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## Multi-objective mixed-integer evolutionary algorithms for building spatial design

Blom, K. van der

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# **Multi-Objective Mixed-Integer Evolutionary Algorithms for Building Spatial Design**

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