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Into the darkness : forging a stable path through the gravitational landscape

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The cover shows a greyscale image of a dock, with colours inverted. The unknown surroundings represent the vast gravitational landscape while the dock stands for the path of stable models within the landscape. The unfinished state of the path signifies the fact that our understanding of the set of stable gravitational models is still a work in progress.

The original image was made by Hoach Le Dinh and taken from the free license image repository unsplash.com.

In memory of Gonzalo

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