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## Dislocations in stripes and lattice Dirac fermions

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# Dislocations in Stripes and Lattice Dirac Fermions

Andrej Mesaroš



# Dislocations in Stripes and Lattice Dirac Fermions

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TER VERKRIJGING VAN DE GRAAD  
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*Mojoj porodici*



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