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## Statistical modelling of repeated and multivariate survival data

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STATISTICAL MODELLING  
OF  
REPEATED AND MULTIVARIATE  
SURVIVAL DATA

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# Statistical Modelling of Repeated and Multivariate Survival Data

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door

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geboren te Montpellier, Frankrijk,  
in 1973

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