A perfect power-law spectrum even at highest frequencies: The Toothbrush relic

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ABSTRACT

Radio relics trace shock fronts generated in the intracluster medium (ICM) during cluster mergers. The particle acceleration mechanism at the shock fronts is not yet completely understood. We observed the Toothbrush relic with the Effelsberg and Sardinia Radio Telescope at 14.25 GHz and 18.6 GHz, respectively. Unlike previously claimed, the integrated spectrum of the relic closely follows a power law over almost three orders of magnitude in frequency, with a spectral index of $\alpha_{120\,\text{MHz}}^{18.6\,\text{GHz}} = -1.16 \pm$ 0.03. Our finding is consistent with a power-law injection spectrum, as predicted by diffusive shock acceleration theory. The result suggests that there is only little magnetic field strength evolution downstream to the shock. From the lack of spectral steepening, we find that either the Sunyaev-Zeldovich decrement produced by the pressure jump at the shock along the line of sight is small or the relic is located far behind in the cluster. For the first time, we detect linearly polarized emission from the "brush" at 18.6 GHz. Compared to 8.3 GHz, the degree of polarization across the brush increases at 18.6 GHz, suggesting a strong Faraday depolarization towards lower frequencies. The observed depolarization is consistent with an intervening magnetized screen that arise from the dense ICM containing turbulent magnetic fields. The depolarization, corresponding to a standard deviation of the Rotation Measures as high as $\sigma_{\text{RM}} = 212 \pm 23 \,\text{rad m}^{-2}$, suggesting that the brush is located in or behind the ICM. Our findings indicate that the Toothbrush can be consistently explained by the standard scenario for relic formation.

Keywords: acceleration of particles — galaxies: clusters: individual $(1RXS\,J0603.3+4214)$ — galaxies: clusters: intracluster medium — large-scale structure of universe — magnetic fields

1. INTRODUCTION

Radio relics are large, diffuse sources that are believed to be associated with powerful shock fronts originating in the intracluster medium (ICM) during clusters merger (for a review, see e.g. [Feretti et al.](#page-5-0) [2012;](#page-5-0) [van Weeren](#page-6-0) [et al.](#page-6-0) [2019\)](#page-6-0). One striking observational feature of radio relics is their high degree of polarization. The magnetic field vectors are often found to be well aligned with the shock surface [\(van Weeren et al.](#page-6-1) [2010;](#page-6-1) [Bonafede et al.](#page-5-1) [2012;](#page-5-1) [Owen et al.](#page-6-2) [2014;](#page-6-2) [de Gasperin et al.](#page-5-2) [2014;](#page-5-2) [Kierdorf](#page-6-3) [et al.](#page-6-3) [2017\)](#page-6-3).

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Despite progress in understanding radio relics, the actual acceleration mechanism at the shock fronts is not fully understood. It is generally believed that diffusive shock acceleration (DSA; [Drury](#page-5-3) [1983\)](#page-5-3) generates the observed cosmic ray electrons (CRe). However, it is currently debated if the acceleration starts from the thermal pool (standard scenario; [Ensslin et al.](#page-5-4) [1998;](#page-5-4) [Hoeft](#page-5-5) & Brüggen [2007\)](#page-5-5) or from a population of mildly relativistic electrons (re-acceleration scenario; [Kang & Ryu](#page-5-6) [2011,](#page-5-6) [2016\)](#page-5-7)

The standard scenario has successfully reproduced many of the observed properties of relics, however, three major difficulties remain: (i) the spectra of some relics are reported to show a spectral break above 10 GHz [\(Stroe et al.](#page-6-4) [2016\)](#page-6-4), which is incompatible with the power-law spectrum predicted by DSA theory, (ii) a power-law energy distribution from the thermal pool

Figure 1. Total power emission from the Toothbrush relic at $70''$ resolution. Left: Effelsberg 14.25 GHz image. The largest linear size of the relic is ~ 1.8 Mpc, similar to those reported below 10 GHz. Contour levels are drawn at $\sqrt{[1, 2, 4, 8, ...)}\times 3\sigma_{\rm rms}$, where $\sigma_{\rm rms,14.25\,GHz} = 0.2\,\rm m\,Jy\,beam^{-1}$ and $\sigma_{\rm rms,18.6\,GHz} = 0.4\,\rm m\,Jy\,beam^{-1}$. Right: SRT 18.6 GHz image overlaid with the SRT (gray) and Effelsberg (white) contours. Cyan boxes define the area used for measuring the integrated spectrum of the relic and its sub-regions. The emission at the top right corner in the SRT image is due to blending of discrete sources.

CRe energies relevant for the synchrotron emission may require an unphysical acceleration efficiency [\(van](#page-6-5) [Weeren et al.](#page-6-5) [2016;](#page-6-5) [Botteon et al.](#page-5-8) [2020\)](#page-5-8), and (iii) the Mach numbers derived from X-ray observations are often significantly lower than derived from the overall radio spectrum [\(Akamatsu et al.](#page-5-9) [2012;](#page-5-9) [Botteon et al.](#page-5-8) [2020\)](#page-5-8).

According to the re-acceleration scenario the shock fronts re-accelerate electrons from a pre-existing population of fossil electrons. There are few examples, which seem to show a connection between the relic and active galactic nuclei. [\(Bonafede et al.](#page-5-10) [2014;](#page-5-10) [van Weeren](#page-6-6) [et al.](#page-6-6) [2017;](#page-6-6) [Di Gennaro et al.](#page-5-11) [2018;](#page-5-11) [Stuardi et al.](#page-6-7) [2019\)](#page-6-7). If relics originate according to the re-acceleration scenario, weak shocks may become radio bright, solving issue (ii) and (iii). A break in the radio spectrum is expected at high frequency, when the shock passes through a finite size cloud of fossil electron population [\(Kang &](#page-5-7) [Ryu](#page-5-7) [2016\)](#page-5-7). If the fossil population is homogeneously distributed, also the re-acceleration scenario predicts a power-law spectrum.

The merging galaxy cluster 1RXS J0603.3+4213, located at redshift $z = 0.225$, is one the most intriguing clusters hosting a spectacular toothbrush-shaped relic [\(van Weeren et al.](#page-6-8) [2012,](#page-6-8) [2016;](#page-6-5) [Rajpurohit et al.](#page-6-9) [2018,](#page-6-9) [2020;](#page-6-10) [de Gasperin et al.](#page-5-12) [2020\)](#page-5-12). It consists of three distinct components, namely the brush (B1) and two parts forming the handle (B2+B3). The relic shows an unusual linear morphology and is quite asymmetric with respect to the merger axis. The handle extends into very low density ICM.

[Stroe et al.](#page-6-4) [\(2016\)](#page-6-4) reported evidence for a spectral steepening above 2.5 GHz in the integrated radio spectrum of the relic. This claim was mainly based on the 16 GHz and 30 GHz radio interferometric observations. It has been suggested that the steepening in the integrated radio spectrum can be reproduced with the reacceleration scenario [\(Kang](#page-5-13) [2016\)](#page-5-13). [Basu et al.](#page-5-14) [\(2016\)](#page-5-14) studied the impact of the Sunyaev-Zeldovich (SZ) effect on the observed synchrotron flux density. They suggested that SZ contamination leads to a high frequency steepening for relics, albeit not at the level claimed by [Stroe et al.](#page-6-4) [\(2016\)](#page-6-4). Recently, we studied the integrated spectrum of the relic between 120 MHz to 8 GHz and excluded any steepening up to 8 GHz [\(Rajpurohit et al.](#page-6-10) [2020\)](#page-6-10). However, the spectral behavior of the relic remains uncertain between 10-20 GHz. The Toothbrush is known to be highly polarized [\(van Weeren et al.](#page-6-8) [2012\)](#page-6-8). Effelsberg observations revealed a high fractional polarization at 8.3 GHz and a strong depolarization and Rotation Measure (RM) gradient from the brush to the handle [\(Kierdorf et al.](#page-6-3) [2017\)](#page-6-3).

The main aim of this paper is to answer the question if the overall spectrum of the Toothbrush steepens in the frequency range between 10-20 GHz. If the spectrum steepens at high frequency, this would have a tremendous impact on the radio relic formation scenario, since it would clearly be in conflict with the standard scenario for relic formation, which predicts a power law towards high frequencies. A steepening would be difficult to explain within the standard scenario and would favor the re-acceleration scenario. We adopt a flat ΛCDM cosmology with $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_{\text{m}} = 0.3$, and $\Omega_{\Lambda} = 0.7$. At the cluster's redshift, 1'' corresponds to a physical scale of 3.64 kpc.

2. OBSERVATIONS

The radio observation at 14.25 GHz were performed with the Effelsberg 100-m telescope in January 2020

with the new Ku-band receiver. The data were obtained in dual polarization mode. The total on-source observation time was 20 hours. We obtained 31 coverages of a field of 11×7 arcmin² and processed the data with the NOD3 tool Basket-weaving. The data reduction involves Radio Frequency Interference removal, and baselevel corrections

The Sardinia Radio Telescope (SRT) observations were performed in a full polarization mode with the 7-feed K-Band receiver centered at 18.6 GHz with a bandwidth of 1200 MHz. The observations were carried out between January and February 2020, for a total of 24 hours. The data were reduced using the proprietary software package Single-dish Spectral-polarimetry Software (SCUBE; [Murgia et al.](#page-6-11) [2016\)](#page-6-11).

The uncertainty in the flux density measurements were estimated as:

$$
\Delta S_{\nu} = \sqrt{(f.S_{\nu})^2 + N_{\text{beam}}(\sigma_{\text{rms}})^2},\tag{1}
$$

where f is the absolute flux density calibration uncertainty, S_{ν} is the flux density, $\sigma_{\rm rms}$ is the rms noise and N_{beams} is the number of beams. We assume an absolute flux density uncertainty of 10 % for both SRT and Effelsberg.

3. RESULTS AND DISCUSSION

In Figure [1,](#page-1-0) we show the Effelsberg and the SRT total intensity images at 70''resolution. The relic is clearly detected at both frequencies. The largest linear size of the relic is $\sim 1.8 \text{ Mpc}$, similar to the one reported below 10 GHz. We measure the flux density of $19.9 \pm 3.1 \,\mathrm{mJy}$ and $15.8 \pm 3.5 \,\mathrm{mJy}$ at $14.25 \,\mathrm{GHz}$ and 18.6 GHz, respectively. These values are significantly larger than those reported by [\(Stroe et al.](#page-6-4) [2016\)](#page-6-4), namely $S_{16\,\text{GHz}} = 10.7 \pm 0.8 \,\text{mJy}$. We speculate that the discrepancy between our measurements and the one taken by the Arcminute Microkelvin Imager interferometer is due to the "resolved-out" effects. Interferometric observations underestimate the flux density of extended emission when the size of emission region gets close to Larges Angular Scale detectable with the interferometer.

3.1. Integrated spectrum

To obtain the integrated spectrum of the relic, we combine our new flux density measurements with those presented in [Rajpurohit et al.](#page-6-10) [\(2020\)](#page-6-10). In addition, we include the flux density measurements from the LOFAR LBA observations at 58 MHz [\(de Gasperin et al.](#page-5-12) [2020\)](#page-5-12). We measure a flux density for the entire relic as well as in sub-regions.

The resulting integrated spectra are shown in the left panel of Figure [2.](#page-3-0) We find that the relic follows a close power law over almost three orders of magnitude in frequency. The integrated spectral index of the relic between 58 MHz and 18.6 GHz is -1.16 ± 0.03 . The spectral index value is consistent with our previous estimates [\(Rajpurohit et al.](#page-6-9) [2018,](#page-6-9) [2020\)](#page-6-10). In addition, the

power-law spectrum is in agreement with the high frequency single-dish results found recently for the relic in CIZA J2242.8+5301(Loi et al. submitted). According to the DSA theory in the test-particle regime and CRe cooling in a homogeneous downstream region, the "integrated" spectrum is related to the Mach number according to

$$
\mathcal{M} = \sqrt{\frac{\alpha_{\text{int}} - 1}{\alpha_{\text{int}} + 1}}.
$$
 (2)

The integrated spectral index has to be steeper than −1, the index above corresponds to a Mach number of $M = 3.7 \pm 0.3$.

Despite the fact that the brush is about 4 times brighter than the handle, the entire relic and its subregions follow a power-law behavior and show similar spectral slopes; see Table [1.](#page-3-1) At face value, this implies that the shock strength remains the same over \sim 1.8 Mpc scale. As argued in [Rajpurohit et al.](#page-6-10) [\(2020\)](#page-6-10), the shock surface indeed shows a distribution of Mach numbers, thus a single Mach number derived above can only roughly characterize the shock. Most importantly, the tail of the Mach number distribution towards high values determine the radio spectral index [\(Wittor et al.](#page-6-12) [2019;](#page-6-12) [Rajpurohit et al.](#page-6-10) [2020\)](#page-6-10).

Our finding is consistent with the standard scenario for the formation of radio relics if the radio spectral index corresponds to the Mach number of the shock. If the shock has a strength as estimated from the X-ray surface brightness, the standard scenario would clearly require an unphysical acceleration efficiency [\(van Weeren](#page-6-8) [et al.](#page-6-8) [2012;](#page-6-8) [Botteon et al.](#page-5-8) [2020\)](#page-5-8). If instead the shock strength corresponds to the radio spectrum according to Equation [2,](#page-2-0) a plausible acceleration efficiency below 10 % results in the observed luminosity if the magnetic field strength amounts to at least a few μ G and a large fraction of the shock surface shows the derived Mach number or higher [\(Botteon et al.](#page-5-8) [2020\)](#page-5-8).

3.2. Constraints on the downstream magnetic field evolution

It is conceivable, that the magnetic field strength downstream of the shock increases, e.g., due to a turbulent dynamo process driven by the curvature of the shock front, or decreases, e.g., by expansion of the shock compressed material. Depending on frequency, the observed radio emission probes very different volumes. At the highest frequency, 50% of the emission are emitted from a volume with an extent of about 5 kpc downstream to the shock front. In contrast, the emission at 58 MHz is extended to about 85 kpc. If the strength of the magnetic field would change significantly on these lengths scales, this would affect the integrated spectrum of the relic.

A non-linear change of the field strength would either significantly boost the emission at short or at large distances, in both cases this would result in a curved spectrum, see e.g., [Donnert et al.](#page-5-15) [\(2016\)](#page-5-15). Since integrated

Figure 2. Left: Integrated spectrum of the Toothbrush relic between 58 MHz and 18.6 GHz. Dashed lines show the fitted power laws. The spectrum follows a close power law with a slope of $\alpha = -1.16 \pm 0.03$. The new flux density points are highlighted by the cyan regions, other values are adopted from [Rajpurohit et al.](#page-6-10) [\(2020\)](#page-6-10). Right: The possible impact of SZ decrement (shown with horizontal color lines) as a function of line of sight depth (d_{LOS}) on the radio spectra of the relic emission. Blue circles show the observed flux densities. In order to produce an SZ decrement compatible within the error-bars of the new 14.25 and 18.6 GHz observations, the depth of the shock pressure jump along the line of sight is required to be $d_{\text{LOS}} \leq 200$ kpc.

spectrum follows almost perfectly a power law, only a marginal non-linear increase or decrease of the magnetic field strength seems to be possible on scales probed by the relic.

However, if the field strength changes linearly with distance, the power-law integrated spectrum is preserved but the relation Equation [2](#page-2-0) does not hold anymore. An increasing field strength would steepen the integrated spectrum while a decreasing one would flatten it. If the field strength doubles one a scale of 85 kpc, the spectrum would steepen by about -0.2 (the actual value depends on many parameters as, e.g., the field strength itself). If the relic is formed according the standard scenario, such a steep magnetic field gradient is clearly disfavored by the observations. A decreasing downstream field strength might be consistent with our observations, however, it would significantly aggravate the efficiency problem.

3.3. SZ decrement between 10-20 GHz

The SZ effect contributes a negative signal against the cosmic microwave background for ≤ 220 GHz. In the case of relics, [Basu et al.](#page-5-14) [\(2016\)](#page-5-14) showed that the SZ effect from the shock downstream also scales proportional to the Mach number squared, producing a contamination within exactly the same spatial scales responsible for the relic emission.

At 15 GHz, the SZ effect is expected to reduce the observed synchrotron flux density by $\sim 10-50\%$, and must be taken into account when attempting a physical interpretation in case of any deviation from the power-

Table 1. Integrated flux densities

Region	$S_{58\,\rm MHz}$ Jy	$S_{14.25\,\mathrm{GHz}}$ mJv	$S_{18.6\,\mathrm{GHz}}$ mJy	$\alpha_{\rm 58~MHz}^{\rm 18.6~GHz}$
relic				12.6 ± 2.3 19.9 ± 3.1 15.8 ± 3.5 -1.16 ± 0.03
B1	$9.8 + 1.5$			15.1 ± 2.0 11.9 ± 2.6 -1.17 ± 0.03
$B2 + B3$	2.8 ± 0.5	4.8 ± 0.8	$\overline{}$	-1.15 ± 0.04

NOTE— The flux densities 14.25 and 18.6 GHz are measured from 70" resolution images. The measurement of the relic flux density excludes the contribution from sources F and P.

law spectra. Conversely, since the SZ decrement must be expected if the shock leading to observed relic involve thermal gas, a lack of spectral steepening can be used to further constrain the shock parameters.

The SZ decrement at a given observation frequency depends on the line-of-sight projection of the pressure jump, d_{LOS} , and therefore on the (unknown) shock geometry at the location of the relic. For a simple planeparallel geometry and ignoring curvature, the total SZ decrement can be obtained by integrating y over the visible relic area: $L \times W$, where L is the shock length and W is the width, leading to an angular size of the relic $\Omega_{\text{relic}} \approx L \mathcal{W} / D_A^2$ steradians (with D_A the angular diameter distance). Following [Basu et al.](#page-5-14) [\(2016\)](#page-5-14), we calculate the maximum total allowed SZ flux decrement

from the region sampled by our new high frequency radio observation of the Toothbrush:

$$
\begin{split} & \mid \Delta S^{\rm SZ}_{\nu, \rm relic} \vert \leq 0.26 \, \mu \rm Jy \left(\frac{D_A}{700 \, \rm Mpc}\right)^{-2} \left(\frac{L}{1 \rm Mpc}\right) \left(\frac{d_{\rm LOS}}{1 \rm Mpc}\right) \\ & \times \left(\frac{\mathcal{W}}{100 \, \rm kpc}\right) \left(\frac{n_{\rm u} T_{\rm u}}{10^{-4} \rm keV cm^{-3}}\right) \ \left(\frac{\mathcal{M}}{3.7}\right)^2 \left(\frac{\nu}{1.4 \ \rm GHz}\right)^2 (3) \end{split}
$$

We use $D_A = 751$ Mpc, $L = 1.86$ Mpc, $W=1277$ kpc, and two possible shock strengths, either $\mathcal{M} = 3.7$ (as suggested by radio observations) or $\mathcal{M} = 1.3$ (as suggested by X-ray analysis, see [Ogrean et al.](#page-6-13) [\(2013\)](#page-6-13); [van Weeren et al.](#page-6-5) [\(2016\)](#page-6-5)). n_u and T_u are the pre-shock density and temperature that can be derived by the two Mach numbers, respectively. For each Mach number, the temperature and density are derived from the standard Rankine-Hugoniot jump conditions based on the assumed post-shock values, $n_d = 3 \times 10^{-3} \text{ cm}^{-3}$ and $T_d = 6$ keV [\(van Weeren et al.](#page-6-5) [2016\)](#page-6-5).

We thus produce estimates of $|\Delta S_{\nu,\text{relic}}^{\text{SZ}}|$ for different frequencies, by fixing the above model parameters and varying the unknown value of d_{LOS} . Our results are given in the right panel of Figure [2.](#page-3-0) In order to produce an SZ decrement compatible within the error-bars of our 14.25 and 18.6 GHz observations, the depth of the shock pressure jump along the line of sight is required to be $d_{\text{LOS}} \leq 200$ kpc for a shock of strength $\mathcal{M} = 3.7$. For a shock of strength $\mathcal{M} = 1.3$, the SZ decrement at $d_{\text{LOS}} = 200$ kpc already produces a spectrum as low as the error-bars of our observations. Hence, requiring an even smaller depth of the shock along the line of sight. We emphasize that the quoted values only refers to the contribution to the SZ decrement from the shock discontinuity along the line of sight, for the same range of spatial scales responsible for the radio emission.

Furthermore, the assumption of a simple planar geometry and the absence of curvature along the line of sight is clearly an oversimplification, which may indeed explain the surprisingly low value of d_{LOS} . Incidentally, such a small SZ decrement may also be explained if the shock responsible for the relic is at a more peripheral location in the cluster. In this case the density and temperature values suggested by X-ray observations originate from regions which are denser than the one responsible for the radio emission. In this case, Equatio[n3](#page-4-0) would significantly overestimate the pressure jump at the shock, and the requirement on d_{LOS} would be relaxed.

3.4. Polarization at 18.6 GHz

All of the information on the polarization properties of relics are mainly collected in the frequency range of 1-8.3 GHz. Since the Faraday rotation is expected to be almost negligible at 18.6 GHz, the intrinsic polarization of the relic could be directly mapped by our observations.

17 $16[°]$ $6^{h}03^{m}24$ $\overline{18}$ $\overline{12}$ $\overline{06^s}$ Right Ascension (J2000) Figure 3. B-vectors distribution across the brush region at 51["] resolution overlaid with the SRT total power contours at 3σ . The length of the vectors depict the degree of polarization. The vectors are corrected for Faraday rotation effect.

For the first time, we detect polarized emission from the relic at 18.6 GHz. We detect polarized emission mainly from the brush region; see Figure [3.](#page-4-1) The degree of polarization varies along the brush and the magnetic field vectors are mainly aligned to the relic orientation. The fractional polarization reaches ∼ 66% in some areas, the average being $\sim 30 \pm 7\%$. We note that these values could be affected by beam depolarization.

The mean polarization fraction at the brush is $(30 \pm 7)\%$.

Previous polarization measurements of the toothbrush relic have shown that the fractional polarization of B1 decreases rapidly towards lower frequencies. B1 is polarized at a level of about 15% at 8.3 GHz [\(Kierdorf et al.](#page-6-3) 2017) and about 11% at 4.9 GHz. The polarization fraction drops below 1% at frequency near 1.4 GHz [\(van](#page-6-8) [Weeren et al.](#page-6-8) [2012\)](#page-6-8). The comparison between 8.3 GHz and our measurement suggests significant depolarization even between 18.6 and 8.3 GHz. Other than the Toothbrush relic, the polarization observations above 4.9 GHz are available only for three relics, namely the Sausage relic, the relic in ZwCl 0008+52, and Abell 1612 [\(Kier](#page-6-3)[dorf et al.](#page-6-3) [2017;](#page-6-3) [Loi et al.](#page-6-14) [2017\)](#page-6-14). For the above mentioned relics, the fractional polarization remains nearly constant at 4.9 GHz and 8.3 GHz.

The standard deviation of the RM, σ_{RM} , is a useful parameter to characterize Faraday rotation and depolarization caused by an external Faraday screen. The depolarization induced by an external Faraday screen containing turbulent magnetic fields [\(Burn](#page-5-16) [1966;](#page-5-16) [Sokoloff](#page-6-15) [et al.](#page-6-15) [1998\)](#page-6-15) can be described as

$$
p(\lambda) = p_0 e^{-2\sigma_{\rm RM}^2 \lambda^4},\tag{4}
$$

where p_0 is the intrinsic polarization fraction. The maps between 4.9 and 18.6 GHz show depolarization of

.

 $DP_{4.9}^{18.6} = 0.36 \pm 0.07$ for B1. This enable us to derive $\sigma_{\text{RM}} = 212 \pm 23 \,\text{rad}\,\text{m}^{-2}$. The observed σ_{RM} for the brush of Toothbrush is several times higher than for any other radio relic. This indicates that the brush region of the relic experiences strong Faraday rotation from the dense ICM. The strong depolarization suggests that the emission lies in or behind the ICM, which is very likely causing a low Mach number shock detected via X-ray observations [\(Ogrean et al.](#page-6-13) [2013;](#page-6-13) [van Weeren et al.](#page-6-5) [2016\)](#page-6-5)

4. CONCLUSIONS

We presented high frequency radio observations of the Toothbrush relic with the SRT and the Effelsberg telescope. We find that the relic follows a close power-law spectrum between 58 MHz to 18.6 GHz, with a slope of $\alpha = -1.16 \pm 0.03$. Our findings indicate that the Toothbrush can be consistently explained by the standard scenario for relic formation. The slope of the spectrum disfavors that the strength of the magnetic field significantly changes on scales probed by the radio emission, i.e., about 85 kpc.

We detected polarized emission at 18.6 GHz. Compared to measurements at lower frequencies, the polarization fraction of the brush increases at 18.6 GHz. The high value of $\sigma_{\rm RM}$ is consistent with $\sigma_{\rm RM}$ fluctuations of an ICM screen with tangled magnetic fields. This suggests that the brush is located in or behind the ICM.

From the lack of steepening in the relic spectra, we find that either that the SZ decrement at the shock along the line of sight is small (i.e., the shock surface $is < 200$ kpc thick along the line of sight), or the pressure jump associated with the relic is located far behind

in the cluster. The latter explanation can also be reconciled with the trends of polarization fraction for the brush region.

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