

**Measures and matching for number systems** Maggioni, M.

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## Curriculum Vitae

Marta Maggioni was born in Italy in 1992. She graduated *cum laude* in 2011 with a scientific degree from the high school M.G. Agnesi. Afterwards she studied Mathematics at the University of Milano Bicocca, where she obtained a Bachelor of Science cum laude in Mathematics in 2014. She was part of the Algant Erasmus Mundus fellowship, studying at the University of Leiden, The Netherlands, and the University of Regensburg, Germany. She obtained *cum laude* a double degree as a Master of Science in Mathematics in 2016 in Bordeaux, with a thesis on *Nearly holomorphic* modular forms, supervised by Prof. Dr. G. Kings. In September 2016 she moved back to Leiden to start her PhD research project under the supervision of Dr. C. Kalle. She served as a teaching assistant in several courses, mainly in the area of Algebra, Probability and Statistics. In 2019 she supervised students of the Leiden PRE-University programme, who won the Jan Kijne Onderzoeksprijs. She presented her research at multiple scientific conferences and was invited to local seminars around Europe. She organised the first event Networks goes to school in 2018 with Dr. N. Starreveld, by an initiative of B. Groeneveld. The masterclass is now an annual meeting for secondary students and teachers across The Netherlands. She is a member of SAMI - Supporting African Maths Initiative, and she volunteered in various Maths camps in Kenya and Tanzania over the years.

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