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Geometric phases in soft materials

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The cover shows a domain between order and disorder. According to Daoist philosophy, happiness lays at the border between yin and yang, or order and chaos. A topological mode ought to stay at this border, even when it faces perturbations in the boundary between the domains.

To my family and Hamraz

Contents

1	Introduction	1
1.1	Adiabatic theorem and the Berry phase	3
1.1.1	Topology and geometric phases	4
1.2	Geometric phases in classical systems	6
1.3	This thesis	9
2	Sonic Landau levels and synthetic gauge fields in mechanical metamaterials	13
2.1	Mechanical graphene	14
2.2	Synthetic gauge field	17
2.3	Mechanical Landau levels	19
2.4	Sublattice-polarized domain wall modes	21
2.4.1	Connection to the Jackiw-Rebbi model	23
2.4.2	Topological robustness of the domain-wall mode	23
2.5	Selective enhancement	28
2.6	Towards mechanical lasers	31
2.7	Conclusion	32
3	Photonic waveguides in liquid crystals	33
3.1	Paraxial light propagation in uniaxial media	35
3.1.1	Large birefringent medium: interaction picture	36
3.2	Guiding regimes for light in a uniaxial medium	38
3.3	Curved waveguides	41
3.4	Fully rotating nematic waveguides	43
3.5	Appendix	46
3.5.1	Dynamics of circularly polarized waves through a uniform uniaxial medium	46
3.5.2	Dynamics of paraxial light propagation in liquid crystals with medium to low birefringence	48

3.5.3	Floquet theory for a periodically driven system	50
4	Liquid-crystal-based photonic topological insulators	55
4.1	Coupled liquid crystal waveguides	56
4.2	Photonic crystals in 1+1d: SSH chain	58
4.3	Symmetries and topological modes in 2+1d	60
4.4	Non-Hermitian description of shifted waveguides	64
4.5	Conclusion	66
4.6	Appendix	67
4.6.1	Liquid crystal configuration	67
4.6.2	Floquet tight-binding model	68
4.6.3	Time-reversal symmetry	69
4.6.4	Why is C_3 -symmetry breaking needed?	73
5	Edge modes in rotating Rayleigh-Bénard systems	77
5.1	Model equations	80
5.1.1	Symmetries of the Rayleigh-Bénard system	81
5.1.2	Simulations of the generalized Swift-Hohenberg equations	83
5.2	Linear dispersion relation	83
5.2.1	Fourier response and edge modes in 1d Swift-Hohenberg model	85
5.3	Nonlinear amplitude equations and system's discretization	88
5.4	Band structure and topology of nonlinear systems	90
5.5	Discussion and outlook	92
5.6	Appendix	93
5.6.1	Band structure of nonlinear Schrödinger/Gross-Pitaevskii equations	93
5.6.2	A nonlinear SSH chain	95
	References	97
	Summary	117
	Samenvatting	119
	List of publications	121
	Curriculum vitae	123

Contents

iii

Acknowledgments 125

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