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## On the computation of norm residue symbols

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# On the computation of norm residue symbols

Jan Bouw

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