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Unraveling temporal processes using probabilistic graphical models

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Unraveling Temporal Processes using Probabilistic Graphical Models

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