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Nonparametric inference in nonlinear principal components analysis: Exploration and beyond

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Nonparametric Inference in
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Exploration and Beyond

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Exploration and Beyond

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