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# Formalizations *après la lettre*

Studies in Medieval Logic and Semantics

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# Formalizations *après la lettre*

Studies in Medieval Logic and Semantics

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For Reinout and Marie  
À memória de meu pai



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