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Imperfections: using defects to program designer matter

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The work presented in this dissertation was conducted at AMOLF, Amsterdam, an institute of the Netherlands Organisation for Scientific Research (NWO), and at the Leiden Institute of Physics, Leiden University.

The cover shows a hand-sized groovy sheet, 3D-printed using a flexible material (courtesy of Jeroen Mesman-Vergeer), snapped into a spiralling shape.

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You are trying to solve a problem.
You're almost certainly halfway done,
maybe more.

Jane Hirshfield