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Noisy patterns: Bridging the gap between stochastics and dynamics

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Simulations of the deterministic and stochastic Barkley model [103], the code is adapted from [78]. Cover design by Tom Simons – Creative Design.

*The moving power of mathematical invention
is not reasoning but imagination*
– August De Morgan

Shut up and calculate
– Richard Feynman

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