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The effect of thermal fluctuations on elastic instabilities of biopolymers

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on
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Marc groet 's morgens de dingen

*Dag ventje met de fiets op de vaas met de bloem
ploem ploem
dag stoel naast de tafel
dag brood op de tafel
dag visserke-vis met de pijp
en
dag visserke-vis met de pet
pet en pijp
van het visserke-vis
goeiendag*

Daa-ag vis

*dag lieve vis
dag klein visselijn mijn
— Paul van Ostaijen*

