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## Spin-momentum locking in oxide interfaces and in Weyl semimetals

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# **Spin-momentum locking in oxide interfaces and in Weyl semimetals**

PROEFSCHRIFT

TER VERKRIJGING VAN  
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Nicandro Bovenzi

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On the cover: schematic illustration of two electrons with opposite spins — one spinning clockwise and one anticlockwise — with respect to the direction of the momentum (the yellow arrow). The momentum arrows (on the front) bend and connect with arc segments (on the back) to form closed orbits, that represent the two “lobes” of the figure-8 cyclotron orbit (see Chapter 5).

*To Vanna and to my parents*



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