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## Geometric phases in soft materials

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# **GEOMETRIC PHASES IN SOFT MATERIALS**

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The cover shows a domain between order and disorder. According to Daoist philosophy, happiness lays at the border between yin and yang, or order and chaos. A topological mode ought to stay at this border, even when it faces perturbations in the boundary between the domains.

*To my family and Hamraz*

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