Loop extrusion drives very different dynamics for Rouse chains in bulk solutions and at interfaces

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Abstract – The loop extrusion theory predicts that the loops of chromosomes are produced by cohesin molecules that uni-directionally extrude a chromatin fiber. We here use an extension of the Rouse model to predict the chain conformational dynamics driven by the loop extrusion process. Our theory predicts that in a bulk solution, the mean square distance between the starting and ending sites of the loop extrusion process decreases with a constant rate. This is because the tension generated by the loop extrusion process drives the displacement of the starting site towards the ending site. In contrast, when the cohesin is entrapped at an interface, the mean square distance does not decrease until the tension generated by the loop extrusion process arrives at the ending site. This theory highlights the fact that the chain dynamics strongly depends on the mobility of the chain segments bound by cohesin.

Introduction. – In the interphase, chromosomes are 1 composed of so-called topologically associated domains 2 (TADs), contiguous regions of enriched contact frequency 3 that are isolated from neighboring regions [1, 2]. In many cases, there are peaks of contact frequency at the bound-5 aries of TADs, implying that TADs are loops of chromatin 6 fiber [3]. Recent theory predicts that the chromatin loops are produced by the loop extrusion process, with which 8 cohesin, a ring-shaped protein complex, uni-directionally 9 extrudes the chromatin fiber until it collides with a pro-10 tein factor, called CTCF (CCCTC-binding factor) [4,5]. 11 CTCF proteins at the boundary of TADs are oriented to-12 wards the interior of the domains [3]. Indeed, most loops 13 are lost when the loading of cohesin to chromosomes is 14 suppressed [6]. The loop extrusion theory captures the 15 features of TADs for a window of parameters [4, 5]. 16

Typically, to start transcription (that is the process to 17 synthesize messenger RNA), the binding of two distant 18 19 DNA sequences, such as promoters and enhancers, are necessary. The binding rate of these sequences are governed 20 by the chain conformational dynamics of the chromatin 21

fiber between the sequences [7, 8]. How does the loop extrusion process modulate the chain dynamics? Simulation 23 models of chromatin fibers, on which cohesin drives a loop extrusion process, were constructed to predict the contact frequency map [4, 5]. An analytical theory by using a simple model may be useful to understand the feature of the chain dynamics that is driven by the loop extrusion process.

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Many of the simulations treat chromatin fibers in a uni-30 form solution [4, 5]. However, recent experiments have 31 shown that droplets of the condensate of transcriptional 32 activators and coactivators are stabilized by phase separa-33 tion and superenhancers, DNA regions condensed with en-34 hancer sequences, are associated with the droplets [9, 10]. 35 Other regions tend to be excluded from the droplets [11]. 36 These experiments imply that chromatin stabilizes a struc-37 ture analogous to microemulsions and cohesin may ex-38 trude chromatin at the surface of the droplets. Recent 39 simulations of the loop extrusion process on chromosomes 40 that show microphase separation did not emphasize the 41 difference of the dynamics between chains in the bulk and 42



Fig. 1: Chains in a bulk solution (a) and at an interface (b). Cohesin (the green hoop) is loaded on the chain and drives the loop extrusion process. In the bulk solution, all the chain segments are freely mobile, whereas at the interface, the chain segment occupied by the cohesin is trapped at the interface because this cohesin binds the two segments that favor different environments. We set the z-direction to be the normal to the interface.

those at an interface [12]. It is thus of interest to theoretically predict the chain dynamics of chromatin in the bulk
and at an interface.

We here use an extension of the Rouse model to predict 46 the mean square of the distance between the starting and 47 ending sites of the loop extrusion process, when a cohesin 48 is loaded on the starting site at t = 0. Our theory pre-49 dicts that in the bulk solution, the mean square distance 50 decreases with constant rate as soon as the cohesin starts 51 the loop extrusion process. This reflects the fact that the 52 loop extrusion process stretches the chain and generates 53 the elastic force that displaces the starting site towards the 54 ending site. In contrast, at an interface, the mean square 55 distance does not change until the tension generated by 56 the loop extrusion process arrives at the chain end. This 57 happens because the starting site, which is embraced by 58 cohesin, cannot escape from the interface and the mean 59 square distance thus does not change until the ending site 60 moves towards the starting site. 61

Model. – We treat the dynamics of a very long chain 62 in a bulk solution and at an interface, see fig. 1. We use 63 the bead-spring model [13] that treats the chain as beads 64 that are linearly connected by springs, see fig. 2. The 65 chain has a region, composed of N beads, that is delin-66 eated by two CTCF molecules (of the converging orienta-67 tions [3]). Cohesin is loaded on the chain from a site in 68 the vicinity of a CTCF molecule, where a cohesin loader, 69 Nipbl, is localized. The cohesin then starts extruding the 70 chain with a constant rate $\tau_{\rm c}^{-1}$ until it reaches the other 71 CTCF site. The cohesin embraces two beads - one is 72 the bead at the starting site and another changes as the 73 cohesin extrudes the chain. At each extrusion process, 74 cohesin pulls the chain so that the bead at the nearest 75 neighbor displaces to the position of the cohesin, while 76 77 the cohesin keeps embracing the starting site, see fig. 2. The asymmetric extrusion has been observed by single 78 molecule techniques for condensin [14, 15], whose struc-79



Fig. 2: We use the bead and spring model to treat the dynamics of the chain. A cohesin (shown by the green bar) is loaded on the chain from a site (S) and embraces the starting site and the *m*-th site (C). At each extrusion process, the cohesin applies forces to capture the bead at the nearest neighbor. The cohesin operates the loop extrusion process with a constant rate τ_c^{-1} until it reaches the ending site (E).

ture is analogous to cohesin, and it is also implied from Hi-C experiments [16]. We predict the mean square of the distance between the starting and ending sites of the loop extrusion process when a cohesin is loaded on the chain at t = 0, assuming that the chain is in the equilibrium for t < 0.

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The chain at the interface is composed of two types of 86 blocks, one tends to be associated with the droplet and 87 one is excluded from the droplet. Although the genomic 88 position of the starting site may depend on experimental 89 systems, cohesin may eventually arrive at the boundary 90 between the two blocks. Because cohesin embraces the 91 beads of different type, it is entrapped at the interface, 92 analogous to surfactants. To highlight the role played by 93 the interface in the dynamics of the chain, we treat the 94 case in which the starting site is at the boundary between 95 the two types of blocks. In the bulk solution, the system 96 is isotropic and thus it is enough to treat the dynamics of 97 the beads in one direction, see fig. 1a. At the interface, 98 the bead that is bound by the cohesin does not move in 99 the normal to the interface (the z-direction); the charac-100 teristics of the interface is manifested in the dynamics of 101 the chain in the z-direction, see fig. 1b. In the following, 102 we thus treat the dynamics of the beads in the z-direction. 103

We use an extension of the Rouse model [13] to treat the dynamics of the chain. The Rouse model takes into account the connectivity of the chain, but neglects the hydrodynamic interactions and excluded volume interactions between chain segments. With this model, the position $z_n(t)$ of the *n*-th bead in the chain is derived by using the force balance equation

$$\zeta \frac{\partial}{\partial t} z_n(t) = k \frac{\partial^2}{\partial n^2} z_n(t) + F_m(t) \delta_{nm} + f_n(t), \qquad (1)$$

where $n (= 1, 2, \dots, N)$ counts the beads from the starting site to the ending site. The left side of eq. (1) is the friction force between the bead and the solvent. The first term of the right side is the elastic force generated by the springs that are connected to the bead. The second term is the force generated by the loop extrusion process when the cohesin is at the *m*-th bead ($\delta_{mn} = 1$ if m = n and

0 otherwise). The third term is the force caused by the 118 random collisions of solvent molecules with the bead. ζ is 119 the friction constant of the bead and $k (= 3k_{\rm B}T/b^2)$ is the 120 spring constant of the springs that connect the beads $(k_{\rm B})$ 121 is the Boltzmann constant, T is the absolute temperature, 122 and b is the Kuhn length). $f_n(t)$ is the Gaussian random 123 force with $\langle f_n(t) \rangle = 0$ and $\langle f_m(t) f_n(t') \rangle = 2\zeta k_{\rm B} T \delta_{mn} \delta(t - t)$ 124 t'). The form of the force $F_m(t)$ due to the loop extrusion 125 process is shown later, see eqs. (6) and (7). Eq. (1)126 predicts that the relaxation time of a chain composed of 127 N segments is the Rouse time [13] defined by 128

$$\tau_N = \frac{N^2 \zeta}{\pi^2 k}.\tag{2}$$

The Green function of eq. (1) is defined by the solution of the equation [17]

$$\frac{\partial}{\partial t}G(n,m,t) = \frac{k}{\zeta}\frac{\partial^2}{\partial n^2}G(n,m,t) + \delta_{mn}\delta(t).$$
 (3)

¹³¹ The solution of eq. (3) has the form

$$G(n,m,t) = \left(\frac{\zeta}{4\pi kt}\right)^{1/2} e^{-\zeta(n-m)^2/(4kt)}$$
(4)

for an infinitely long chain. The solution of eq. (1) thus
has the form

$$z_n(t) = z_n(0) + \frac{1}{\zeta} \int_0^t dt' \, G(n, m, t - t') F_m(t') + r_n(t), \quad (5)$$

where $r_n(t)$ is the displacement due to the random force. In the following, we neglect the displacement $r_n(t)$ for simplicity. Eq. (5) implies that the *n*-th bead is not affected by the force $F_m(t)$ until the tension, generated by the force $F_m(t)$, diffuses to this bead.

¹³⁹ Eq. (5) predicts that in the bulk solution, the force ¹⁴⁰ $F_m(t)$ that is necessary to displace the *m*-th bead by u_m ¹⁴¹ during the loop extrusion process has the form

$$F_m(t) = \frac{\zeta u_m}{\sqrt{\pi}} \sqrt{\frac{r\tau_c}{\tau_1}} \delta(t), \qquad (6)$$

where r is the duty ratio of cohesin and τ_1 is the monomer 142 relaxation time, see eq. (2) with N = 1. Eq. (6) is an 143 asymptotic form of the extrusion force for $t > r\tau_c$. Eq. (6) 144 is derived by assuming that cohesin generates a constant 145 force on the *m*-th bead only during the time $r\tau_{\rm c}$ and that 146 the force displaces the bead by a distance u_m , see the first 147 paragraph of sec. S3 in the Supplementary Material. The 148 bead is freely mobile for $t > r\tau_c$, reflecting the fact that 149 the bead is in the bulk solution. At the interface, the force 150 $F_m(t)$ has the form 151

$$F_m(t) = \frac{1}{\pi^{3/2}} \frac{1}{\sqrt{\tau_1}} \frac{\zeta u_m}{\sqrt{t}}.$$
 (7)

Eq. (7) is the force to displace the *m*-th bead by a distance u_m and keep the bead at the position for time t,

see the first and second paragraphs of sec. S2 in the Supplementary Material for the derivation. The interface is introduced in the boundary condition, with which cohesin and the bead occupied by the cohesin are entrapped at z = 0 until the cohesin extrudes the next bead.

By using eqs. (5), (6), and $u_m = z_{m-1}(m\tau_c) - z_m(m\tau_c)$, ¹⁵⁹ the position $z_n(t)$ of the *n*-th bead at time $t (m\tau_c < t < \frac{160}{(m+1)\tau_c})$ is derived in the form ¹⁶¹

$$z_{n}(t) - z_{n}(0) = -\sum_{l=2}^{m} (z_{l}(l\tau_{c}) - z_{l-1}(l\tau_{c})) \times K(n, l, t - l\tau_{c}),$$
(8)

with the function $K(n,m,t) = \sqrt{\frac{\tau\tau_c}{\pi\tau_1}}G(n,m,t)$ for the bulk solution, see sec. S3 in the Supplementary Material for the derivation. The form of the position $z_n(t)$ for for the interface is derived by using $z_{l-1}(l\tau_c) = 0$ and $K(n,m,t) = \operatorname{erfc}(\frac{\pi(n-m)\sqrt{\tau_1}}{2\sqrt{t}})$ to eq. (8) (erfc(x) = $\frac{2}{\sqrt{\pi}} \int_x^{\infty} dt \, e^{-t^2}$ is the complementary error function), see sec. S2 in the Supplementary Material for the derivation. By using eq. (8), one derives the relationship

$$z_m(m\tau_c) - z_{m-1}(m\tau_c) = \sum_{l=1}^m \Gamma_{ml}(z_l(0) - z_{l-1}(0)), \quad (9)$$

where Γ_{mn} is the solution of the equation

$$\Gamma_{mn} = \delta_{mn} - \sum_{l=n}^{m-1} \Gamma_{ln} \left[K(m, l, (m-l)\tau_{c}) - K(m-1, l, (m-l)\tau_{c}) \right].$$
(10)

The position $z_n(t)$ is derived as a function of the positions $z_l(0)$ $(l = 1, 2, \dots, n)$ of the beads at t = 0 by substituting eq. (9) into eq. (8).

The mean square distance $\langle P^2(t) \rangle$ between the starting and ending sites 174

$$\langle P^2(t)\rangle = \langle (z_N(t) - z_{m=t/\tau_c}(t))^2 \rangle \tag{11}$$

is derived by using the initial condition, with which the 176 chain is ideal for t = 0 ($\langle \rangle$ is the average with respect to 177 the initial positions of the beads). Indeed, at the inter-178 face, the initial distribution of the beads is not Gaussian 179 because the beads of the chain are not distributed equally 180 to the two domains [18]. However, we here use the Gaus-181 sian beads distribution for both in the bulk and at the 182 interface to highlight the roles played by the entrapment 183 of the beads to the dynamics of the chain. 184

Results. – The mean square distance $\langle P^2(t) \rangle$ is a ¹⁸⁵ function of the number N of beads in the looping region ¹⁸⁶ and the ratio of the time scales that is defined by ¹⁸⁷

$$\alpha = \frac{\tau_N}{\tau_{\rm ex}},\tag{12}$$

where $\tau_{\rm ex}$ (= $N\tau_{\rm c}$) is the time scale of the loop extrusion process.

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Fig. 3: The mean square distance $\langle P^2(t) \rangle$ between the starting and ending sites of the loop extrusion process (rescaled by the equilibrium value) is shown as a function of time t (rescaled by the time scale $\tau_{\rm ex}$ of loop extrusion) for $\alpha = 0.1$ (cyan), 1.0 (black), and 5.0 (magenta) (α is defined by eq. (12)) when the chain is in a bulk solution. The broken curves are the local equilibrium values. These curves are derived by numerically calculating eq. (10). We used N = 50 and r = 0.5 for the calculations.

Our theory predicts that in the bulk solution, the mean 190 square distance $\langle P^2(t) \rangle$ decreases approximately with a 19 constant rate, as soon as the cohesin starts the loop ex-192 trusion process. This is because the loop extrusion process 193 stretches the chain region between the site embraced by 194 cohesin and the ending site, and the elastic force generated 195 by this process displaces the starting site towards the end-196 ing site, see fig. 2. In the first approximation, the mean 197 square distance is thus the local equilibrium value, 198

$$\frac{3\langle P^2(t)\rangle}{Nb^2} \simeq 1 - \frac{t}{\tau_{\rm ex}}.$$
 (13)

The mean square distance is indeed slightly larger than 199 the local equilibrium value because the chain is stretched 200 by the loop extrusion process, see fig. 3. The deviation 201 $\langle \delta P^2(t) \rangle$ from the local equilibrium value increases with 202 time until the tension generated by the loop extrusion 203 process arrives at the ending site, see fig. 4. The time 204 at which the tension arrives at the ending site decreases 205 with increasing the ratio α . It is because the distance by 206 which the tension propagates scales as $t^{1/2}$ and the dis-207 tance by which the cohesin extrudes as t. The deviation 208 $\langle \delta P^2(t) \rangle$ has an asymptotic form 209

$$\frac{3\langle\delta P^2(t)\rangle}{Nb^2} = -\frac{r}{2\pi\alpha\beta} \left(1 - e^{2N\beta t/\tau_{\rm ex}}\right) \times \left(1 - e^{-(\pi^2\alpha + N\beta)(1 - t/\tau_{\rm ex})}\right)^2 \quad (14)$$

²¹⁰ for large values of the ratio α (with $\beta = \log(\sqrt{r}/2)$).

At the interface, the mean square distance $\langle P^2(t) \rangle$ does not change when the cohesin starts the loop extrusion



Fig. 4: The deviation $\langle \delta P^2(t) \rangle$ of the mean square distance from the local equilibrium value (the difference between the broken curve and the curves of corresponding color in fig. 3) is shown as a function of time t (rescaled by the time scale $\tau_{\rm ex}$ of the loop extrusion process) for $\alpha = 0.1$ (cyan), 1.0 (black), and 5.0 (magenta), where α is defined by eq. (12). These curves are derived by numerically calculating eq. (10). We used r = 0.5and N = 50 for the calculations.

process, see fig. 5. This is because the starting site is entrapped at the interface and thus the mean square distance $\langle P^2(t) \rangle$ does not change until the tension generated by the loop extrusion arrives at the ending site. The time at which the tension arrives at the ending site decreases with increasing the ratio α . For large values of α , the mean square distance $\langle P^2(t) \rangle$ has an asymptotic form

$$\frac{3\langle P^2(t)\rangle}{Nb^2} = 1 - \frac{4}{\pi^2} \frac{N}{\alpha} \left(2\frac{t}{\tau_{\rm ex}} - 1\right) e^{-\pi^2 \alpha (1 - t/\tau_{\rm ex})}$$
(15)

for $t/\tau_{\rm ex} > 1/2$ and $\frac{3\langle P^2(t) \rangle}{Nb^2} = 1$ for $t/\tau_{\rm ex} < 1/2$. For 220 small values of α , the mean square distance asymptotically 221 approaches the local equilibrium value, see eq. (13). 222

Discussion. – We used an extension of the Rouse 223 model to predict the dynamics of a chain in the bulk so-224 lution and at an interface, when the chain is extruded by 225 cohesin with a constant rate. This system has two charac-226 teristic features -i) the bead to which forces are applied 227 changes as a function of time and ii) the displacement of 228 the beads due to the loop extrusion process depends on the 229 history of the chain dynamics. The first feature is shared 230 by the problem of polymer translocation through a small 231 pore in a membrane. A scaling theory predicts that the 232 end of the polymer is not influenced by the force applied 233 at the pore until the tension arrives at the end [19, 20], 234 analogous to the loop extrusion at the interface. When 235 the ratio α of the time scale is large, the motion of the 236 cohesin is faster than the diffusion of the tension gener-237 ated at the starting site. The stretching of the chain is 238 amplified as the cohesin extrudes the loop. This second 239

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Fig. 5: The mean square distance $\langle P^2(t) \rangle$ between the starting and ending sites (rescaled by the equilibrium value) is shown as a function of time t (rescaled by the time scale of loop extrusion $\tau_{\rm ex}$) for $\alpha = 0.1$ (cyan), 1.0 (black), and 5.0 (magenta). These curves are derived by numerically calculating eq. (10). We used N = 50 for the calculations.

feature is taken into account in the recursion relationship,
eq. (10).

Our theory predicts that the mean square distance be-242 tween the starting and ending sites of a chain decreases ap-243 proximately with a constant rate in the bulk. In contrast, 244 at an interface, the mean square distance does not change 245 until the tension generated by the loop extrusion process 246 diffuses to the ending site. The difference of the mean 247 square distance between the chains in the bulk and those 248 at an interface increases with increasing the rate of the 249 loop extrusion process. Recent simulations showed that 250 the size of the extruded loops decreases with increasing 251 the rate of the loop extrusion process [12]. These features 252 reflect the non-equilibrium nature of this process. 253

In our theory, we have used a couple of assumptions: i) 254 we model the chromatin fiber as a Rouse chain that does 255 not take into account the hydrodynamic interactions and 256 excluded volume interactions between the chain segments, 257 ii) we neglected the tension propagation along the loop, 258 which may be significant for the case of the loop extrusion 259 in the bulk solution, iii) cohesin extrudes the chain with 260 a constant rate, iv) the surface tension is large enough so 261 that the shape of the interface is not perturbed by the 262 loop extrusion process, v) cohesin is loaded at t = 0 onto 263 the chain which is at that point in equilibrium, and vi) the 264 displacement due to the random force is omitted by preav-265 eraging eq. (5). These assumptions are useful to simplify 266 the model to highlight the roles played by the entropic 267 elasticity of the chain and the fact that the chain dynam-268 ics significantly depends on the mobility of the bead that 269 is embraced by cohesin. We could even derive the analyt-270 ical form of the mean square distance for large values of 271 α , see eqs. (14) and (15). An extension of our theory may 272 be useful to study more biologically (and experimentally) 273 relevant problems, such as the dynamics of the promoter-274

enhancer binding and the steady state conformation of chromatin at larger scales.

Because of its simplicity, our theory may be better 277 tested by an *in vitro* experiments. In contrast to cohesin, 278 condensin was shown to act as a molecular motor that ex-279 trudes DNA loops [14,15]. The Rouse model is (thought to 280 be) effective to treat the dynamics of a chain in a concen-281 trated solution (in which the excluded volume interactions 282 and the hydrodynamic interactions are screened) on long 283 time and length scales [13]. Our theory is thus best tested 284 by an experiment that measures the end-to-end distance 285 (or the radius of gyration) of DNA in a concentrated solu-286 tion. Taking into account hydrodynamic interactions in an 287 extension of our theory treats the loop extrusion of DNA 288 in a dilute solution. A scaling theory predicts that hydro-289 dynamic interactions (and excluded volume interactions) 290 only change the scaling exponent of the dynamics of ten-291 sion propagation [21]. This implies that the dynamics of 292 DNA in the bulk solution is very different from that at the 293 interface even when hydrodynamic interactions (and/or 294 excluded volume interactions) are significant. However, it 295 is of interest to theoretically predict how such long-range 296 interactions change our results. 297

Recent single molecule experiments indicated that co-298 hesin may not show uni-directional motion [22–24]. One 299 experiment suggests that the cohesin ring is not large 300 enough to accomodate two chromatin fibers and thus co-301 hesin molecules have to form dimers to produce a chro-302 matin loop [22]. We have proposed the osmotic mechanism 303 with which the uni-directional motion of cohesin dimers is 304 driven by the osmotic pressure that is generated by cohesin 305 monomers [25]. Marenduzzo and coworkers proposed a 306 similar mechanism, but only with cohesin dimers [26]. The 307 dynamics of a chain extruded by an osmotic mechanism 308 is different from the dynamics of a chain extruded by a 309 motor mechanism in the following points: First, the ex-310 trusion rate is a function of time. It also depends on the 311 loading rate of cohesin monomers (and dimers). The dy-312 namics of the chain also influences the dynamics of cohesin 313 dimers. Second, the time scale of the loop extrusion pro-314 cess scales as N^2/D_c , where D_c is the diffusion constant 315 of cohesin monomers/dimers. Third, when the motion of 316 the two units of a cohesin dimer is completely random, 317 these units may move in the same direction, relative to the 318 starting site. In this case, the dimer does not decrease the 319 average square end-to-end distance significantly. When 320 each unit of a dimer can move in each side of the start-321 ing site, dimers decrease the average square end-to-end 322 vector significantly. However, the maximum number of 323 dimers that are loaded on the chain is limited by the dis-324 tance between the starting site and the domain boundary 325 due to the excluded volume interactions between cohesin 326 monomers/dimers. The uni-directional motion of cohesin 327 may be driven by RNA polymerase (or other motors) that 328 pushes cohesin during transcription [27]. Our theory is ef-329 fective for the case in which these motors push cohesin all 330 the way along the domain. When a domain is composed 331

of multiple transcription units, the dynamics of a cohesin
molecule switches between thermal motion and episodes
of uni-directional motion caused by transcription.

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