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## On periodically driven quantum systems

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# On periodically driven quantum systems

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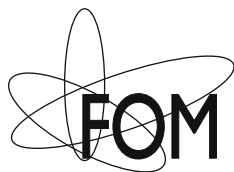
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Cover: Geometric interpretation of the two winding numbers of a non-trivial time evolution operator of a driven Su-Schrieffer-Heeger model (cf. Chapter 3).





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