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## **Constraint-based analysis of business process models**

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### **Citation**

Changizi, B. (2020, February 21). *Constraint-based analysis of business process models*. IPA Dissertation Series. Retrieved from <https://hdl.handle.net/1887/85677>

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**Author:** Changizi, B.

**Title:** Constraint-based analysis of business process models

**Issue Date:** 2020-02-25

# Constraint-Based Analysis of Business Process Models

**Proefschrift**

te verkrijging van  
de graad van Doctor aan Universiteit Leiden,  
op gezag van Rector Magnificus Prof. Mr. C.J.J.M. Stolker,  
volgens besluit van het College voor Promoties  
te verdedigen 25 February 2020  
klokke 13:45

door

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The work in this thesis has been carried out at Centrum Wiskunde & Informatica and Leiden University, and under the auspices of the research school IPA: Institute for Programming research and Algorithmics. The research was partially funded by the EU project EU FP7 IST project COMPAS: Compliance-driven Models, Languages, and Architectures for Services.

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