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On periodically driven quantum systems

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On periodically driven quantum systems

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Brian Michael Tarasinski

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Cover: Geometric interpretation of the two winding numbers of a non-trivial time evolution operator of a driven Su-Schrieffer-Heeger model (cf. Chapter 3).

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