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Structure, shape and dynamics of biological membranes.

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Structure, shape and dynamics of biological membranes

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