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A fixed point approach towards stability of delay differential equations with applications to neural networks

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A fixed point approach towards
stability of delay differential equations
with applications to neural networks

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