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## Foam Rheology Near the Jamming Transition

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# Foam Rheology near the jamming transition

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in 1984

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