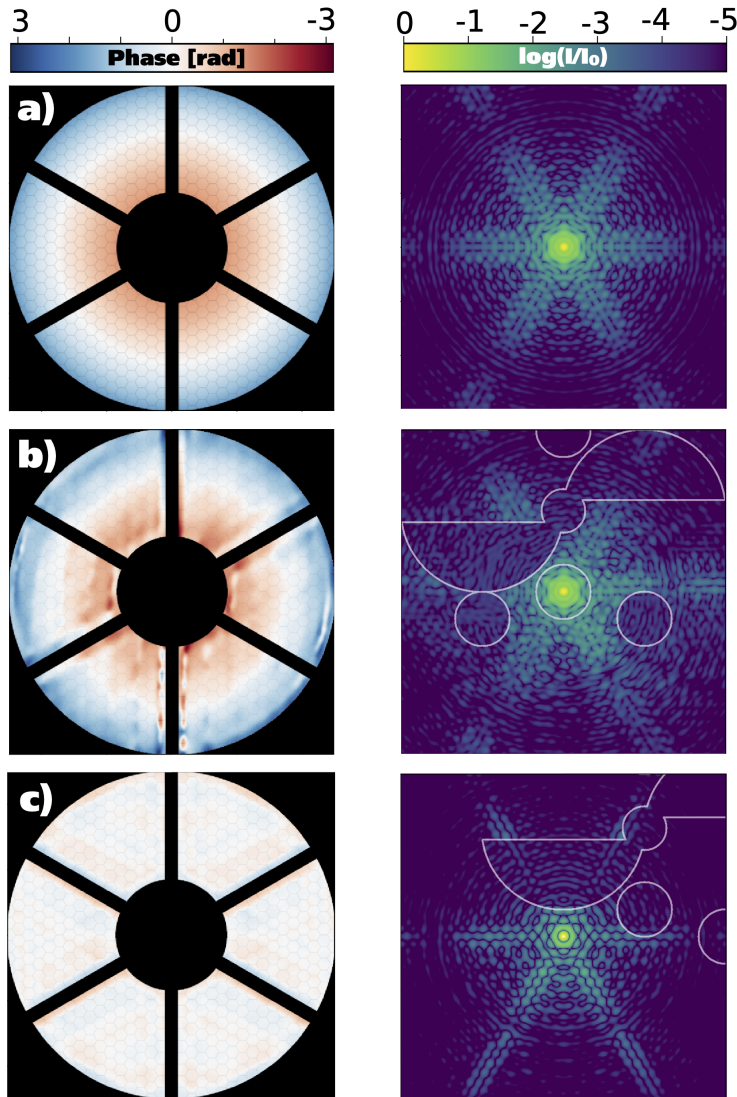


Figure 2.4: Updates of the holographic phase patterns to minimize crosstalk and light scattering into the dark zones. **a)** An unaltered phase diversity hologram with a defocus of 0.87 radian RMS. **b)** The updated PD hologram with suppressed diffraction structures in all dark zones, calculated using the Gerchberg-Saxton (GS) algorithm. **c)** Same as b), only without defocus to create a photometric or astrometric reference hologram. Each hologram has displaced dark zones. This displacement corresponds to the relative location of the hologram with respect to the dark zones of the coronagraphic PSF after multiplexing the phase patterns.

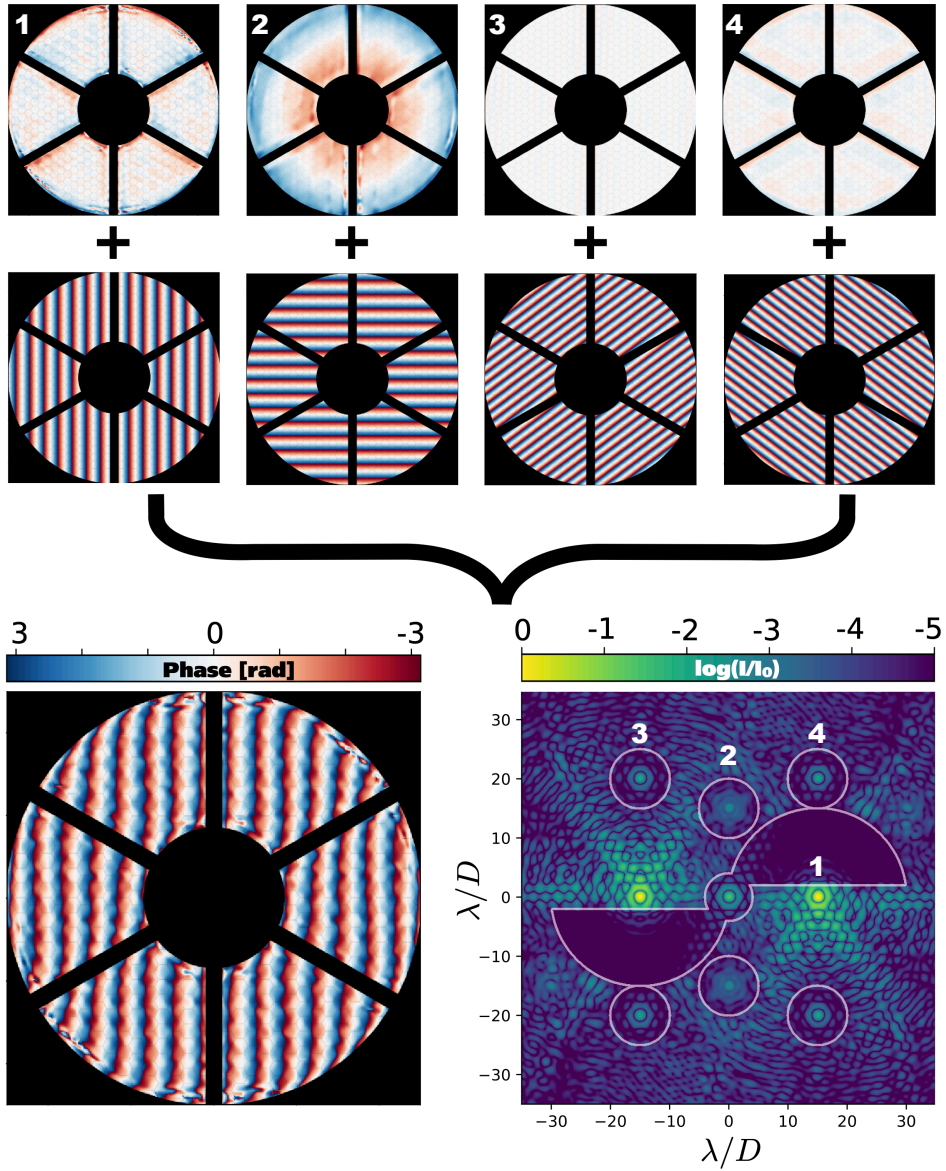


Figure 2.5: Creation of a gvAPP phase pattern by multiplexing the APP design (1) with the three holograms. Hologram 2 is defocused and could be used for focal-plane wavefront sensing. Hologram 3 and 4 are unaberrated and are located in a square grid at the grating frequency for astrometric referencing. Additional iterations with GS have cleared the dark zone of second order effects caused by multiplexing. The PSF is calculated assuming unpolarized light and a polarization leakage of 1%.

sponse in the bright field, allowing it to control a larger number of modes. As LDFC can only drive back the wavefront to a reference state, it requires an initial calibration by non-linear model-based wavefront sensing algorithm, making both methods complimentary. LDFC uses the linear response to wavefront aberrations in the bright side of the vAPP PSF to reconstruct the wavefront. For Magellan/MagAO-X, simulations have shown that LDFC is capable of correcting the full dark zone using 400 modes (Miller et al., 2019). Recently, LDFC in combination with an APvAPP was installed and tested using Subaru/SCEXAO (Miller et al., 2020). An on-sky demonstration followed soon after (Bos et al., Submitted for publication). By multiplexing two coronagraphic PSFs per polarization state, each of these PSFs designed with a different pupil-plane amplitude asymmetry, it is also possible to design APvAPPs that can measure both pupil-plane phase and amplitude modes simultaneously (Bos et al., 2020). The possibility of adding photometric, astrometric, and wavefront sensing capabilities to the vAPP make it a unique and diverse coronagraph. Exploring these techniques for a more integrated approach to building high-contrast imaging systems shall lead to a better performance at the systems level.

Implementation into vAPP designs

Adding holograms by multiplexing phase patterns does not result in an optimal combination. Crosstalk between modes and the vAPP PSF will decrease the contrast in the vAPP coronagraphic dark zones. Moreover, the crosstalk will change the response of the holograms. Minimizing this crosstalk is implemented by changing the vAPP PSF, the modes and optimizing after multiplexing. First, the coronagraphic PSF can be suppressed at the locations of the holograms, such that interference is minimized. Additional dark zones can be added during the upscaling of the APP design. Second, the modes can be adapted to also have a reduced intensity at the location of the APP dark zone. These dark zones can be added using the GS algorithm, as is shown in Fig. 2.4. All modified holograms, including the coronagraphic vAPP hologram, can then be combined by multiplexing. Third, the crosstalk in the vAPP dark zones caused by the multiplexing can be removed by applying an additional round of GS. The combined result is shown in Fig. 2.5. Every time GS is applied, it has a minor impact on the Strehl of the coronagraphic PSF. The final cleaning of the dark zone could impact the performance of holographic wavefront sensors, though we estimate that this effect is minimal, as no significant deviation from expected performance was found in (Miller et al., 2019)

2.2.4 Additional design choices

So far we have focused on the design of the vAPP phase pattern. However, there are additional choices regarding the vAPP optic that are independent of the phase pattern. We will highlight two design choices that impact the manufacturing complexity and the wavelength dependent performance of the vAPP.

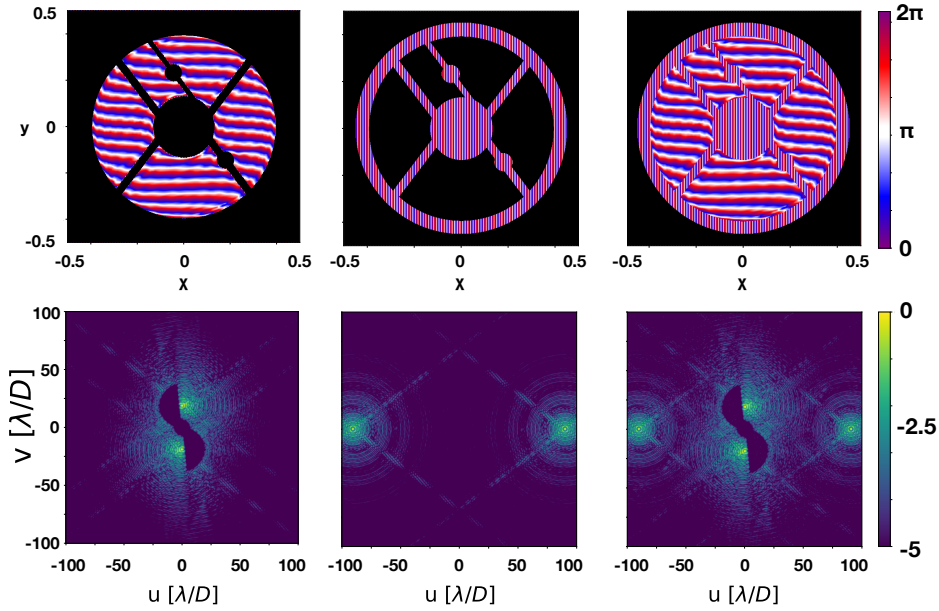


Figure 2.6: *Top left:* Phase of a grating-vAPP for an undersized pupil of the Subaru Telescope. An amplitude mask for the pupil is shown in black. *Bottom left:* Logarithmic plot of the PSF of the grating-vAPP, showing two coronagraphic PSFs for opposite handedness of circularly polarized light. The grating-vAPP was simulated to be a perfect half-wave retarder, so no leakage is present. *Center:* The grating mask (top) and resulting PSF (bottom) that will be used as an amplitude mask. The grating has 90 periods across the diameter of the pupil. *Right:* The phase and PSF of the grating-vAPP combined with the grating mask. The incoming light has a pupil of radius 0.45 (black) and the light is separated in a grating mask component and a grating-vAPP component. A small misalignment of the pupil does not affect the coronagraphic PSF, relaxing alignment tolerances. Adapted from Doelman et al. (2017).

The grating mask

As discussed in section 2.2.2, the pupil definition is critical for the performance of the vAPP. During manufacturing it is therefore standard to add a physical binary amplitude mask to the assembly that is aligned with sub-micron accuracy with the phase pattern. These amplitude masks and their alignment add significant complexity and cost to the vAPP optic. Especially for lab demonstration projects that often require multiple phase patterns, it is not cost effective to use these amplitude masks. Separate metal laser-cut masks can provide a cheap solution at the cost of reduced alignment accuracy. We note that it is not necessary to absorb or reflect the light at the pupil plane. A different solution is to diffract the light outside of the field of view of the coronagraphic PSFs. Diffracting the light that is not falling onto the coronagraphic phase pattern to outside the FOV requires a patterned high-frequency polarization grating outside of the pupil, e.g. beyond the outer diameter, inside the spiders, and within the central obscuration. This grating should have a different orientation and frequency than the grating of the gvAPP. A simple spatial filter in an intermediate focal plane can remove the light outside the pupil. We call this concept the “grating mask”. This concept is described in detail in Doelman et al. (2017), and a reworded version is added here for clarity. An example of the gvAPP with a grating mask is shown in Fig. 2.6. Critical for the workings of a PG as amplitude mask is that the tilt is applied *locally*, as the phase is accumulated inside the liquid-crystal layer (Escuti et al., 2016). This is unlike a regular grating where the interference between the *full* grating results in the diffraction orders. Adding a mask only outside the pupil does not significantly alter the coronagraphic PSF. It does, however, change the leakage term from the PSF of the undersized vAPP pupil to the PSF of the telescope or instrument pupil.

How the grating mask reduces the complexity of the vAPP optic can be seen in Fig. 2.7. With a grating mask the first substrate is no longer necessary, removing a glue layer as well. Moreover, the lab demo vAPPs can be manufactured without any additional substrates. While their phase patterns and pupils can be extremely complex, only homogeneous illumination is necessary for them to work as expected. We note that an end cap would make them more durable and less easy to damage. For lab testing a 1 cm grating mask was produced with 8 pixels of 8.75 micron per period. The pupil is a simplified version of the Nancy Grace Roman Space Telescope and was chosen for the thin spiders and complex pupil design. The full mask between crossed polarizers is shown on the left in Fig. 2.8 in addition to a microscopic image which shows a spider with the grating pattern. The width of the spider is a few times the grating period, yet this does not affect the performance of the grating mask. The right panel of Fig. 2.8 shows the reimaged pupil when a field stop is added to the focal plane. The light outside the simplified RST pupil, which is diffracted by the grating, is blocked and does not appear in the reimaged pupil.

When applied in a real high-contrast imaging system, two things need to be considered. First, one has to be careful where the diffracted light from outside the

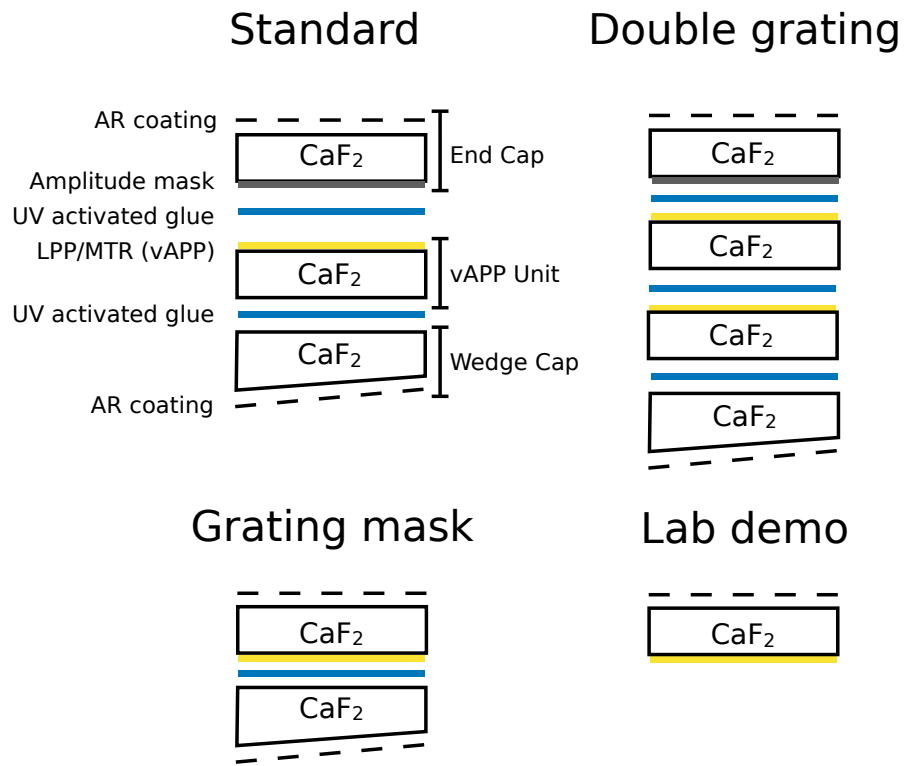


Figure 2.7: Various substrate designs for vAPP manufacturing.

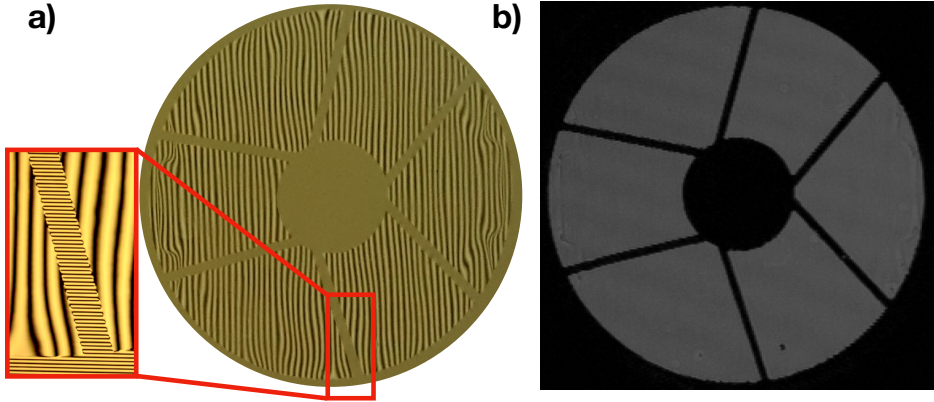


Figure 2.8: **a)** Photograph of the vAPP with a simplified RST pupil between crossed polarizers, manufactured for testing the grating mask. The zoomed in microscope image shows the high-frequency grating used for the grating mask that is not captured by the normal camera. **b)** Reimaged pupil with a field stop inserted in the focal plane. The field stop removes the diffracted light from outside the pupil defined by the grating mask. Even spiders with a width of a few times the grating period are removed extremely well.

pupil is directed to. The diffracted light can scatter back onto the detector by reflections inside the instrument if not blocked. Because the direction of the PG is a free design parameter, the reflections can be directed to non-reflective parts with prior knowledge of the instrument layout. Second, a few percent of the light that would be normally blocked by an amplitude mask would end up on the science camera due to polarization leakage. This polarization leakage is always non-zero for a deviation in retardance from half-wave. The influence of the polarization leakage will be small when the coronagraphic PSFs have enough spatial separation from the leakage. This separation is also a free parameter and is set by the frequency of the grating of the coronagraphic phase pattern. In addition, the pupil defined by the grating mask will be undersized a few % compared to the telescope pupil, so the amount of light that is diffracted by the grating mask is limited. Overall, the grating mask is a cheap alternative for amplitude masks and alleviates the problems that come with aligning an amplitude mask with the phase pattern.

Wavelength selective multi-twist retarders

Another option for the vAPP involves the tuning of the retardance in a non-standard way. For most applications the retardance is tuned to be close to half-wave over the full bandwidth of an instrument (Komanduri et al., 2013; Otten et al., 2017) to maximize the efficiency. However, by changing the liquid-crystal recipe one can, in principle, make the retardance follow any continuous curve as

function of wavelength (Hornburg et al., 2014). We note that this is possible because the fast-axis orientation and retardance of the devices are decoupled. One specific application of a liquid-crystal recipe is the “wavelength-selective coronagraph” (Doelman et al., 2017). Here we include a short summary of this work. A wavelength-selective coronagraph has rapidly changing efficiencies, where the retardance switches between intervals of 180 degrees as function of wavelength. A retardance of zero or a full wave results in a zero efficiency, such that the light traveling through the coronagraph does not acquire geometric phase. The coronagraph is effectively switched off at those wavelengths, while it is switched on in the range where the retardance is close to half-wave. This technology has been demonstrated for RGB lenses (Hornburg et al., 2019). An example for the vAPP coronagraph is shown in Fig. 2.9. The retardance is close to 180 degrees for $H\alpha$ and close to zero for smaller than 600 nm and larger than 750 nm. The light outside the $H\alpha$ spectral band can be used by a wavefront sensor, enabling wavefront sensing close to the science bandwidth with optimal efficiency. In addition, the wavefront sensor can be placed after the coronagraph to minimize non-common path aberrations. This requires a simple focal plane mask that separates the central term from the coronagraphic PSFs, aided by some spectral filters to minimize spectral cross-talk.

2.3 Observing and data reduction

The gvAPP can be described as a simple coronagraph, as it is only a single pupil-plane optic that suppresses the diffraction halo. However, there are two differences between other coronagraphs that make both observing and data reduction much less straightforward, i.e. the D-shaped dark zone and the grating. For the D-shaped dark zone of a gvAPP the dark zones do not cover 360 degrees, which takes away a larger fraction for closer-in orbits caused by sky-rotation. This has to be taken into account for planning observations and in the data reduction process. In addition, the grating can smear the planet PSF over multiple pixels in the grating direction, reducing signal-to-noise and the effectiveness of observing techniques like angular differential imaging (ADI) (Marois et al., 2006).

2.3.1 Influence of the D-shaped dark zone

The D-shaped dark zone provides phase solutions that have much higher Strehl ratios for similar smaller inner working angles than a 180 degree dark zone, while providing a similar total area. We note that the term inner working angle is somewhat misleading here. It is correct that the D-shaped and 180 degree dark zone designs can detect a planet down to the same separation, yet the *amount of time* it is in the dark zone for pupil tracking mode is very different. For a 180 degree dark zone the coverage is a full 360 degrees, while a bar is missing for the D-shaped dark zone, which takes away a larger fraction for closer-in orbits. The fraction of a circle, F_{DH} , with radius r that is inside a dark zone with an inner

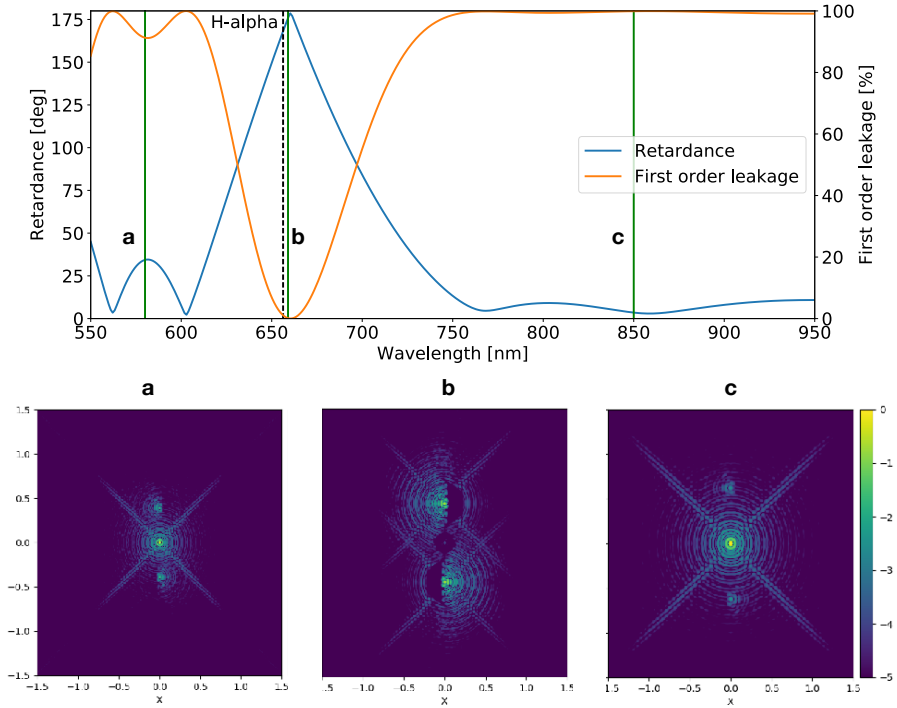


Figure 2.9: *Top*: Simulated retardance (blue) and first order leakage (orange) as a function of wavelength for a 3-layered MTR. The total thickness is 20.7 micron and it was optimized to have 0 retardance everywhere except for a 10 nm band around $H\alpha$ wavelength (656.28 nm), where the retardance is close to 180 degrees. *Bottom*: The simulated PSFs of a grating-vAPP with the retardance profile shown above. The green lines in the top figure correspond to the wavelengths of the bottom panel. At wavelengths shorter than $H\alpha$ the leakage term dominates and almost no coronagraphic PSF can be seen (a). This is the same for wavelengths larger than 750 nm (c). Around $H\alpha$ the leakage term disappears and the gvAPP operates as normal (b).

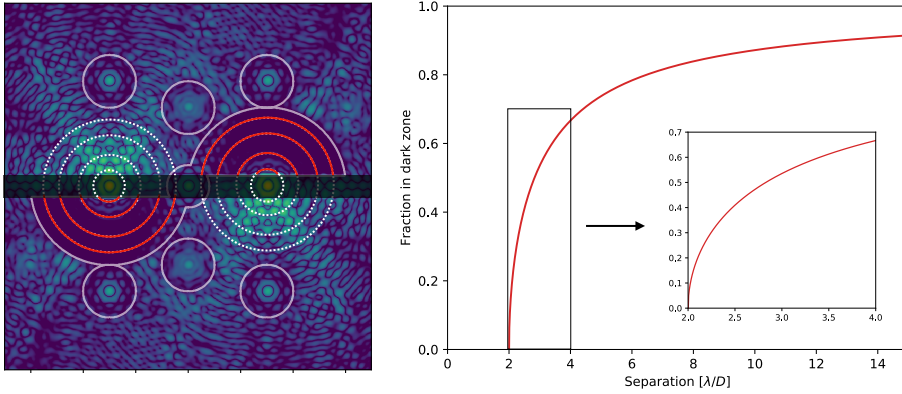


Figure 2.10: Planets rotating in the dark zone in pupil-stabilized mode are not always in the dark zone. *Left*: Fraction of a circle (white) that is in the dark zone (red). *Right*: The same fraction as function of separation for an inner working angle of $2\lambda/D$.

working angle IWA is given by

$$F_{DH} = \frac{\pi - 2 \arcsin(\text{IWA}/r)}{\pi}. \quad (2.2)$$

This fraction is also shown in Fig. 2.10 for a typical gvAPP design. On-sky the rotation speed can change dramatically near Zenith, and the position in the dark zone depends on the local sidereal time at the observatory. Therefore, observations with the gvAPP should be carefully planned if a known target is observed. Planning does not help with detecting unknown objects where certain areas around the star will have more noise due to the sky-rotation placing objects in the bar between dark zones.

For known objects the blind spots created by the incomplete coverage of the D-shaped dark zones can be predicted. To this end, we created a preliminary version of an observation preparation tool in `python`, which can be found on [Github](https://github.com/18alex96/vAPP_preparation)². The goal of this tool is to predict the locations of known companions and provide information on when it is in the dark zone to help determine observation strategies. The current version has an internal library that contains the information of a few operational gvAPPs, such that a simple query returns the predicted locations of companions in a PSF image. The code needs the instrument name, target name, the companion position angle and separation, and the observation times. Wavelength scaling has not been implemented yet. The core of the observation tool is based on `Astropy` (Price-Whelan et al., 2018), which is used to retrieve object information and coordinate transformations.

²https://github.com/18alex96/vAPP_preparation

2.3.2 Influence of wavelength smearing

The grating of the gvAPP is an elegant solution to separate the polarization leakage from the coronagraphic PSFs. It does, however, represent a challenge for the data reduction. For narrow-band data it displaces the two coronagraphic PSFs which need to be recombined after centering them separately. This is similar for data taken with an integral field spectrograph (IFS), except the instrument provides simultaneous multi-wavelength observations. For each wavelength, the stellar PSF and companion PSF will have shifted and also needs to be recombined. This can be characterized, especially if there are no optical distortions in the IFS such that the displacement from the grating is linear. Wavelength smearing is likely to reduce the astrometric accuracy in addition to make object spectra more sensitive to the lenslet flat. For larger bandwidths the wavelength smearing introduces more problems. The light of the planet is smeared over many pixels, resulting in an increase in camera noise and a larger sensitivity to speckle noise. In addition, the planet PSF rotates around the stellar PSF for every wavelength, which is a different location on the detector for every wavelength. In the derotated rest frame of the stellar PSF the orientation of the elongation changes in time, such that ADI techniques are less effective. Collapsing the PSF in the grating direction before derotation might solve this problem, but this does not remove the sensitivity to speckle and camera noise.

The classical vAPP, which separates the two polarization states with a Wollaston prism, would not have these issues caused by the grating (Snik et al., 2012). However, they would be limited by polarization leakage at the smallest separations for large bandwidths. A double-grating vAPP is also not affected by the grating, it is not limited by polarization leakage, and does have full 360 degree FOV at the cost of a larger inner working angle. Combining these two techniques creates a solution for the wavelength smearing and large inner working angle. This combination would consist of a Wollaston prism to separate the two polarization states of a double-grating vAPP with D-shaped dark zones (Bos et al., 2018).

2.3.3 Data reduction

From the complications of data reduction caused by the D-shape of the dark zone and the grating, it is clear that gvAPP data can not simply be reduced with commonly-used data reduction pipelines like the vortex image processing package (VIP) (Gonzalez et al., 2017) or *PynPoint* (Amara & Quanz, 2012; Stolker et al., 2019). These pipelines include different data reduction algorithms that have been developed for data taken without coronagraphs or with focal-plane coronagraphs. In both situations the stellar PSF is not separated and the search space is 360 degrees. However, with a relatively simple adaptation it is possible reshape gvAPP data in a way that these pipelines can be used. We create a window for each coronagraphic PSF and combine them into a single new data frame that is centered on both PSF cores. An example is shown in Fig. 2.11. This method also works for IFS data if the windows change location with wavelength,

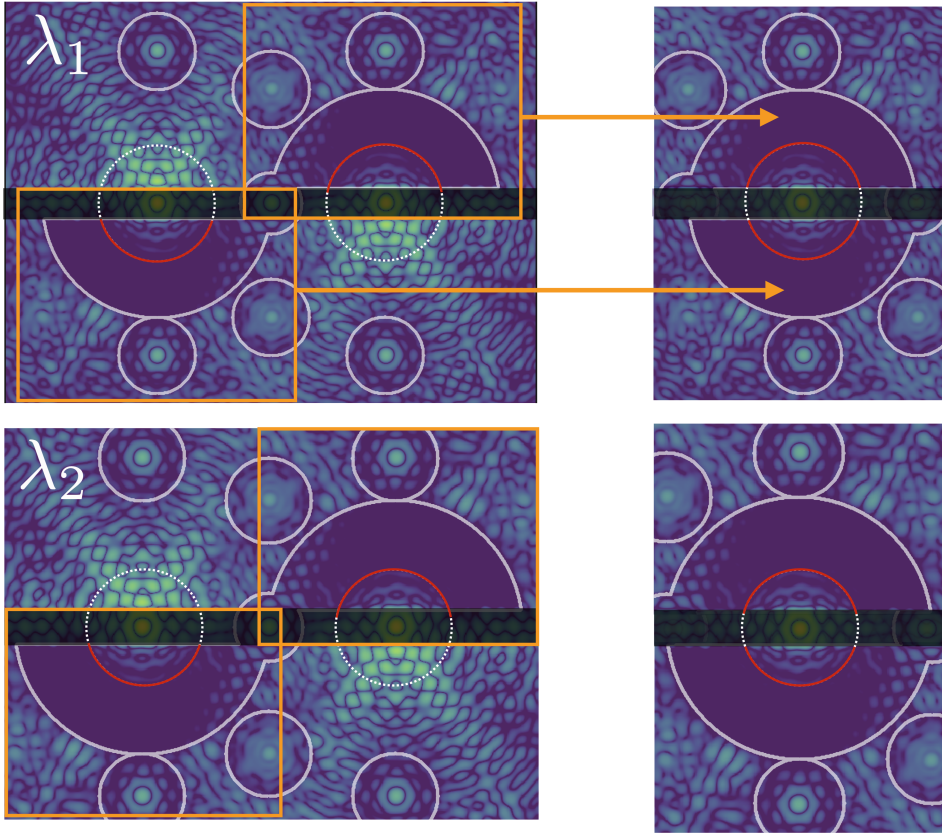


Figure 2.11: Method of recombining both coronagraphic PSFs such that the data can be processed using conventional data reduction techniques.

but does not solve the wavelength smearing for large bandwidths. In addition, it does not make use of the fact that both coronagraphic PSFs are aberrated by the same wavefront aberration. The rotate subtract algorithm, suggested by (Otten et al., 2017), provides an additional contrast gain by using this symmetry. An improved version of this algorithm does not simply subtract the average PSF but uses principle component analysis (Wold et al., 1987) to create a PSF library using one coronagraphic PSF and optimally removing these components from the other PSF. Another interesting technique that seems well suited for gvAPP data is the Temporal Reference Analysis for Exoplanets (TRAP) algorithm (Samland, 2019). TRAP creates a data driven model of the temporal behavior of the systematics using reference pixels, which can also be the pixels at the other coronagraphic PSF. This algorithm would also work for large bandwidths.

2.4 The world of vAPP

Over the last decade the vAPP has been installed in 7 instruments on 6 telescopes, and will be installed in two instruments on the Extremely Large Telescope (ELT). The success of the vAPP can be explained by two of its properties: simplicity and adaptability. Each vAPP is unique and fully optimized for the system it is implemented in, both in wavelength coverage as phase design, while only a single optic needs to be installed. The vAPPs cover almost an order of magnitude in bandwidth, i.e. $0.55\text{-}5\ \mu\text{m}$, provide multiple ways of focal-plane wavefront sensing, and provide photometric/astrometric capabilities. First, we will provide an overview of the different properties and locations of the vAPPs. Then, we will shortly describe the unique capabilities of each vAPP.

2.4.1 The vAPP: a global view

High-contrast imaging systems are now part of most 8m-class telescopes. The vAPP has benefited from the enormous growth in the number of high-contrast imaging systems. A global view of the vAPP coronagraphs is shown in Fig. 2.12. The vAPPs are operational in both the Northern and Southern hemisphere. For each vAPP, we show the phase pattern and the simulated PSF. In addition, we display the project status, indicated by the color of the marker on the map. As of 2020, the vAPP has been tested in two former instruments, is operational in four instruments and will be installed on three more instruments. A summary of most properties of all vAPPs are presented in Table 2.1.

Another important property of the vAPP is the polarization leakage as function of wavelength. The design of the liquid-crystal recipes aims to minimize polarization leakage over the full bandwidth and are given in Table 2.1. For small bandwidths ($< 15\%$), the liquid-crystal design can be kept simple with only single layer with zero twist. Larger bandwidths require multiple layers, each with different thickness and twist, to form a multi-twist retarder (MTR).

Table 2.1: Properties of the vAPP coronagraphs. FPWFS techniques: 1 = AP-WFS (Bos et al., 2019), 2 = cMWS (Keller, 2016; Wilby et al., 2017; Miller et al., 2019), 3 = PD (Gonsalves, 1982; Miller, 2018).

Telescope	Instrument	Type	Inst.	λ [μm]	MTR	Contrast	IWA [λ/D]	OWA [λ/D]	Strehl [%]	FPWFS
Magellan	MagAO/Clio	gvAPP 2x180	2015	2-5	3	10^{-5}	2.0	7	39.8	-
WHT	LEXI	vAPP 360	2017	0.6-0.8	1	10^{-4}	2.5	6	57.2	2
Subaru	SCEXAO/ CHARIS	gvAPP 2x180	2018	1-2.5	3	10^{-5}	2.1	11	49.2	1+3
FC	HiCIBaS	gvAPP 2x180	2018	0.83-0.88	1	10^{-6}	2.1	8.5	28.8	2+3
Magellan	MagAO-X	gvAPP 2x180	2018	0.55-0.9	3	10^{-5}	2.1	15	40.7	1+2+3
LBT	LMIRcam	gvAPP 2x180	2018	2-5	3	10^{-5}	1.8	15	52.6	3
LBT	LMIRcam/ ALES	dgvAPP 360	2018	2-5	3	10^{-5}	2.7	15	42.0	-
VLT	ERIS	gvAPP 2x180	2022	2-5	3	10^{-5}	2.2	15	50.9	1
ELT	METIS	gvAPP 2x180	2028	2.9-5.3	3	10^{-5}	2.5	20	63.8	1
ELT	MICADO	gvAPP 2x180	2026	1-2.5	3	10^{-5}	2.6	20	68.8	-

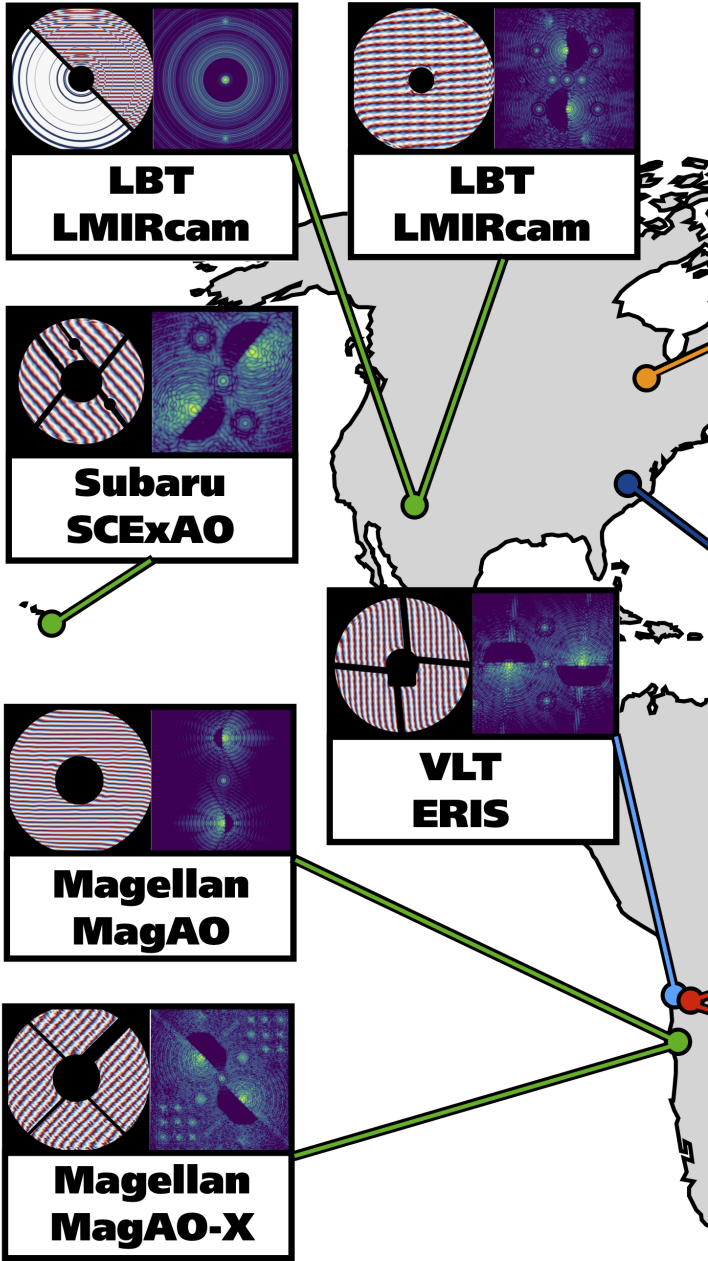
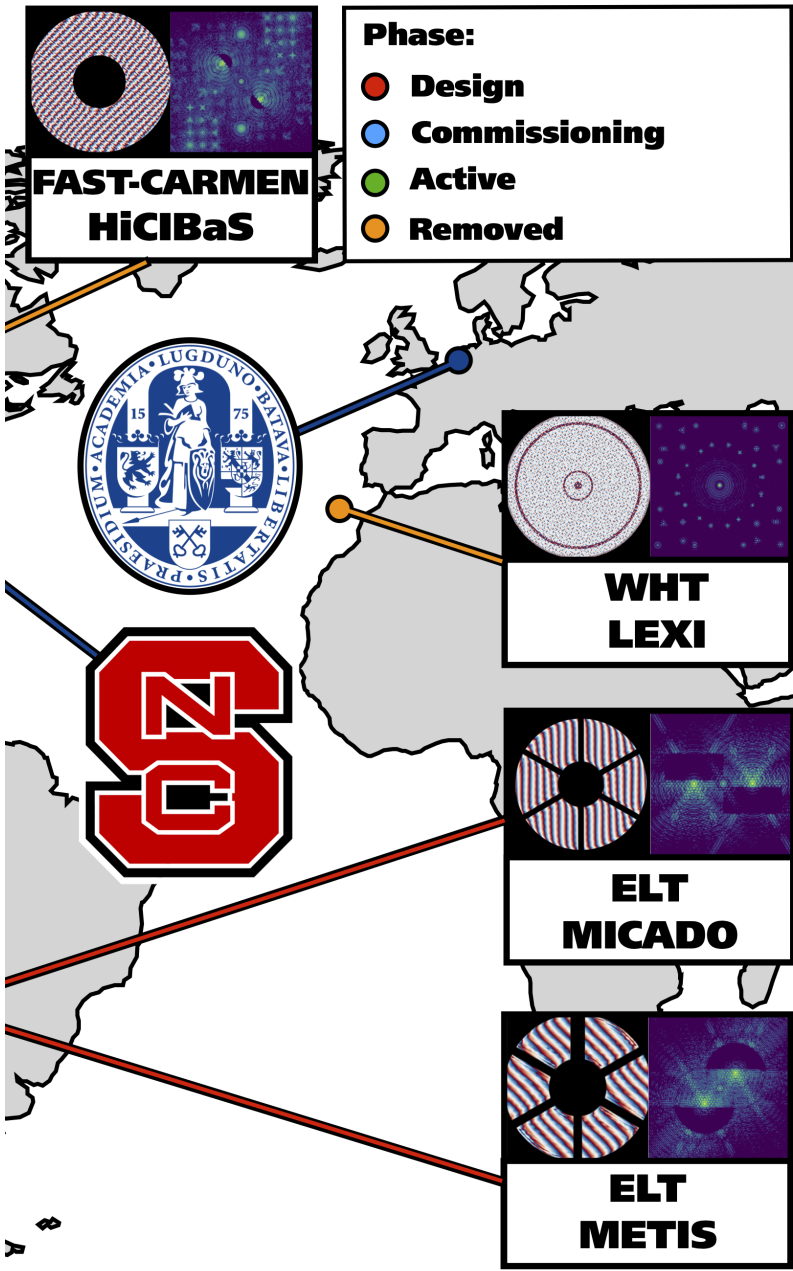


Figure 2.12: Overview and status of the vAPP coronagraphs around the world.



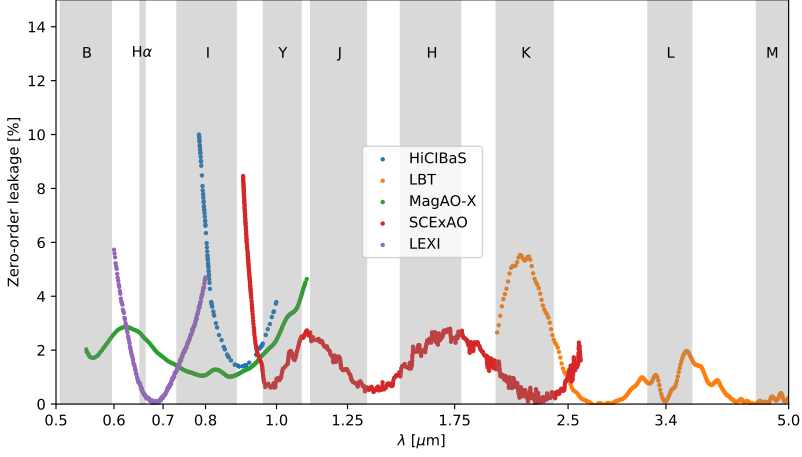


Figure 2.13: Zero-order leakage as a function of wavelength for different liquid-crystal recipes, colored by instrument.

In general, if the bandwidth is between 15 – 40%, a double-layered recipe, i.e. a 2TR, can have a polarization leakage < 3% for the full bandwidth. Similar performance can be reached with a 3TR for bandwidths up to 100%.

When a specific design is chosen, the manufacturing process is tuned to generate a liquid-crystal film with a measured retardance and polarization leakage that mimics the theoretical as closely as possible. The manufactured test films are polarization gratings (PGs), such that it is easy to measure the zero-order leakage using transmission measurements. When a recipe is perfected, the vAPP is manufactured using this recipe. Measuring the zero-order leakage of the final optic can be cumbersome with the small angular separations between the main beams and the leakage, caused by the large grating periods of a gvAPP. Therefore, the leakage measurement of a representative PG is used. These polarization leakages of five different recipes, representative of 5 different instruments and wavelength ranges, is shown in Fig. 2.13. All presented recipes have < 6% leakage over their required bandwidth. Together, they span the almost the full visible and near-infrared (0.55-5 μm). Interestingly, we currently cover this range with three standardized recipes that have good performance in their respective bandwidths. The same data is presented in log-scale in Fig. 2.14. We added the estimated performance of the double-grating vAPP that is installed in the LBT, by multiplying the single-grating curve with itself. We note that no direct measurement of its performance exists.

While the leakage measurements are representative, the actual vAPPs can have different performances. Lab conditions during manufacturing, like temperature and humidity, can generate differences between liquid-crystal films for identical

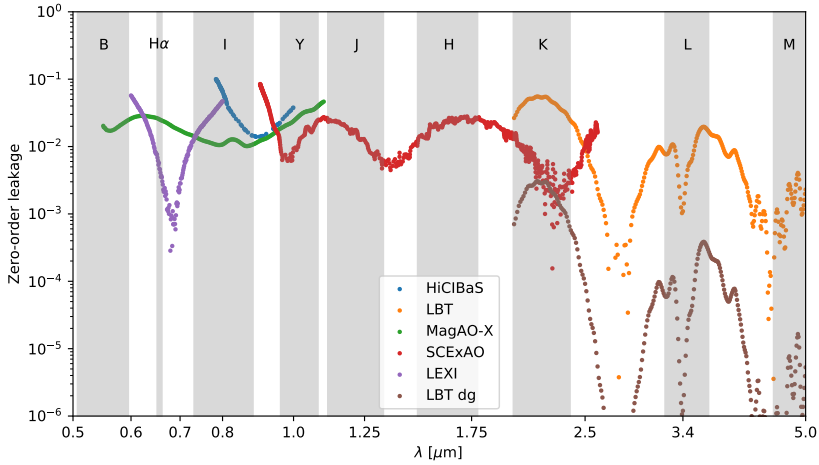


Figure 2.14: Same as Fig. 2.13, but on log-scale and an additional estimate of the LBT double-grating vAPP.

recipes. Characterizing the actual polarization leakage of a vAPP can then be done after installation or in a high-contrast imaging setup. Moreover, all vAPPs with identical wavelength coverage will have different polarization leakages as function of wavelength. These differences can be up to 2% for a specific wavelength, but the impact on the average is minimal. Most likely, it is merely a shift of the maxima and minima as function of wavelength.

2.4.2 The vAPP: individual properties

A large diversity exists between vAPPs, in designs, design goals, additional functionality, and the instruments that use them. We will provide a summary of design trade-offs, unique properties, historical details, notable results, and references to more detailed papers of each vAPP.

Magellan/MagAO/Clio

The first operational broadband gvAPP was installed in 2015 in the MagAO/Clio instrument (Close et al., 2010; Morzinski et al., 2014) at the 6.5-m Magellan Clay telescope. The gvAPP has a dark zone between 2-7 λ/D and operates between 2 to 5 micron, with a polarization leakage less than 3% over this bandwidth. A detailed description of the design, manufacturing and on-sky performance can be found in Otten et al. (2017). Being the first gvAPP to be commissioned, it was a technology demonstrator with the additional goal to use it as a science-grade component. To demonstrate the performance, Otten et al. observed a bright A-

type star with an L' -band magnitude between 0 and 1. Characterization of the leakage term and the PSF showed that the gvAPP was performing as expected. A new method of data reduction, subtracting the opposite rotated coronagraphic PSF, yielded an improvement in contrast of 1.46 magnitudes, i.e. a factor 3.8, at $3.5\lambda/D$. The performance of the gvAPP for this observation was better than the best reported performance in literature of coronagraphs at other systems at this small angle. We note that the method of calculating the noise is necessarily different between the contrast curves reported in literature, as noted in Jensen-Clem et al. (2017). The method of noise calculation in Otten et al. (2017) does not take into account azimuthally correlated speckle noise caused by non-common path aberrations, pointing jitter, and thermal variations. For a gvAPP it is especially difficult to properly estimate the speckle noise at the smallest separations due to the limited amount of photometric apertures that fit in the D-shaped dark zones. A better comparison between this gvAPP and other coronagraphs would be to use the same detection limit methods that are commonly used, e.g. fake planet injection.

So far, the scientific yield of the MagAO/Clio gvAPP is limited, with only a marginal detection of a brown dwarf companion of HR 2562 (Sutcliffe et al., 2019, Submitted for publication). This can be explained by the total awarded observing time (<10 nights), which is insignificant in comparison to the SPHERE and GPI surveys (>300 nights) that detected on the order of 10 sub-stellar companions (Nielsen et al., 2019; Vigan et al., 2020). Moreover, observing with a gvAPP can be challenging, especially when using broadband filters, see section 2.3.

WHT/LEXI

The Leiden Exoplanet Instrument (LEXI) was a visiting instrument at the William Herschel Telescope (WHT) (Haffert et al., 2016, 2018). The goal of the LEXI instrument was to develop and test new technology for new high-contrast imaging techniques, e.g. the cMWS and high-contrast, high-dispersion integral field spectroscopy (Wilby et al., 2016, 2017; Haffert et al., 2018). The instrument changed between different visits, changing the pupil (4m on-axis, 1m off-axis), the wavefront sensor, imaging modes, spectrographs and vAPP designs. The first observation run in 2016 employed a spatial light modulator with an APP + cMWS design. This test succeeded, making it the first demonstration the focal plane wavefront sensing capabilities of the cMWS on-sky. A second run in 2017 used a simplified instrument, replacing the SLM for a vAPP. Two instrument properties were taken into account for the design of the vAPP. First, the ALPAO deformable mirror with 97 actuators, which has a limited control radius. Second, the AO-loop speed was limited at 800 Hz by the camera frame rate. Thus, the vAPP designs were optimized for 10^{-4} contrast between 2.5 - $6 \lambda/D$, resulting in a phase pattern 0 - π concentric rings. A grating mask used to define the aperture with the vAPP. With a narrow science band between 600 nm and 800 nm, the vAPP is a 1TR, resulting in a polarization leakage less than 6%. The intensity of the leakage at the IWA

is lower than the design contrast, which enabled the use of a 360 vAPP without gratings. The vAPP was multiplexed with 20 Disk Harmonic holograms, resulting in an improved wavefront correction (Haffert et al., 2018).

Subaru/SCEXAO/CHARIS

The Subaru Coronagraphic Extreme Adaptive Optics (SCEXAO) (Jovanovic et al., 2015) instrument is an ever-evolving high-contrast imaging system at the 8.2-m Subaru Telescope, with the aim of providing a platform for technology demonstration for next generation telescopes. A more recent, and already outdated, overview of the instrument can be found in (Lozi et al., 2020). The gvAPP in SCEXAO was installed in 2017 in the near-infrared arm (0.9-2.5 μm) (Doelman et al., 2017). The design of the gvAPP has a reduced grating frequency compared to previous designs to make the PSF fit in the SCEXAO/CHARIS field of view (FOV) for the full bandwidth (Doelman et al., 2017). CHARIS is an integral field spectrograph with a resolution of $R \sim 18.4$ for a bandwidth spanning the J , H , and K bands (1.13-2.39 μm) and a FOV of $2'' \times 2''$ (Groff et al., 2017). To fit these instrument specifications, the gvAPP was manufactured with a new liquid-crystal recipe with a diffraction efficiency greater than 97% between 1-2.5 μm . Two additional features of this gvAPP are the grating mask that is undersized with respect to the amplitude mask of SCEXAO and defines the gvAPP pupil, and the first implementation of phase diversity spots. At the inner working angle of $2.1 \lambda/D$, the design contrast is 10^{-5} , and the outer working angle is $11 \lambda/D$, which is limited by the CHARIS FOV in K-band.

The gvAPP was installed together with a patterned ND-filter in the focal plane, which reduces the coronagraphic and leakage PSF intensity by a factor 10-50, depending on wavelength. An image of the PSF with the patterned ND-filter is shown in Fig. 2.15. Such a focal plane mask enables longer integration times and reduces the risk of saturation and resulting persistence of the sensitive NIR cameras. The PD holograms are not blocked and can also be used as a photometric reference. After installation, the first-light images of the gvAPP with CHARIS showed a PSF shift by ~ 1 arcsecond caused by the wedge of the optic. A second wedged optic that is identical to the one used in the gvAPP was installed in a filter wheel downstream to successfully correct this shift.

Testing with the internal source showed promising results with a raw contrast $< 10^{-3}$ at the inner working angle, and $< 10^{-4}$ beyond $4.5 \lambda/D$ (Bos et al., 2019), demonstrating that the delivered gvAPP is within specifications and commensurate with the performance of the system and other coronagraphs. However, on-sky testing resulted in raw-contrasts that were a factor 5-10 worse, caused by prominent diffraction structures present in the dark zones. These structures are visible in Fig. 2.15 as bright lines of speckles orthogonal to the flat side of the dark zone. These structures are not present when using any other coronagraph present in SCEXAO. Inspection of pupil images with and without the gvAPP showed that these structures are not caused by pupil misalignment. In addition, the absence of these structures in the internal source data suggests that they are caused by optics

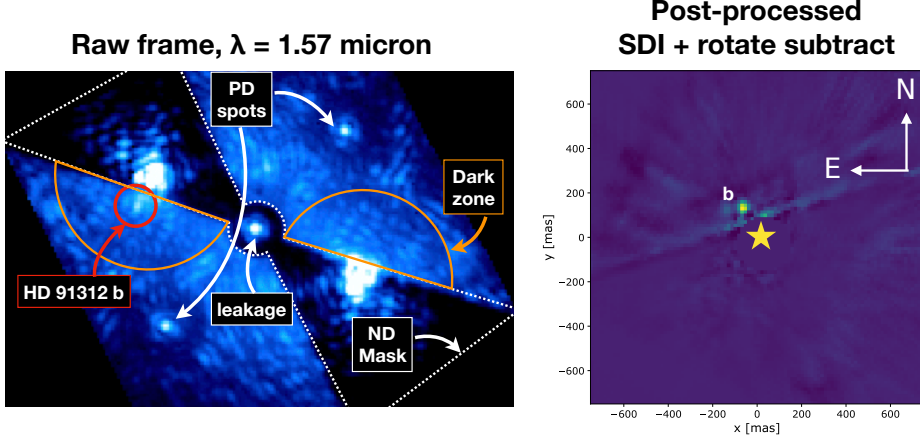


Figure 2.15: Observations of HD 91312 with the gvAPP with CHARIS. *Left:* Image slice from the extracted data cube showing the raw PSF. *Right:* Final image of HD 91312, showing the companion clearly. The bright streak is a result of post-processing. The scale of both images is different.

upstream of SCExAO, e.g. the telescope mirrors or AO188, an upstream adaptive optics instrument. Simulations show that annular phase offsets at the pupil edges can reproduce similar dark zone structures, which would not be noticed by other coronagraphs when a Lyot stop is used. An annular phase structure can be seen in the on-sky wavefront reconstruction in (Bos et al., 2019) and it also has been observed with the pyramid wavefront sensor, but so far any attempt to correct these phase offsets did not result in a significant improvement of the dark zone contrast.

Despite the lower-than-expected raw-contrast, on-sky observations have been carried out with both the imager SCExAO/Chuckcam and the IFU SCExAO/CHARIS. One of the first tests of the gvAPP was the observation of HD 91312 with CHARIS on 7 February 2018, for a total of integration time of 5 minutes 29 seconds. HD 91312 is a good candidate as it is a binary system, with a companion at a separation of 150 mas (~ 5 AU), which has a minimal mass of $80 M_{Jup}$ (Borgniet et al., 2019), and therefore is most likely a M-dwarf. Because HD 91312 A is an A-star, the relative contrast to HD 91312 b in the near infrared is already favourable and becomes lower towards longer wavelengths. The companion was detected in the raw frames, even with the diffraction structures present. Post-processing with spectral differential imaging (SDI) (Racine et al., 1999) and rotate subtract (Otten et al., 2017) removed the diffraction structures. The extracted PSF at $\lambda = 1.57\mu\text{m}$ and the final post-processed image are shown in Fig. 2.15. While the on-sky raw contrast is limited by the uncorrected diffraction structures, the SCExAO gvAPP is still valuable as a technology demonstration of focal-plane wavefront sensing. The phase diversity between both coronagraphic PSFs, combined with the asym-

metric pupil of SCExAO, resulted in the first demonstration of FPWFS with only the coronagraphic PSFs (Bos et al., 2019). The improvement of a factor two in raw contrast between $2\text{--}4 \lambda/D$ is similar to other FPWFS techniques (Galicher et al., 2019). An additional improvement can be realised by implementing LDFC (Miller et al., 2019, 2020; Bos et al., Submitted for publication). However, it is unclear if the combination of both FPWFS techniques will resolve the issue with diffraction structures in the on-sky PSF. A future upgrade of AO188 could resolve the issue and enhance the gvAPP performance.

FAST-CARMEN/HiCIBaS

As is mentioned in the name, the High-Contrast Imaging Balloon System (HiCIBaS) is a balloon-borne telescope and is installed on the FAST-CARMEN gondola (Côté et al., 2018). The main goals of this mission were to test new high-contrast imaging technology in a space-like environment and the training of five master students of Laval university (Thibault et al., 2019). The scientific goal was to measure and characterize the wavefront distortions from high-altitude ($>40\text{km}$) turbulence, using low-order wavefront sensors (LOWFS) (Allain et al., 2018). The balloon launched August 25 2018 at 11:18 pm local time from the Timmins Stratospheric Balloon Base in Ontario, Canada. The flight plan was to ascend to 40 km, and stay there for the duration of ~ 12 hours. A separate arm was created for high-contrast imaging. This arm would benefit from the pointing stabilization necessary for the LOWFS measurements. The 37-element IRIS AO MEMS deformable mirror was installed to correct wavefront aberrations, however, it was not connected to the LOWFS to reduce complexity. The gvAPP was selected because the coronagraph is stable against residual pointing inaccuracies. The design has a small dark zone from 2.1 to $8.5 \lambda/D$ and a contrast of 10^{-6} , delivering more extreme performance in the low-turbulence regime. With a limited bandwidth between 0.83 and $0.88 \mu\text{m}$, a 1TR gvAPP was sufficient. Also, the gvAPP was designed to provide complementary wavefront sensor information using a 12-mode Zernike basis cMWS or PD holograms. The performance of the LOWFS and the gvAPP FPWFS were successfully tested close-loop in the system before the flight. The PSF before the flight is shown in Fig. 2.16. An internal laser source was used to show that both the cMWS and the PD holograms worked.

While the launch and flight happened according to the flight plan, an unfortunate mechanical failure resulted in the inability to operate the telescope. As a result, the telescope never pointed at a celestial source. An internal source was present in the flight instrument case of such a failure, which was used to record the gvAPP PSFs. It was also discovered that the deformable mirror did not respond to commands in flight and was stuck in a random, non-flattened state. Extreme noise from electronic crosstalk resulted in low-quality images of the PSF. The resulting images are not useful to characterize the gvAPP performance during flight, see Fig. 2.16. The balloon and payload were recovered after the flight. The high-contrast imaging system, including the gvAPP, were still operational. Post-launch images of the gvAPP PSF do not show any significant deviation from pre-launch

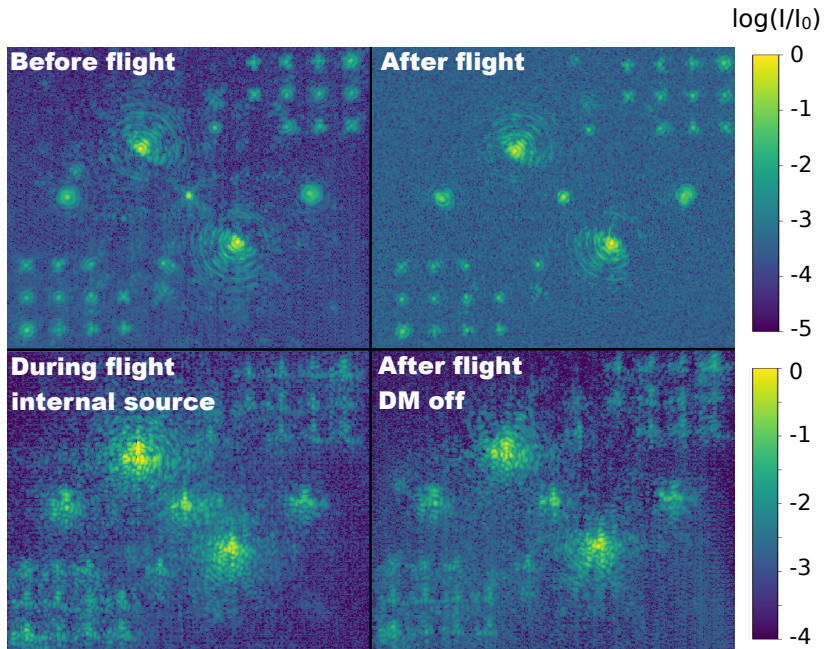


Figure 2.16: Measurements of the HiCIBaS gvAPP PSF ($\log_{10}$ scale) before, during, and after the flight using the internal source of the HiCIBaS instrument. No optical component of HiCIBaS sustained major damage during the landing. The system was realigned after the flight.

performance, and the flight PSF is similar to the after-flight PSF with the DM off. We note that both comparisons are qualitative, and have not been fully characterized. We conclude that the gvAPP or similar LC coronagraph can operate in a space-like environment.

Magellan/MagAO-X

The MagAO-X instrument is a completely different instrument than MagAO, operating in the visible and near-infrared with an extreme AO (ExAO) system (Males et al., 2018). The key science goal of MagAO-X is high-contrast imaging of accreting protoplanets at $H\alpha$ (656.28 nm). To achieve this goal, MagAO-X will deliver high Strehls ($>70\%$ at $H\alpha$), and high contrasts ($< 10^{-4}$) from ~ 1 to $10 \lambda/D$. In addition, MagAO-X implements many of the lessons-learned from SCExAO, including the real-time controller CACAO³. The first phase (Phase I) aims to fully characterize and calibrate the instrument while obtaining the first science results. With non-optimal wavefront correction in phase I, the gvAPP was chosen as a robust coronagraph. To accommodate wavefront sensing and good coronagraphic performance, the Strehl ratio of the design is lower than most other coronagraphs (40.7%). The coronagraph design creates a dark zone from $2.1\text{--}15 \lambda/D$, with 10^{-5} contrast at the IWA, and the dark zones are elongated in the grating direction. Therefore, wavelength smearing up to 20% does not compromise the dark zone towards the edges.

The gvAPP pupil was specifically altered with a thicker spider to be asymmetric with the goal of enabling focal-plane WFS using the coronagraphic PSFs. As a result, the gvAPP design employs three ways of wavefront sensing, i.e. PD, cMWS, and AP-WFS, in addition to LDFC for wavefront control. Each of these wavefront sensing modes have been tested separately using a test plate with different gvAPP designs (Miller, 2018; Miller et al., 2019). The wavefront sensing capabilities enable better instrument calibration by accurately measuring non-common path aberrations (NCPA), which are more severe in the visible. MagAO-X employs a separate DM that is dedicated to correct NCPA, which will be fed directly by the focal-plane wavefront sensors of the gvAPP. FPWFS can be done at much greater speeds with MagAO-X because a laser-cut mask in the intermediate focal plane separates the dark zones from the bright field. This mask transmits the dark holes to the EMCCD science camera and reflects the stellar bright field back to a second EMCCD that will act as the dedicated FPWFS. The cMWS was especially useful for alignment of the off-axis paraboloids, providing direct visual feedback on the first 9 low-order Zernike modes. For on-sky operations, a likely strategy would be to use PD, cMWS and AP-WFS to minimize the non-common path aberrations before observing and use LDFC to remove any drifts.

MagAO-X had first light in 2019, where it demonstrated a Strehl ratio of 46%, and a 5σ post-processed gvAPP contrast of 10^{-4} at $3 \lambda/D$ at 900 nm (z') (Males et al., 2020). These results are promising for discovering exoplanets during formation through direct detection of $H\alpha$ from accretion of hydrogen onto these protoplan-

³<https://github.com/cacao-org>

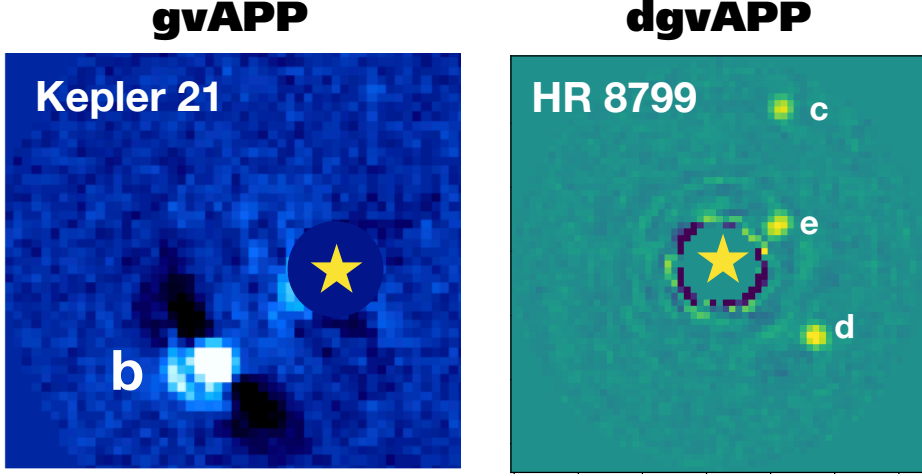


Figure 2.17: Detection of Kepler 21B using the gvAPP at LBT/LMIRcam ($\Delta m = 3.9$ and the inner three HR 8799 planets ($\Delta m \approx 10$) using the dgvAPP at LMIRcam/ALES.

ets. Applying the Massive Accreting Gap (MAG) protoplanet model (Close, 2020) to the observed first light MagAO-X contrasts results in a predicted maximum yield of 46 ± 7 planets from 19 stars (Close et al., 2020).

LBT/LMIRcam/ALES

The Large Binocular Telescope Mid-Infrared camera (LMIRcam) is an imager/spectrograph that operates behind the Large Binocular Telescope Interferometer (LBTI) (Skrutskie et al., 2010). The LBT is a unique telescope with two 8.4-m primary mirrors mounted next to each other. Both apertures can be combined with LBTI and create fringes on LMIRcam, resulting in a 22.8-m baseline. The LBT and LMIRcam are ideal for L and M band observations with a minimal number of warm optics and a deformable secondary mirror. This makes LBTI/LMIRCAM the most sensitive infrared instrument in the Northern hemisphere. We take advantage of this opportunity with two different vAPPs, a grating vAPP ($1.8-15 \lambda/D$) and a double-grating vAPP ($2.7-15 \lambda/D$). The designs are pushing the limits in inner working angle, and the gvAPP also incorporates focal-plane wavefront sensing with PD holograms and photometric/astrometric reference spots. Their more extreme designs are enabled by the small secondary and the extremely thin secondary support structure. The optic contains two vAPPs, one for each aperture. Their beams can be imaged separately, partially combined with overlapping fringing holograms, or completely overlapped to produce fringes for nulling.

LMIRCam was augmented in 2015 with the Arizona Lenslets for Exoplanet Spectroscopy (ALES) (Skemer et al., 2015), an integral field spectrometer (IFS). After

a recent upgrade, ALES facilitates 2 to 5 μm low-resolution ($R\sim 35$) spectroscopy of directly imaged gas-giant exoplanets (Skemer et al., 2018). Currently, it is the only IFS operating in the L and M bands, containing broad molecular features (CO , CH_4), and also covers the 3.1 μm ice feature, 3.3 μm PAH feature, and 4.1 μm Br-alpha emission line. Therefore, low-resolution spectroscopy can provide a unique window for gas giants in the L-T transition, where their atmospheres transition from CO-rich and cloudy (L-type), to CH_4 -rich and relatively cloud free (T-type).

Both vAPPs installed in LMIRcam are available for ALES, and, together with the annular groove phase mask (AGPM) coronagraph, they are the only coronagraphs installed in LMIRcam/ALES that cover the full wavelength range. Both vAPPs do have significant absorption (up to 100%) between 3.15 and 3.45 μm from glue and the liquid-crystals. The outer working angle of both coronagraphs is larger than the FOV of ALES for wavelengths larger than $\sim 3 \mu\text{m}$. For the gvAPP only one of the two coronagraphic PSFs can be fitted inside the FOV, and the wavelength smearing moves it across the detector. While this is not ideal, the gvAPP provides a much smaller inner working angle compared to the dgvAPP. The dgvAPP provides a stable central PSF and is more sensitive than the gvAPP due to the recombination of both coronagraphic PSFs. Moreover, as it provides a 360 degree dark zone it is much more user friendly and intuitive.

Tests with the internal source show that both vAPPs are operating as expected. Only a few observations have been carried out, but already show the great promise of these vAPPs, see Fig. 2.17. The results on the HR 8799 system will be discussed in more detail in a future paper. The unique feature of the vAPPs is the presence of the stellar PSF on the detector. This is particularly interesting for photometric monitoring of exoplanets. For example, monitoring the stellar PSF can be used to reduce the impact of variability in AO performance during the observing run. In addition, an upgraded data reduction technique has been developed to remove the thermal background with great accuracy using the science frames themselves. Nodding the telescope to characterize the thermal background with off-source measurements is still necessary, however at much lower cadence, increasing the on-source time. To summarize, there are still many opportunities with the vAPPs in LMIRcam/ALES.

VLT/ERIS

The Enhanced Resolution Imager and Spectrograph (ERIS) will be installed in the Cassegrain focus of UT4 at the Very Large Telescope in the near future (Amico et al., 2012; Davies et al., 2018). ERIS is a 1-5 μm instrument with an imager (NIX) operating from J - M_p band and an IFS (SPIFFIER) in J - K band with $R\sim 8000$. ERIS/NIX will have a vortex coronagraph and a gvAPP, while ERIS/SPIFFIER is non-coronagraphic. The ERIS gvAPP has a dark zone from 2.2-15 λ/D , which has been widened to accommodate wavelength smearing, and the APP phase is multiplexed with two photometric/astrometric reference spots (Kenworthy et al., 2018b). The pupil has an asymmetric central obscuration because the (warm)

tertiary mirror (M3) will be moved aside to illuminate the Cassegrain focus where ERIS is residing. While the asymmetry is small, it is still possible to estimate NCPA with FPWFS (Bos et al., 2019) if the software is implemented. The gvAPP has been manufactured in 2018, and was later tested in the near-infrared test bench of the group for Exoplanet & Habitability at ETH Zurich (Boehle et al., 2018). The setup imaged the gvAPP PSF at $3.8 \mu\text{m}$ and was limited by background noise to $\sim 10^{-3}$. Since then an updated setup has been realized and the gvAPP was tested to the $\sim 10^{-5}$ level (Boehle et al., Submitted for publication). These measurements demonstrate the ERIS/gvAPP operates as expected, within the limits of the test bench.

While ERIS/NIX is an imager, it will have a long-slit spectroscopic mode with $R \sim 850$, covering the full L band. With the gvAPP absorption feature between $3.15\text{--}3.45 \mu\text{m}$, direct detection of methane will be more difficult. For atmospheres with elevated methane levels, e.g. T-type brown dwarfs, the spectral slope beyond $3.5 \mu\text{m}$ can be used to measure methane levels. Another unique opportunity of ERIS/NIX is enabled by the combination of a sensitive wavefront sensor and the powerful (20W) laser guide star. The laser guide star allows observations of much fainter science targets, which will greatly increase the number of potential targets accessible to this new instrument.

ELT/METIS and ELT/MICADO

The Extremely Large Telescope (ELT) (Gilmozzi & Spyromilio, 2007) will revolutionize direct imaging of exoplanets because of its primary mirror diameter of 39 meters. The supreme resolution will be fully exploited by first generation instruments. With five times the resolution of the VLT and 25 times the sensitivity, the ELT will provide new insights in planet formation, protoplanetary disks, planet-disk interaction, planetary atmospheres and planet evolution. Both the Mid-infrared ELT Imager and Spectrograph (METIS) (Brandl et al., 2016) and the Multi-Adaptive Optics Imaging Camera for Deep Observations (MICADO) (Davies et al., 2016) have exoplanet detection and characterization as one of the main science goals. To this end, both instruments have a gvAPP baselined.

METIS covers the science bands between $3\text{--}14 \mu\text{m}$, and has a high-resolution IFS mode with $R \sim 100,000$ in L and M band, in addition to an imaging mode from L to N band. This high spectral resolution is achieved over a large FOV of 0.5 by 1.0 arcseconds, which is made possible by an image slicer that divides the field of view into multiple strips on a slicer mirror. Simulations show that METIS will detect and characterize multiple planets found with radial-velocity studies (Quanz et al., 2015). Two gvAPPs with different dark zone designs will be installed in the IFS and the imager in L and M band (Kenworthy et al., 2018a). A specific downside of the gvAPP is that the star light is not blocked, leading to high intensities in the IFS focal plane. This can be prevented by changing the position of the star in the field of view using the chopper. Due to this offset only the dark zone of the gvAPP PSF is imaged onto the image slicer. The ELT pupil is not favourable for coronagraph design, with the large central obscuration. The METIS pupil is

a cold stop and has additional thick spiders, complicating the design process further. The METIS gvAPP design therefore has a larger inner working angle of $2.5 \lambda/D$ to keep the Strehl above 65%. Moreover, the gvAPP has a more moderate contrast towards the inner working angle, going down from a few times 10^{-4} at $3 \lambda/D$ to 10^{-6} beyond $6 \lambda/D$. Simulations show that this does not affect the performance of the coronagraph compared to other baselined coronagraphs like the AGPM, as NCPA, residual wavefront aberrations, and missing mirror segments of the primary will limit the performance at the smallest separations. In addition, the AGPM is quite sensitive to tip-tilt which can be significant for nodding and high frequency structural vibrations (Glück et al., 2016).

MICADO, the European ELT first-light imager (Clénet et al., 2018a), covers the science bands between $0.8\text{--}2.4 \mu\text{m}$ and will benefit from both the M4 single-conjugate AO system (Clénet et al., 2018b) and the dedicated multi-conjugate AO system instrument (MAORY) (Diolaiti et al., 2016). With diffraction limited performance, MICADO will deliver extremely high-resolution imagery to study the inner regions of planetary systems (Baudoz et al., 2019). The high contrast imaging modes will comprise two classical Lyot coronagraphs (Perrot et al., 2018), one gvAPP and two non redundant masks (Lacour et al., 2014). One challenge in designing the high contrast imaging modes of MICADO comes from the fact that they have to be limited to one focal plane upstream the atmospheric dispersion corrector, and one downstream pupil plane. While the atmospheric dispersion might have an impact on the performance of the smallest Lyot coronagraph in broadband, gvAPP is not sensitive to this effect and will thus offer high performance even at high airmass. The MICADO gvAPP design is optimized between $2.5 \lambda/D$ and $20 \lambda/D$ with a square shape. On-sky expected contrast performance reaches 2×10^{-5} at $3.5 \lambda/D$ in K band with a Strehl ratio of 70%. For bright nearby stars, the starlight could saturate the detector for the shortest exposure time, and the use of a neutral density filter might be necessary.

2.5 Current status and future developments

With the vAPP successfully installed in many different telescopes, the focus for the vAPP developments is now transitioning from testing and commissioning the technology, to science observations. Much of the time spent on vAPPs so far has been oriented towards technology development and design optimization. However, the on-sky technology demonstration, observation planning, and data reduction are critical to achieve competitive science results.

The majority of the current on-sky data with a vAPP have been taken with the MagAO, LEXI and SCEXAO instruments. Bright targets were selected to provide optimal AO correction for technology demonstration of the vAPP and FPWFS. While the technology demonstration was often successful and benefited from test observations and consequent understanding and iterations, time awarded to science observations has been limited, and conditions for these observations have been sub-optimal. Moreover, attempts on more challenging targets, e.g. HD

206893 with SCEXAO, resulted in non-detections. We tried bridging this gap by pursuing targets with intermediate contrast by looking into stellar multiplicity and to understand the detection limits. This science case was awarded a few nights at the LBT and Subaru, most of which were lost due to bad weather. Currently the vAPPs of the LBT have yielded the best results, recovering HR 8799 c,d,e.

To fully exploit the opportunities of the ERIS, MICADO and METIS gvAPPs, getting more experience with on-sky observations is paramount. We note that these instruments have had a gvAPP baselined in the instrument design, and have dedicated engineering time planned to resolve any issues. Moreover, of all the vAPPs that are currently installed, only the SCEXAO gvAPP did not reach the expected performance on-sky. The diffraction structures in the SCEXAO dark zones are not caused by the gvAPP itself because the lab results do not show these structures. So, it is likely caused by uncorrected aberrations from the optics upstream of the internal source injection, which is unlikely for the ERIS instrument that is installed in the Cassegrain focus. For METIS and MICADO the vAPPs will be tested extensively and problems should be identified during this process. We conclude that future efforts should focus on observation planning and a standardized vAPP data reduction pipeline.

For both observation planning and a data reduction pipeline a preliminary version already exists, as discussed in Section 2.3. The vAPP observation preparation tool does include most vAPPs that are currently available, however, it does not provide a proper indication whether a companion will be in the dark zone. In future upgrades we will add this functionality, in addition to showing the field rotation of the companion in the dark zones of on-sky PSFs. Ultimately, this could be used to calculate which days of a semester are optimal for observations of known objects to help proposal writing.

The data reduction pipelines are currently all custom for each vAPP. A unification of these pipelines would centralize all efforts on vAPP data reduction and provide a standardized pipeline that can be used by anyone with vAPP data. In addition, it would increase efficiency of implementing new algorithms like rotate-subtract or TRAP. To minimize duplication of previous efforts, it is essential that the pipeline can also port to existing post-processing pipelines like the vortex image processing package (VIP) (Gonzalez et al., 2017) or *PynPoint* (Stolker et al., 2019). Lastly, these pipelines should include methods to use capitalize on the astrometric and photometric holographic PSFs.

Future technical developments should be towards enabling broadband imaging with the vAPP. The main challenge to overcome is a (super)achromatic QWP that adds minimal wavefront aberration and ghosts to the system (Bos et al., 2018). By adding another QWP before the vAPP, it is also possible to combine the vAPP with imaging polarimetry (Snik et al., 2014; Bos et al., 2018), another powerful tool to distinguish astronomical signals from speckle noise (Kuhn et al., 2001). Adding multiple coronagraphic PSFs per polarization state can then simplify more advanced polarimetric vAPP designs (Bos et al., 2020). Another potential interesting avenue to explore is the combination of the vAPP with multi-color holography (Doelman et al., 2019), as that would completely eliminate leakage

problems (Bos et al., 2020). However, this implementation is more difficult to implement in an instrument and puts strong requirements on the shape of the pupil.

2.6 Conclusion

The vector-apodizing phase plate coronagraph is a versatile single-optic pupil-plane coronagraph that is easily adapted to any telescope aperture. It delivers good contrast ($\geq 10^{-4}$, limited by AO performance) at small inner working angles ($\sim 2\lambda/D$), it can host many different focal-plane wavefront sensing techniques, and can include astrometric and photometric reference PSFs. The manufacturing using direct-write for liquid-crystal technology enables extreme and accurate patterning and the multi-twist retarder technology provides excellent efficiencies ($> 96\%$) for bandwidths up to 100% between $0.55\ \mu\text{m}$ and $5\ \mu\text{m}$. Because of these properties, the vAPP has now been installed in 6 different instruments. Measurements with the internal source of these instruments demonstrate that the vAPPs are operating as expected. The grating of gvAPPs and their D-shaped dark zone make observing and data reduction more complicated compared to focal-plane coronagraphs. Future efforts should focus on software for observation planning and data reduction to fully exploit the opportunities provided by future instruments that have the vAPP baselined, i.e. VLT/ERIS, ELT/METIS, and ELT/MICADO.

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